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Towards a Classification System of Manufacturing Objects for the Evaluation of Perception Systems

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1 Introduction

The objective of the Robot Perception for Identifying and Locating Parts for Assembly Project is to develop test methods to evaluate perception systems used for identifying and locating unfixtured manufacturing parts under static conditions. System evaluation often involves testing the system under various conditions to determine the influence of different factors on system performance. The dimensionality of the problem is very large, including the nature of the perception system, the manufacturing application, the environmental conditions, the requirements for identification and location accuracy, and the nature of the parts. Therefore, robust test methods need to be developed that would enable evaluation for as wide a range of factors and perception systems as possible.

The evaluation of perception systems requires the use of parts or objects. However, manufacturing parts cover a wide array of parts from small parts (e.g., nuts) to large parts (e.g., airplane wings), from parts made of plastic to parts made of titanium, from parts that are flexible to parts that are rigid, and from parts that are simple (e.g., simple geometric shapes such as spheres or boxes) to parts that are very complex in shape (e.g., engine blocks). Thus, the selection of representative objects is a crucial task.

A solution to this task was to develop a part/object classification system. An object classification system will allow for the evaluation of perception systems based on objects in a particular class, and this may eventually lead to the development of standard reference artifacts of objects in the various classes.

A classification system will allow vendors to accurately specify the advantages and limitations of their systems for the different classes of objects. Such a system will also allow users to determine if a particular system would work for their specific application/object prior to making a large capital investment in the equipment, to compare various perception systems, and to have confidence in the perception system.

Manufacturing parts are naturally classified by application, material, fabrication method, function, manufacturer, and other characteristics. This study looks at commonalities in shape across natural categories, so the classification criteria may group flat parts whatever the function or fabrication method. This study focused on object shape as could be described in a computer-aided design (CAD) file, rather than taking into account surface finish for multiple reasons. Parts found under the hood of an automobile are typically kept in natural finish since their appearance is not critical. For identification, color is an obvious and powerful cue and can be easily considered after shape. The same is true of labels or heavily marked texture; and shape is key for localization and pose determination whatever the surface finish.

For the purpose of evaluating perception systems, parts can be classified by the strength of their features likely to be useful for perception, or more generally by a grading from easy to difficult to perceive. This study uses both approaches. A classification system that encompasses all manufacturing parts would be beyond the scope of this project. To keep within the project and program objectives, the scope for the classification system was narrowed down to automotive parts. Publically available CAD models were used to classify shapes manually and by numerical algorithms. A number of shape metrics were considered for classification, and a subset selected for implementation and testing.

This report documents the efforts involved in trying to develop an object classification system for evaluating perception systems. As part of the development of an object classification system, this study reviewed previous publications that classify parts from the shape retrieval literature. This limited review is presented in Section 2 of this report. Section 3 describes some concepts that were explored or discussed when developing a classification system. Also presented in Section 3 are the metrics that can be used to characterize an object. The selection of the objects used in the classification system is presented in Section 4. Descriptions of the metrics used in this report and the how they were computed are given in Section 5. Section 6 presents the three approaches for manual classifications and an algorithmic-based approach for classification. Section 7 presents findings from the classifications and a summary.

2 Literature Review

A literature review was conducted to determine existing object classification systems. The goals of many of the classification systems are for object retrieval from a database and for manufacturing systems/processes (McCarthy, 1995) (e.g., Group Technology). Classifications can be based on the part appearance and/or shape, manufacturing process to create the part, or the function of the part. There has been much research on this topic especially in the field of computer vision and pattern recognition. In the past decade, there has been an increase in interest in object retrieval in the mechanical engineering domain in part due to the widespread use of CAD and the large number of CAD models available. However, there is limited work on three-dimensional (3D) shape searching for engineering and CAD applications. The remainder of this section will summarize research and/or concepts that are relevant to 3D shape searching for engineering and CAD applications. Of particular interest are the metrics and methods discussed in these studies.

2.1 Tangelder and Veltkamp (2008)

Tangelder and Veltkamp (2008) conducted a survey of 3D shape retrieval methods. In the paper, shape matching methods are divided into: feature based methods, graph based methods, and geometry based methods.

Feature based methods depend on measuring and comparing features and are based on pure geometry of the shape. These methods can be sub-divided into:

1. Global features: global features characterize the global shape of the 3D model. Examples of these features are volume of the model, volume-to-surface ratio, area, the Fourier transform of the volume, or the boundary of the shape. A disadvantage of this method is that it does not discriminate object details well.
2. Global feature distribution: Instead of comparing global features, this method compares distributions of global features. Shape distributions are compared based on properties such as distance, angle, area, volume between random points, and shape histograms using the principal axes of inertia of the model (e.g., moment of inertia about the axis, average distance from the surface to the axis, variance of distance from the surface).
3. “Spatial maps are representations that capture the spatial location of an object. The map entries correspond to physical locations or sections of the object, and are arranged in a manner that preserves the relative positions of the features in an object. Spatial maps are in general not invariant to rotations, except for specially designed maps.” (Tangelder and Veltkamp, 2008).
4. Local features: This method accounts for surface shape in the neighborhood of points on the boundary of the shape. Metrics for similarity are obtained from mapping of the surface curvature of the object onto a unit sphere, using histograms of shape indices calculated over the entire mesh, and applying semi-local descriptions of object shape centered at points on the surface of the object (3D shape context).

Graph based methods “attempt to extract a geometric meaning from a 3D shape using a graph showing how shape components are linked together. Graph based methods can be divided into three broad categories according to the type of graph used.”

1. Model graphs: Model graph based similarity methods are applicable to 3D CAD solid models and are difficult to apply to natural shapes like humans and animals. The most common “solid model representation methods are boundary representation (B-rep) and constructive solid geometry (CSG).”
2. Reeb graphs: A Reeb graph is defined as “the quotient space of a shape S and a quotient function f . Reeb graphs defined by a geodesic distance are suited for matching articulated objects, but they are sensitive to topological changes. Also, they cannot be applied to arbitrary meshes, because topological problems like missing faces disturb the computation of geodesic distances.”
3. Skeletons: This method uses a skeletal graph that has geometric and topological information. Some researchers have combined global features and skeletal graphs.

“For graph based descriptors the complexity of the exact computation of a metric obeying the triangle inequality prevents practical application.”

Geometry based methods can be categorized into:

1. View based similarity: The premise of this method is that two 3D models are similar if they are similar from all viewing angles.
2. Volumetric error based similarity: This approach is based on “calculating a volumetric error between one object and a sequence of offset hulls of the other object.”
3. Weighted point set based similarity: This method is based “on shape descriptors consisting of weighted 3D points.” Researchers have used weights that are based on the volume of the component, curvature, or sum of squared distances for models aligned in the same coordinate frame.
4. Deformation based similarity: This method “compare[s] a pair of 2D shapes by measuring the amount of deformation required to register the shapes exactly.” Tangelder and Velkamp commented that it would be difficult to implement this method of 3D shape matching.

2.2 Princeton Shape Benchmark – Shilane et al. (2004)

The Princeton Shape Benchmark (PSB) (Shilane et al., 2004) contains a database of 3D models and software tools to compare 3D shape matching algorithms. In the paper, a review of several 3D model databases was conducted and some observations of these databases were made:

- Most previous databases contain a small number of classified models.
- Most databases contain a limited range of objects. For example, some only contain household objects or only vehicles.
- The databases have a wide range of granularities in the classifications. For example “Kitchenware” and “motorcycles with 3 wheels.”
- Many classifications mix function and form. For example, “buildings” and “machine.”

The PSB classification is based mainly on semantic and functional concepts (e.g., furniture and table) and secondly on shape (e.g., round tables). Other potential classifications include: grouping models based on function, grouping based on how they are manufactured (e.g., man-made vs. natural), grouped based on where they are used (e.g., office vs. home vs. outdoors), and grouping based on who uses them (e.g., adults vs. children). The PSB allows multiple classifications – an ASCII file contains a hierarchy of class names; each with a different granularity. For example, three classifications in increasing coarseness would be tables, furniture, man-made. Additionally, the benchmark attaches several geometric attributes to each model such as:

- Center of mass – the average (x, y, z) coordinates of all points on the surfaces of the polygons
- Scale – the average distance from all points on the surface of the polygons to the center of mass
- Principal axes – “eigenvectors (and associated eigenvalues) of the covariance matrix obtained by integrating the quadratic polynomials $x_i \cdot x_j$ with $x_i \in \{x, y, z\}$, over all points on the surfaces of all polygons.”

Of the 12 benchmarks used to compare shape matching algorithms, those of interest are:

- “D2 Shape Distribution (D2): a histogram of distances between pairs of points on the surface [Osada, 2001].
- Extended Gaussian Image (EGI): a spherical function giving the distribution of surface normals [Horn, 1984].
- Shape Histogram (SHELLS): a histogram of distances from the center of mass to points on the surface [Ankerst et al., 1999].
- Shape Histogram (SECTORS): a spherical function giving the distribution of model area as a function of spherical angle [Ankerst et al., 1999].
- Shape Histogram (SECSHEL): a collection of spherical functions that give the distribution of model area as a function of radius and spherical angle [Ankerst et al., 1999].
- Voxel: a binary rasterization of the model boundary into a voxel grid.
- Spherical Extent Function (EXT): a spherical function giving the maximal distance from the center of mass as a function of spherical angle [Saupe and Vranic, 2001].
- Radialized Spherical Extent Function (REXT): a collection of spherical functions giving the maximal distance from center of mass as a function of spherical angle and radius [Vranic, 2003].
- Gaussian Euclidean Distance Transform (GEDT): a 3D function whose value at each point is given by composition of a Gaussian with the Euclidean Distance Transform of the surface [Kazhdan et al., 2003].
- Spherical Harmonic Descriptor (SHD): a rotation invariant representation of the GEDT obtained by computing the restriction of the function to concentric spheres and storing the norm of each (harmonic) frequency [Kazhdan et al., 2003].”

2.3 Iyer et al. (2005)

In Iyer’s et al. (2005) review of 3D shape searching, shape is defined as “all the geometrical information that remains when location, scale, and rotational effects (Euclidean transformations) are filtered out from an object.” Shape searching involves the determination of similarities among 3D shapes. Included in the paper are discussions of:

- global feature-based techniques (e.g., moments, invariants, Fourier descriptors, and geometry ratios)
- manufacturing feature recognition-based techniques for CAD models
- graph-based techniques (e.g., B-Rep graph, Spectral graph, Reeb graph, skeletal graph)
- Histogram-based techniques - sample points on the surface of the 3D model and extracted characteristics from the sampled points.
 - o Shape histogram
 - Shell model – “The space is decomposed into concentric shells around the center point. This representation is independent of rotation.”
 - Sector model – “The space is decomposed into sectors that emerge from the center point of the model.”
 - Spiderweb model – a combination of the Shell and Sector models.
 - o “Shape distribution represent the shape signature as a probability distribution sampled from a shape function measuring the geometric properties of a 3D model”
 - A3: Measures the angles between lines joining three random points on the surface of a 3D model.
 - D1: Measures the distance between a fixed point and a random point on the surface.
 - D2: Measures the distance between two random points on the surface.
 - D3: Measures the square root of the area of the triangle formed by three random points on the surface.
 - D4: Measures the cube root of the volume of the tetrahedron formed by four random points on the surface.
- Product information-based techniques – designed specifically for engineering parts. “Part designs are described either based on their manufacturing attributes or on their geometry.”
 - o Group technology (GT) – “coding and classification schemes attempt to capture design and manufacturing attributes such as the main shape and size features of the product, production quality, and material.”
 - o Section image-based – uses 2D silhouette of parts or sections for similarity comparison.
- 3D object recognition-based techniques
 - o Aspect graph – consists of a multiple 2D views of a 3D model of the object as seen from various regions on a sphere encompassing the object.
 - o Extended Gaussian images (EGI)
 - o Geometric hashing – a 3D object is broken down into basic geometric features such as surface points. A set of basis points are chosen and the coordinates of all other points are determined based on the basis points and are stored in histograms. This process is repeated for other basis sets.

2.4 Corney et al. (2002)

Corney et al. (2002) proposed three convex-hull based indices as coarse filters in preliminary steps in the shape matching of 3D engineering data which supports the internet-based search engine ShapeShifter. Factors in selecting these indices include:

- the ability of the search engine to identify similar shapes independent of size

- filters that resulted in an almost complete set of correct candidates (i.e., filters did not eliminate correct candidates)
- Shapeshifter employs several metrics based on the model's convex hull

Other metrics calculated in ShapeShifter include volume, surface area, aspect ratios (of an axis-aligned bounding box), crinkliness, compactness, number of facets, number of holes, and convex hull. Corney et al. used four dimensionless ratios based on the hull as filters to assess their sensitivity to object variations (scaling, taper, twist, feature removal, and fits in a 100 x 100 x 100 box):

- Bounding box aspect ratio: ratio of the longest edge to the shortest edge
- Hull crumpliness: ratio of the object's surface area to the surface area of its convex hull
- Hull packing: proportion of the convex hull volume not occupied by the original object computed as $\left(1 - \frac{V_{model}}{V_{hull}}\right)$
- Hull compactness: ratio of the convex hull's surface area cubed to the volume of the convex hull squared

They found that:

- the bounding box aspect ratio could potentially exclude many potential candidate matches and was thus excluded as a filter,
- hull crumpliness is relatively insensitive to twisting and warps and sensitive to feature removal and non-uniform scaling,
- hull packing is insensitive to all but feature removal, and
- hull compactness is relatively insensitive to tapering, is sensitive to twisting and non-uniform scaling, and insensitive to feature removal.

For the three filters based on the convex hull, the optimal tolerance values were 25 % for compactness, 50 % for packing, and 10 % for crumpliness where optimality is based on minimizing the false-negatives and false-positives.

2.5 Jayanti et al. (2006)

Jayanti et al. (2006) developed a benchmark dataset of engineering artifacts to enable evaluations of various shape descriptors for engineering shape retrieval. Some challenges in developing the benchmark:

- a function-based classification is difficult because parts with similar shapes have different functions
- a classification based on manufacturing process is complicated by advances in manufacturing processes and capabilities which blurs the mapping between form and manufacturing method

The classification of 3D models in the engineering shape benchmark (ESB) is based on shape. The ESB contains 867 3D CAD models in STereoLithography¹ (STL) and Wavefront Technologies' OBJ formats, and is available from <http://purdue.edu/shapelab>. The models are initially put into three super-classes:

¹ Also known as Standard Tessellation Library

- Solids of revolution – part envelope is largely a solid of revolution
- Rectangular-cubic prism or prismatic - part envelope is largely a rectangular or cubic prism
- Thin-walled – parts with thin-walled sections and shell-like components

These super-classes were then further divided into groups of similar shapes. For example, clusters under solids of revolution included bolt-like parts, container-like parts, cylindrical parts, and discs. The authors used the following shape representations for their benchmarking:

- Feature vector-based methods
 - Moment invariants (MI)
 - Principal moments (PM)
 - 3D spherical harmonics (SH)
 - Surface and area based attributes
 - Surface area and volume (SAV)
 - Surface area to volume ratio (SVR)
 - Crinkliness and compactness (CC)
 - Geometric ratios (GR) – aspect ratios of the bounding box
- 3D shape distribution (3DSD) using the D2 shape measure
- Convex hull histogram (CHH)
- 3D shape histogram – solid angle (SAH)
- View-based representations
 - Light field descriptors (LFD)
 - 2.5D spherical harmonics (2.5DSH)
 - 2D shape distributions (2DSD)

The reader is referred to the paper for detailed descriptions of these shape representations.

Precision-recall curves were used to evaluate these shape representations. “Precision is the ratio of the relevant models retrieved to the retrieval size. Recall is the fraction of the relevant models retrieved for a given retrieval size.” Some conclusions based on the results using the ESB are that the three methods based on 2D views (LFD, 2.5DSH, and 2DSD) consistently outperformed the other methods, with the LFD resulting in significantly better precision compared to all other methods. However, view-based methods require more computation as compared to 3D shape measures. 3D spherical harmonics (SH) perform reasonably well for the prismatic parts and solids of revolutions as compared to other shape representations. In terms of the three super-classes:

- Thin-walled components
 - View-based methods performed better than other methods
 - 3D shape distributions, surface area, and volume performed better than more complex feature vectors – SH, CHH, and SAH
 - SAH performs better for this class than other point-based methods
 - Of the view-based methods (LFD, 2.5DSH, and 2DSD), all three methods performed comparably
- Prismatic parts
 - LFD had significantly high precision for all recall levels

- o 2.5DSH, 2DSD, SH, and SAH consistently performed better than the 3DSD method
- o Topology-based methods did not perform well especially at lower recall values
- Solids of revolution
 - o All view-based methods (LFD, 2.5DSH, 2DSD) performed significantly better than the other methods
 - o 3DSH and CHH performed better than 3DSD

2.6 Cardone et al. (2003)

Cardone et al. (2003) conducted a survey of shape similarity assessment algorithms for product design and manufacturing applications. 3D similarity assessment is described as the generation of shape signatures from the 3D models and comparing them using distance functions; the larger the value, the more dissimilar. The shape signatures should be “representation independent and completely describe the features of the 3D model.” Examples of shape signatures are graphs, vectors, or ordered collections of numeric values. The choice of signatures is dependent on the reason for the similarity analysis. Shape signatures and distance functions should have the following properties:

- Positivity – distance between two CAD models should be non-negative
- Identity (Self-similarity) – if the distance between two CAD models is zero, then the models are the same
- Symmetry – given solid models x and y with shape signatures $S(x)$ and $S(y)$, respectively, a symmetric distance function needs to satisfy:

$$\delta(S(x), S(y)) = \delta(S(y), S(x))$$
- Triangle inequality – given solid models x , y , and z with shape signatures $S(x)$, $S(y)$, and $S(z)$, respectively, the distance function must satisfy:

$$\delta(S(x), S(y)) + \delta(S(y), S(z)) \geq \delta(S(x), S(z))$$
- Invariance – a part may have many different representations; “the shape signature should be invariant with respect to the underlying representation.” The shape signature should also be invariant to any rotation or translation applied to the object.
- Robustness and sensitivity – shape signature should change proportionately to the change in the object. If small changes are magnified and result in the conclusion that similar objects are dissimilar, then the measure is not robust. If there is a large change in the object which results in a small change in the shape signature, then it is not sensitive.
- Computational efficiency

The similarity assessment techniques were grouped into:

- Features: “Feature-based techniques evaluate the shape signature of an object based on the type, size, orientation, number, and other properties of the features and their interactions. Once the features are extracted and their significant characteristics are determined, the comparison is carried out using a suitable distance function.” Disadvantages include that the technique does not consider the gross shape of object and feature interactions complicate feature extraction. Techniques described in paper were developed for product design and manufacturing.
- Spatial functions: “These techniques use shape signatures that are spatial functions. An example of a spatial function is the Gaussian map that maps the set of normals of a solid onto a unit

sphere. The problem of matching and comparing 2D spatial functions defined over unit sphere involves manipulating two degrees of freedom (the two angles needed to align the surface of a sphere). The main challenge in these techniques is to identify the characteristics to be represented using spatial functions and to determine an efficient matching procedure to compare two shape signatures.”

- Local curvature distributions over mesh representations: the signature is the spherical representation of the curvature distribution of 3D surfaces of solids without holes. This technique is useful for applications where curvature is a primary factor. Advantages include that the measure is invariant to translation, rotation and scaling. Disadvantages are the restriction to solids without holes and that accuracy depends on the mesh size – a finer mesh increases accuracy but increases computational time.
- Slope diagram representations: this technique uses the slope diagram representation of a convex polyhedron. It is invariant to translation and rotation but computationally intensive and restricted to convex polyhedra.
- Shape histograms: “These techniques are based on sampling of points on the surface of the 3D models. Several significant characteristics can be extracted from the set of points obtained.” The larger the number of points, the more accurate the representation, but the more expensive it is to compute. These techniques do not satisfy the conditions of identity and symmetry but are useful for detecting gross shape similarity, that is, useful as coarse filters.

Several shape functions were described in the paper but the most robust of these was the D2 shape function.

- D2 shape function “computes the distance between two random points. This function is invariant to rotation and translation and is robust.” The distances between random points are calculated and normalized using the mean distance. “The shape distribution is the histogram that measures the frequency of occurrence of distances within a specified range of distance values.” The distance between the two models is usually computed using the L2 norm.
- Section images: “These techniques use sections of the solids as shape signatures. Solids are sectioned at various places and the sections are then analyzed for similarity. A disadvantage is that the method is not invariant to scaling, translation, and rotation. It is best suited for parts that are rotationally symmetric.”
- Topological graphs: “These techniques use topological graphs as shape signatures. These graphs usually represent the connectivity information of the boundary of the solid such as the adjacency between faces. The nodes and edges of the graph may carry additional information related to the solid model.”
- Shape statistics: Shape comparison techniques commonly use basic geometric properties for coarse comparison between objects. Some commonly used properties are volume, surface area, and convex hull volume. Disadvantages include that the measures do not yield sufficient information for detailed comparison, but can be used as coarse filters.

A table comparing the representative algorithms is given in the paper.

2.7 Bespalov et al. (2005)

Bespalov et al. (2005) used several benchmark datasets to evaluate nine techniques for matching CAD data. CAD models can either be solid models or shape models represented by polygonal meshes. The increasing use of laser scanners has made the generation of polygonal meshes a relatively easy task. The matching techniques evaluated were:

- Shape based
 - Shape distributions (SD) (Osada et al., 2002)
 - Shape distributions with point pair classifications (SD-class) (Ip et al., 2002)
 - Reeb graph comparison (Reeb) (Hilaga et al. 2001)
 - Shape distributions with weight learning (SD-Learn) (Ip et al., 2003)
 - Scale-Space comparison (Scale-Space) (Bespalov et al., 2003)
- Solid based
 - B-Rep techniques
 - Invariant topological vector (ITV) (McWherter et al., 2001)
 - Eigenspace indexing on B-Rep graphs (Eigen-BRep) (Peabody 2002)
 - Feature based
 - Model dependency graph approximate matching (MDG) (Cicirello and Regli 2002)
 - Eigenspace indexing on matching feature interaction graphs (Eigen-Feat) (Peabody 2002)

The k -nearest neighbor classification (k NN) and conventional recall and precision measures were used to evaluate the techniques. Recall and precision were defined as:

$$recall = \frac{\text{Retrieved and relevant models}}{\text{Relevant models}}$$

$$precision = \frac{\text{Retrieved and relevant models}}{\text{Retrieved models}},$$

where

relevant models was “the number of models that fall into the same category as the query model”

retrieved models was “the number of models returned by a query”

retrieved and relevant models was “the number of models returned and that fell into the same category as the query model.”

The datasets used to evaluate the techniques were:

- Synthetic datasets
 - Primitive dataset: 101 cubes, 141 cylinders, 29 tori, and 29 spheres with various deformations.
 - Minor topological variation dataset
 - cube-holes: 16 cubes with different numbers of holes (1 to 4) – some with holes of different radii and some with holes of the same radius

- brick-holes: 11 rectangular box models with 0 to 4 holes of the same size in different locations.
- Actual artifact dataset:
 - o CAD models from the National Design Repository Dataset (<http://edge.cs.drexel.edu/repository/>) were used.
 - Manufacturing classification:
 - prismatic machined (56 models) - machined parts are typically high precision parts made in small batches
 - cast-then-machined (54 models) - cast-then machined parts are typically larger production jobs with less stringent tolerance requirements
 - Functional classification: 70 models total, example functional classes: nuts, gears, screws, springs, linkage arms.
 - o LEGO Dataset – 47 components grouped by appearance: plates, wheels and gears, cylindrical parts, and X-shaped axles.
 - o Variable fidelity dataset – 40 CAD models were used to generate 40 polygonal meshes each of low, normal, and high fidelity (highest number of polygons), i.e., 120 models total.

Some findings and observations from the evaluation:

- The graph and solid based ITV and Eigen-BRep techniques performed best on the cube-holes and brick-holes datasets. Among the shape based techniques, the Reeb graph technique performed best.
- Boundary representations (B-Reps) are more useful than mesh-based representations and improving ways to better use B-Reps for matching would be beneficial
- Based on the precision-recall plots, the manufacturing and functional classifications yielded unacceptable and “mediocre” results, respectively, for all the techniques.

3 Object Classification for Perception Systems

As stated in the introduction, our purpose for developing an object classification is to evaluate perception systems, agnostic to the nature and details of the system. This is different from the purpose of the classification systems developed by most researchers in Section 2, where the intent typically was to develop a perception system or to evaluate specific algorithms. The purpose for the system developed by Jayanti et al. (2006) is closest to our purpose, with an analysis that relates general classes of objects to the effectiveness of particular algorithms.

Ideally, our proposed classification system would put objects into classes where the objects in a class would yield similar results, good or bad, from the performance of a wide selection of perception systems. A particular class of objects might be easy to perceive (e.g., textured boxes), or difficult (highly curved, specular parts). Ideally this would be sensor agnostic, so an easy to perceive class of objects remains easy to perceive across all perception systems, but in practice there will remain dependences on the nature of the sensor and perception algorithm. A passive sensor attuned to color will work well in distinguishing identically shaped but differently colored objects, while a monochrome active sensor attuned to shape may do better with color-less but differently shaped objects. The classification system would then be useful in specifying which class of object is most easily perceived by which type of sensor system.

Several concepts for developing a classification system were considered. These included classification systems based on:

1. Technology of the perception system, such as these examples:
 - a. Laser line scanner
 - b. Machine vision (with one or more cameras)
 - c. Structured light/pattern projection (may be visible or non-visible)
2. Objects with similar features or descriptors
3. *A priori* knowledge of issues for perception systems based on feedback from vendors, integrators, and users on objects that were problematic or not problematic for their perception systems

A logical choice would be classification based on perception system technology, giving up sensor-agnostic classification in return for more effective, technology-specific categorizations. However, this would require acquiring intimate knowledge of the various types of perception systems and the availability and extensive evaluation of these systems to determine the advantages and disadvantages of systems that represented each of the various technologies. Given budgetary and time constraints, a decision was made that, as a first step, the classification system would be based on object characteristics and the authors' knowledge and experience with the various technologies.

The authors felt that a classification system that encompasses all manufacturing objects would not be feasible, and a narrowing of the types of objects was needed. Since the focus of the project was for bin picking applications, it was decided that the classification system would initially be developed for rigid, automotive parts found in the engine compartment and parts in the powertrain. The maximum size of the part/object was therefore set, arbitrarily, to be (50 x 50 x 50) cm.

Given the above discussion, we compiled a set of metrics that were used by other researchers to characterize an object. By metrics we mean features of the object, local or global, that can be used to classify it. When possible, we emphasized quantitative features. The full set of metrics is given in Table C1 in Appendix C. Table C1 has the following information for each metric:

- Feature: Name of feature
- Local feature: a characteristic of the object computed on a limited, local region
- Global feature: a characteristic of the object computed with global support.
- 2D/3D/Both: Whether the feature is primarily two dimensional, three dimensional, or both.
- Shape/Surface: Whether the feature applies primarily to the shape or surface of the object.
- Description: Description of the metric to be computed.
- Relevant or Non-Relevant: Whether the metric is relevant to our classification task, based on the judgment of the project team members.
- Algorithm/software needed? Y/N; Available? This column indicates whether an algorithm or software is required to compute the metric. If an algorithm or software is needed, is it available?
- Source: Reference(s) in which the metric was invented or described.

The metrics were chosen to describe a broad range of perceptual characteristics of objects, including:

- Geometry: metric properties of shape (Table 3.1)
- Topology: relationship of components (Table 3.1)
- Viewpoint projections/appearance: features computed on 2D projections of the part (Table 3.2)
- Surface properties: color, texture and other (Table 3.3)

The metrics do not provide a complete physical description of an object, as mass and material characteristics, aside from appearance, are not included. We were assuming that sensors would be primarily non-contact and utilize visual or near-infrared (IR) wavelengths and not utilize thermal IR bands, sonic wavelengths, magnetic, weight, or other non-visual physical properties. Also, a given shape described by a CAD model can be manufactured from different materials, which can result in different physical properties (including surface reflectance). Our primary goal was to consider those aspects of an object captured by shape encoded in a CAD model and that would be found in the object even if made with different materials.

For the geometric metrics in Table 3.1, we selected a range of object characteristics that could be used either directly as a perceptual feature, or are likely to contribute to the appearance of perceptual features. An example would be whether the object is prismatic, with a number of flat surfaces that might lead to internal visual edges in an image, or rounded, with less likelihood of internal edges aside from folds and limbs. We were inclusive in the metrics, cataloging many with differing amounts of information rather than focusing on a few, high information features. The intent was not to build an efficient perception system, but rather to understand how the metrics might partition the space of objects.

Some geometrical metrics were selected not because they alone represented a visual feature, but because they may indicate the presence of visual features. In a manufacturing application, the problem of object

identification may require relatively simple discriminations, such as between a long thin object and a more compact one, so simple extents would be adequate. Similarly, object density (here not density of mass, but of shape as represented by the ratio between the volume of the object and the volume of its convex hull) could be a marker for relatively hollow objects, like springs, that are likely to have self-occlusions.

Table 3.1. List of Selected Metrics for Object Classification.

	Metric	Metric Measured	Comments
1	Size	X,Y, Z extents	
2	Size	Surface area	
3	Size	Volume	
4	Size	Convex hull	
5	Compactness	Volume/Surface Area	
6	Compactness	Max/Min extent	
7	Compactness	$(\text{Area of Convex Hull})^3/(\text{Volume of Convex Hull})^2$	
8	Density	$1-\text{Volume}/(\text{Volume of convex hull})$	
9	Flatness	Short/Middle extent	
10	Flatness	Middle/Long extent	
11	Prismatic	% surface flat	
12	Curvature	Integrated total curvature	
13	Curvature	% convex, concave, saddle	
14	3D Uniqueness	# significant feature points	Use SURF ² or SIFT ³ to get this metric (Dutagaci et al., 2012)
15	Symmetry	Rotational moments	
16	Symmetry	# axes+type	Mirror, rotational, point
17	Anti-symmetry	Chirality	
18	Smoothness	Hull crumpliness: ratio of object surface area to surface area of its convex hull	
19	Smoothness	Crinkliness: defined as the surface area of the model divided by the surface area of a sphere having the same volume as the model.	
20	Topology	# holes	

Another reason for selection of some metrics is the performance of current perception systems. Many bin picking systems perform well on symmetric objects, such as discs and cylinders. The performance may be related to ease of perception, or ease of grasping, but in either case symmetry is an important metric.

Reviewing the metrics in Table 3.1, the first set (1-10 in Table 3.1) was selected to classify the compactness and extent of the object. The x, y, z extents, surface area and volume are basic measures of the object size, which are not directly useful in perception unless sensor distance or field-of-view is taken into account. Metric 4, convex hull, is also less useful directly but is useful as an intermediate computation for other metrics.

² Speeded Up Robust Features

³ Scale-Invariant Feature Transform

The compactness metrics (5-7 in Table 3.1), as well as the global flatness metrics (9-10), measure ratios that estimate whether the object is compact in all three dimensions (metrics 5-7), or in one dimension and is therefore flat (metrics 9-10). Compactness alone may not be significant in ease of perception, but indirectly may influence other features. A flat object yields fewer possible poses and may result in effectively a 2D shape easy to perceive by traditional machine vision approaches.

The density metric (8 in Table 3.1) measures the open volume of an object. The logic is: if the object is compact and dense, the volume of the convex hull will be close to the volume of the original object and the ratio would be close to 1, so the density measure will be 0. If the object is very open inside, or has long extensions, the volume of the convex hull will be greater than the original volume, so the ratio will be smaller and the density measure larger. A density measure near 1 could indicate a visually hollow object, like a spring, which is likely to have self-occlusions and other distinct visual characteristics. (Some objects may be hollow, like a box or a gas tank, but look solid from the outside – in this case the metric may misfire, or need to be properly interpreted.)

The second set of metrics (11-13 in Table 3.1) was selected to classify surface roundness and curvature. These measures have long been used in object description and perception, but are hard to describe in single numbers for an entire object. Curvature is a local feature (e.g., for a meshed object, the curvature is calculated at a vertex), and an object can have a highly curved element attached to a flat section. We looked for measures that would help distinguish a relatively flat object, like a box, from a highly curved object, like a ball bearing or a section of pipe. Our measures all essentially integrate the local curvature. For prismatic shapes (metric 11), the measure is the percentage of the shape that is locally flat with zero curvature. For more curved shapes we consider metric 12, the integrated total curvature (e.g., for a meshed object, the curvature averaged over all vertices). This is intended to give the average curvature over the entire object. Finally, metric 13 is intended to measure the percentage of the object that is locally convex or concave.

The third set of metrics (14 in Table 3.1) was selected to identify objects with many distinct 3D, high-curvature local features. This would distinguish homogenous objects like a sphere from heterogeneous objects with many local dips, angles, and extensions, like the body of a fuel pump. In this case, there are many different 3D feature measures that could be used, but we determined that most measures would give highly correlated results at the level of discrimination we need. If an object has a large number of distinctive corners or bumps found by one measure, another measure is likely to also find many features even if not the same ones.

The fourth set of metrics (15-17 in Table 3.1) was selected to measure symmetry. Symmetry is a complex concept that can be difficult to quantify on a CAD model, so the metrics were difficult to choose (and compute). Shapes can be symmetric by rotation, by reflection, by a helix, and other mechanisms. To categorize a shape's symmetry, the nature of its symmetries has to be discovered and quantified for imperfect symmetries. We found the symmetry characteristic difficult to quantify and to compute, and did not arrive at metrics we found adequate to fully and appropriately describe symmetry. Still, symmetry can be important in perceptual systems – symmetric objects allow matching by techniques like generalized cylinders, and simple circular shapes admit to fast detectors.

The fifth set of metrics (18-19 in Table 3.1) was selected to measure surface smoothness (roughness), which influences the appearance of color and texture. The two metrics essentially measure the ratio of the

object's surface area to the surface area of an idealized version of the object (convex hull or sphere), and if the ratio is high, the object should have folds or other high-frequency variations in its surface.

The sixth and last class of metrics (20 in Table 3.1) was selected as a marker for topology. The measure we selected was the genus of the surface, or the number of holes invariant to plastic distortions. A sphere has zero, a torus one, and so on. These are holes completely through the object. In this case, we are not certain that the number of holes an object has will be significant in characterizing its appearance. A small, hard-to-see hole drilled through the object will increase the genus just as much as a large, distinguishing hole. We did not select metrics related to the branching or subpart relations of an object, which are sometimes described as topological. These can be complex and are beyond the scope of this study.

The metrics in Table 3.2 were selected to determine the viewpoint-dependent features of an object. There should be some correlation between the viewpoint-independent shape metrics in Table 3.1 and the viewpoint-dependent metrics in Table 3.2, since density, curvature, and smoothness may influence the nature and number of local 2D features in 2D projections. However, we also wanted a direct measure of the number and distinctiveness of 2D features across possible viewpoints. The more distinctive 2D features, the more likely an object can be identified and located in 2D projective sensors (e.g., cameras).

Table 3.2. Metrics Based on Pose or Viewpoint.

	Metric	Metric Measured	Comments
1	Poses	# stable poses	See Yee, Wan, Ventura 2001
2	Unique views	Visually distinguishable poses	
3	2D Uniqueness	# significant 2D feature points	

However, the metrics in Table 3.2 require considerable effort to compute. To properly do so, many views of the object have to be systematically produced, with the views simulating the camera or sensor of interest, and each view analyzed for the number of distinct feature points. Similarly, to determine the number of stable poses requires a physical simulation of the object. Also, the simulated 2D views will change if the object has texture.

The metrics in Table 3.3 are material, color, texture, and reflectivity. These were selected for their obvious influence on object appearance. However, we did not emphasize these in the study for a few reasons. The first is that CAD models do not typically represent inherent surface properties, so shape is paramount. The second is that in manufacturing assembly, many parts do not have distinctive texture or color. They can be machined metal or texture-less plastic, used in internal assemblies where markings are not essential. The third is that surface textures can be arbitrary and highly varying, such as a single shape of a soft drink can that may be printed with many variations of logos and brand names. Finally, object appearance can vary over the object, face by face or section by section – should objects be classified on average appearance, maximum texture, a histogram of color or texture metrics, or some other way? Classifying appearance and textures for ease of perception would be another complete study. Finally, once color or texture is introduced into perception for a manufacturing application, there are likely to be existing, successful machine vision approaches for object identification.

Table 3.3. Surface Appearance Metrics.

	Metric	Metric
1	Reflectance	Bidirectional reflectance distribution function (BRFD)
2	Object material	As given in object description
3	Color	Metric is appropriate color or radiometric space; possibly sensor dependent
4	Texture	Many possible structural, statistical and power spectrum metrics

4 Creation of an Object Database

The calculation of the proposed metrics for an object requires a 3D representation of that object. An initial strategy was to try to obtain CAD models of engine parts (from older or discontinued auto models) from the various automobile manufacturers or from free sources on the web. Both Ford Motor Company and General Motors were contacted, and unfortunately, this strategy was not viable due to proprietary issues. The latter option of finding engine parts on the web required developing a list of engine part names and few, free CAD models of engine parts were found.

An alternative was to use the models available in the Purdue Engineering Shape Benchmark (ESB) (<https://engineering.purdue.edu/cdesign/wp/>) database that were deemed similar to engine parts. The database contained images of the part, an OBJ file for the part, and a mesh of the part in STL format. A subset of about 200 objects from the over 900 objects were selected from the ESB database. Metrics based on geometry were calculated for the selected parts. However, the results from the curvature algorithm did not yield rational results. The reason for this was because a finer mesh was required. An attempt was made to create finer meshes of the parts using the OBJ files of the objects that were available from the Purdue ESB database, but we were unable to open these files with any of the commercially available software that we had.

As a result, another web search of freely available CAD models was conducted. This search yielded over a hundred parts from the following website: www.GrabCAD.com. The restriction of parts associated with automobile engine parts and the availability of usable file formats (i.e., file formats for which the authors had software to open the files), limited the selection of objects. As stated in Section 3, objects that fit within a (50 x 50 x 50) cm volume were used in the analysis.

Another option that arose was the purchase of CAD models, such as of an automotive engine. However, there were a few drawbacks to this option: cost, procurement time, and type of file. The cost was not prohibitive as CAD models of an engine are available for about \$600. The files for the parts were meshed files, and they did not appear to be fine meshes. This issue may have been resolved by requesting the polygonal models of the parts, which would allow us to re-mesh to finer meshes, but we did not get a response from the creator of the mesh files.

Therefore, the objects used for testing the metrics and classification system were those obtained from the GrabCAD website and are given in Appendix A. One hundred and thirty-three (133) objects were downloaded; however, two of the objects could not be meshed and curvature metrics could not be performed for another 15 of the objects. There are some known bugs in the curvature algorithm and

further debugging of the algorithm was not pursued as this was beyond the scope of this effort. This reduced the object database to 116. Six of the objects had at least one dimension larger than 50 cm. These objects were left in the database as it did not have a significant effect on the manual classifications or the cluster-based classifications. However, when plotting the metrics for the High/Low observations, the metrics for the six oversized objects were excluded; thus, these observations were based only on objects that were (50 x 50 x 50) cm or smaller.

5 Computation of Metrics

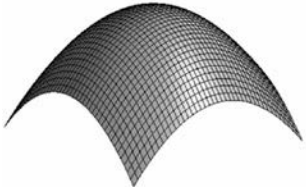
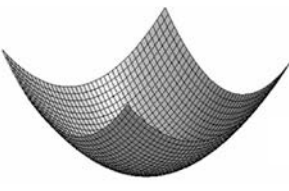
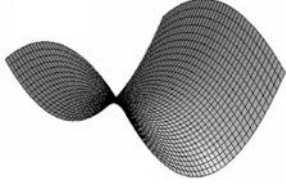
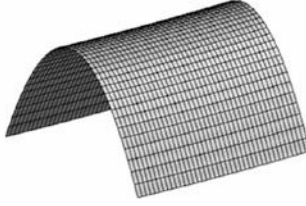
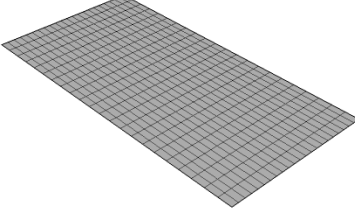
Different metrics characterizing an object were computed using a triangulated mesh of the object. Meshes of the objects, in STL format, were created from CAD models of the objects. The STL files were then converted to PLY (Polygon File Format) files. A direct generation of PLY files from the CAD models was not done as the generated PLY meshes were not always triangulated. The conversion from STL to PLY format was done to remove duplicate nodes.

The mesh files (in PLY format) were processed using a custom script written in MATLAB. Some functions used in the script were downloaded from the publicly available *toolbox_graph* which contains procedures for processing mesh data, http://www.mathworks.fr/matlabcentral/fileexchange/5355-toolbox-graph/content/toolbox_graph/html/content.html (last accessed: 08/30/13). Below are two lists of metrics: a list of primary characteristics calculated directly using the mesh of an object and a list of characteristics derived from the primary characteristics. Each metric is briefly described below.

A. Primary characteristics

- 1) Total surface area of an object: this is the sum of the areas of all triangles. The area of a single triangle was calculated as one half of the length of the cross product of two vectors forming two sides of a triangle. NOTE: the surface of the selected objects (see Section 4) had to be represented by one continuous and closed mesh. This restriction excludes CAD models of objects built from distinct subcomponents with more than one surface.
- 2) Total volume of an object: the algorithm is based on the method described in Zhang and Chen (2001). NOTE: the function which calculates the volume assumes that all normals are correctly oriented, i.e., pointing outward.
- 3) X, Y, Z extents (DX, DY, DZ): The maximum extents along the x-, y- and z-axes in which the CAD model was created. NOTE: the three extents are not necessarily equal to the dimensions of the bounding box containing the object. However, in most cases, the coordinate frame of the CAD model is aligned with the natural directions associated with the object, e.g., axes of symmetry or three longest edges.
- 4) Area of the convex hull. The MATLAB function *convhull()* was used to generate a mesh representation of the convex hull of the object. The total surface area of the convex hull was then computed using the same procedure used to compute the total surface area.
- 5) Volume of the convex hull. The same algorithm used to compute the total volume was used on the mesh created with MATLAB function *convhull()* to obtain the convex hull volume.
- 6) Fraction of an object's surface area having a given shape type. Shape type is determined from the principal curvatures (c_{min} , c_{max}) computed at a node. The principal curvatures for the six shape types are given in Table 5.1. In Table 5.1, the notation within the parentheses indicate whether (c_{min} , c_{max}) are positive, negative, or zero.

Table 5.1. Shape types and associated principal curvatures.

 Cap (+, +)	 Cup (-, -)	 Saddle (-, +)
 Ridge (0,+)	 Rut(-,0)	 Flat (0,0)
The above images were obtained from http://radiographics.rsna.org/content/22/4/963/F18.expansion.html.		

The curvature tensor was calculated by calling the function *compute_curvature()* from *toolbox_graph*. This function calculates the tensor at every vertex. Then, the curvature tensor for a triangle is calculated as the average of the tensors for the three vertices that define the triangle. The shape type of a triangle is determined by the average tensor. The area of all triangles with the same shape type are summed up and normalized by the total surface area of the object. The algorithm for calculating the curvature is based on the method developed by Alliez et al. (2003) and Cohen-Steiner and Morvan (2003). The method calculates the angular difference between the normals of all triangles which share the same vertex for which the curvature tensor was calculated.

NOTES: i) The computed curvatures will likely not have values exactly equal to zero, i.e., a flat surface. Therefore, a parameter called the flatness threshold was defined to determine whether the vertex was on a flat region or not. A meshed cube, sphere, and cylinder were used in simulations to determine a value for the flatness threshold. Based on the simulations, the flatness threshold value was set to 0.001. ii) Principal curvatures have dimension of (1/length) and are sensitive to scale. However, the function *compute_curvature()* outputs results which are scale invariant because the code normalizes the length of each triangle edge by the average length of all edges (for example, the curvatures of a sphere do not depend on the radius of a sphere). Normalization does not affect the shape type classification – in fact, normalization bounds the calculated curvatures for all the objects in a narrow range, making it easier to determine the flatness threshold. iii) The function *compute_curvature()* may sometimes fail as it did in 15 of 131 cases. The reason for this is unknown and this bug was

reported a few years ago but was not fixed⁴. iv) Since the mesh obtained from a CAD model does not contain any noise (only discretization error due to meshing), the parameter *option.curvature_smoothing*, in the function *compute_curvature()*, was set to 1. Basically, this means that no averaging was applied.

- 7) Total length of sharp edges. An edge is classified as sharp if the directions of the two normals of the adjacent triangles differ by more than 45°. The reported value is the sum of all sharp edges divided by the sum of the maximum extents (calculated in 3 above). Although, this metric is not in Table 3.1, we could easily calculate this metric since we calculated the shape type in (6) and we felt that it could be a useful metric. For laser-based perception systems, a higher value for this metric may indicate potentially noisier data due to edge effects (i.e., splitting of the laser beam at edges).

NOTE: normalization makes the comparison between different objects scale invariant, for example the normalized length of a cube is 4, regardless of the size of the cube. The normalized lengths for some geometrical primitives are given in Table 5.2.

Table 5.2. Normalized length of sharp edges for some geometrical primitives.

Geometrical primitive	Value
Sphere	0
Cube	4
Cylinder with diameter D and height H	$\frac{\pi}{\left(1 + \frac{H}{2D}\right)}$
Cylindrical ring with inner diameter D_{in} , and outer diameter D_{out} , and height H	$\frac{2\pi \left(\frac{D_{in}}{D_{out}} + 1\right)}{\left(2 + \frac{H}{D_{out}}\right)}$
Circular cone with diameter D and height H	$\frac{\pi}{\left(2 + \frac{H}{D}\right)}$
Square pyramid with side L and height H	$\frac{4 \left[1 + \sqrt{\left(\frac{H}{L}\right)^2 + 0.5}\right]}{\left(1 + \frac{H}{L}\right)}$

B. Derived characteristics

- 1.) In the literature, we found three definitions for compactness (we used all three definitions in this study):
 - a. Volume/Surface area

⁴ See <http://stackoverflow.com/questions/12922419/rectifying-compute-curvature-m-error-in-toolbox-graph-in-matlab> and <http://www.mathworks.com/matlabcentral/fileexchange/5355-toolbox-graph>, Post 03 Mar 2009 by David S.

- b. Max extent/Min extent
 - c. $\text{Convex hull area}^3 / \text{Convex hull volume}^2$
- 2.) Density = $(1 - \text{object volume} / \text{convex hull volume})$
- 3.) Smoothness
 - a. Hull crumpliness = $\text{Object surface area} / \text{Convex hull area}$
 - b. Crinkliness = $\text{Surface area} / (\text{Surface area of a sphere with the same volume as the object})$
- 4.) Aspect ratio
 - a. DX/DY
 - b. DX/DZ
 - c. DY/DZ

The above metrics were calculated for all the objects in Appendix A and the calculated values are tabulated in Appendix B. In Table B1, the summation of the values for Cap, Ridge, Cup, Flat, Saddle, and Rut should equal 1 as the values represent the fraction of the object that is considered to be cap, cup, flat, ridge, rut, or saddle.

The metrics associated with symmetry were not computed because we could not find algorithms to adequately quantify symmetry. We also felt that the reason symmetry is important to perception is because objects that are more symmetric result in more pose ambiguities than asymmetric objects. Therefore, the metric “unique views” would be able to capture that aspect of an object without having to compute the “symmetry” of the object. Also, the number of significant features was not computed due to time constraints. Topological features such as the number of holes was also not obtained due to:

- Definition of a hole: would a hole that did not go entirely through the object be considered a hole? For perception systems, an incomplete hole can appear the same as a through hole, but topologically is not the same.
- Size of hole. If a perception system could not identify a hole due to poor resolution, or the hole is not readily sensed from the exterior, then would the number of holes be a relevant metric?
- Hole count is global. The topological number of a shape is a global feature that may not be sensed from any particular sensor view.

6 Classifications

There were several different methods used to classify the objects in the database given in Appendix A using the metrics described in Section 5. The two main methods for classification used in this work were manual (Section 6.1) and algorithmically-based (Section 6.2). Since classification methods rely on a set of parameters to characterize an object, a manual classification system was felt to yield a better system since it is difficult to develop classifiers that encompassed prior knowledge, experience, and intuition. However, this method is very subjective and may be difficult for more complex objects, which may create ambiguities when determining how to classify an object. An algorithmically-based method would be more objective but requires time and effort to develop.

6.1 Manual Classification

Three approaches were considered for the manual classifications. These approaches are described in the following sub-sections.

6.1.1 Geometric Approach

This approach involves classifying objects based on their geometry where similar shaped objects were put into the same class. The objects were grouped based on viewing a 2D image of the object and other information regarding scale or size was not considered. The obvious drawback to classifying objects based on geometry is that many objects are a combination of various basic geometric shapes and judgment will have to be depended upon.

The objects from the database were placed into six classes, A to F, and the groupings are given in Table 6.1. In general, the objects in Classes A to F consisted of:

- Class A - flat and thin (high aspect ratio) objects; objects that were “2D” or planar
- Class B – gears, wheels, or round objects
- Class C – bulky or block-like objects
- Class D – rounded/curved objects that did not fit into Class B
- Class E – objects made with flat, thin material; objects similar to Class A but that are “3D” (e.g., bracket). Objects in this class are also more angular than those in Class D.
- Class F – cylindrical or tubular type objects

Once the classification was performed, bar plots of each metric (surface area, volume, etc.) were generated. Two of these plots are shown in Figure 6.1. The plots were made to determine if there was any clustering of the metrics for a given class. For example, from visual inspection, two general observations based on Figure 6.1 are that, on average, objects in Class C have higher volumes, and that the compactness (defined as the ratio of maximum extent to minimum extent of an object) for objects in Class A were higher than those in the other classes. These observations are noted in Table 6.1. An observation of High/Low was made only if it was clearly evident in the plot; if there was no clear evidence, no observation of High/Low was noted for the metric (see Figure 6.2). As this is a visual observation, the determination of High/Low is subjective. These plots were generated for all classifications – manual and algorithmic based.

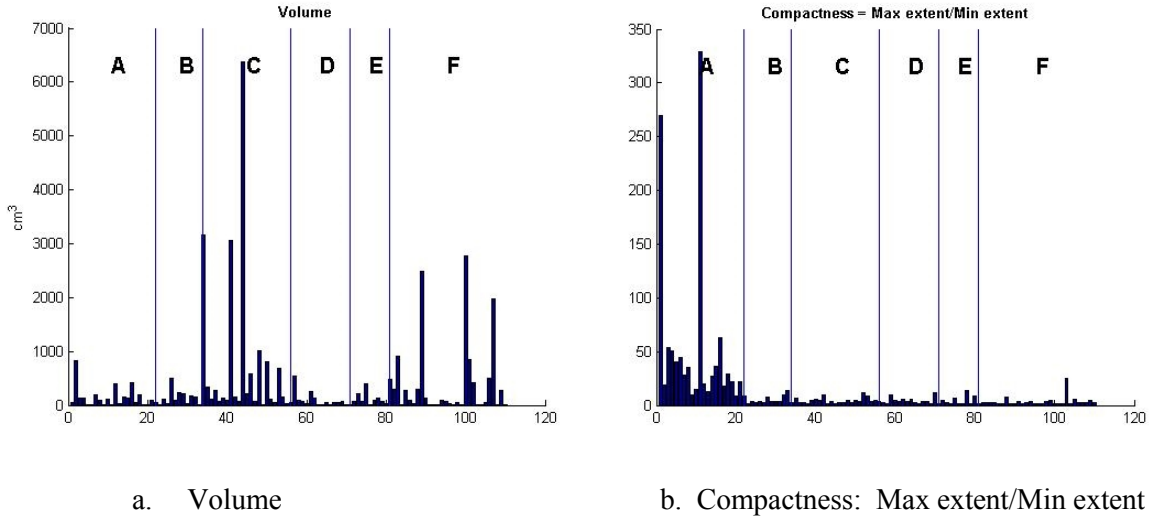


Figure 6.1. Plots of (a) Volume and (b) Compactness for objects in classes A to F.

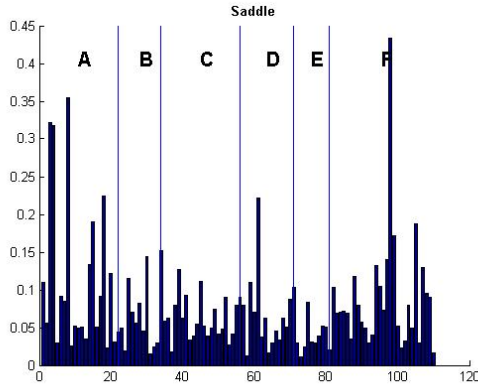
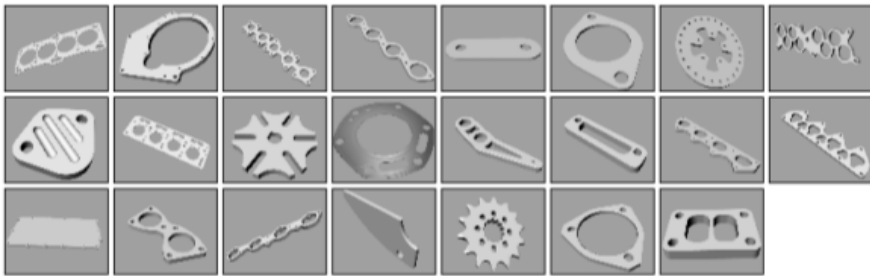
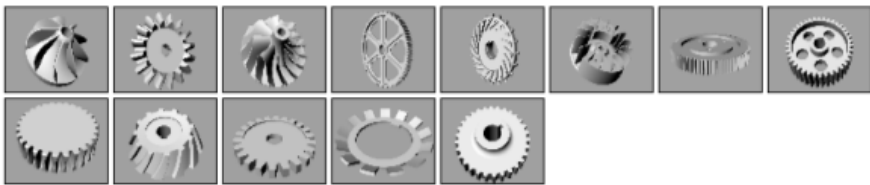
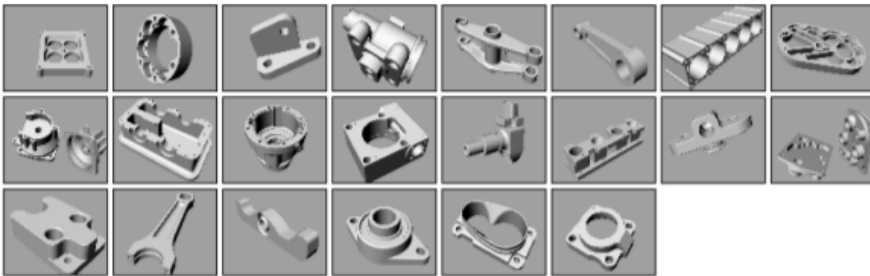
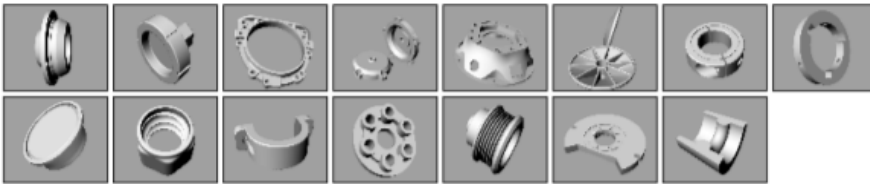
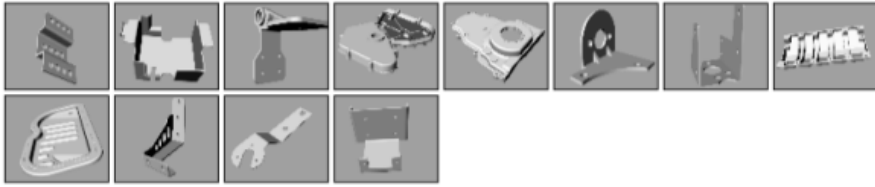


Figure 6.2. Plot of the Saddle metric shows no clear indication of High/Low for a given class.

An objective way to determine whether a metric was High/Low for a given class would be based on the comparison of the statistical averages for each class for a given metric. However, the standard deviations of the average for many of the classes are large (in some cases extremely large) indicating that the observations based on the average would not be statistically significant. Thus, this method was not used.

Table 6.1. Classification based on object geometry.

Class A (thin, flat objects – “2D” objects) 	HIGH: • compactness (max/min extent) • compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) • aspect ratio LOW: • crumpliness • ridge • cup
Class B (gears, wheels, round objects) 	HIGH: • length of sharp edges LOW: ---
Class C (bulky or block-like objects) 	HIGH: • surface area • volume • convex hull volume • compactness (volume/surface area) • cup LOW: ---
Class D (round objects that did not fit in Class B) 	HIGH: --- LOW: • volume

Class E (thin, flat objects that are “3D”) 	HIGH: • convex hull volume • density • crinkliness • flat LOW: • compactness (volume/surface area) • ridge • saddle • rut • cup
Class F (cylindrical, tubular objects) 	HIGH: • volume • convex hull volume • cap • ridge • cup LOW: • flat

6.1.2 Laser-based Technology Approach

This approach grouped the objects in the database based on how difficult it would be for a particular type of perception system to obtain the pose of the object given certain conditions. The objects were placed into one of five levels (i.e., 5 classes) of difficulty as follows:

Levels of Difficulty

- 1 – Very Easy: All 6 DOF (degree of freedom; 3 positional and 3 rotational) can be obtained with relatively high accuracy
- 2 – Easy: All DOF can be obtained, but with relatively low accuracy
- 3 – Medium: Only 4 or 5 of the DOF can be obtained with relatively high accuracy
- 4 – Hard: Only 4 or 5 of the DOF can be obtained, but with relatively low accuracy
- 5 – Very Hard: Only the 3 positional DOF can be obtained

In order to aid in gauging the difficulty of measuring an object’s pose using a certain perception system, three additional metrics were defined for an object: 1) *Pose Unambiguity*, 2) *DOF Needed*, and 3) *Ambiguous DOF Needed*. Definitions for these metrics and possible values for them are presented below.

Pose Unambiguity: Measure of how many degrees of freedom can be determined unambiguously for an object when all relevant features are visible.

- 3 – Only a 3DOF position can be calculated unambiguously
- 4 – Only a 4DOF pose can be calculated unambiguously
- 5 – Only a 5DOF pose can be calculated unambiguously
- 6 – No ambiguity, full 6DOF pose can be obtained unambiguously

DOF Needed: Number of degrees of freedom that must be calculated in order to properly assemble the object into a larger assembly. Although in some cases, some of the degrees of freedom may remain ambiguous (e.g., differentiating between the front and back face of a flat washer) that degree of freedom may still need to be calculated in order to assemble the object (e.g., an assumption must be made about which is the front side of a flat washer in order to calculate its two angles of rotation which will allow a robot to insert a screw through it).

- 3 – Only a 3DOF position must be calculated (e.g., ball bearing)
- 4 – 4DOF must be calculated
- 5 – 5DOF must be calculated
- 6 – All 6DOF must be calculated

Ambiguous DOF Needed: Number of ambiguously-defined DOF that need to be calculated. This is the difference between *DOF Needed* and *Pose Unambiguity*.

For each object in the database, values for the above three metrics were first assigned.

Perception Systems

For this approach, the perception systems for which the object pose determination difficulty would be gauged had to be defined. To do this, a perception system was defined as a combination of four factors:

1) technology, 2) clutter, 3) background, and 4) presentation. Definitions for these four factors and possible values for them are explained below.

Technology: Sensor hardware is based on:

- 1) a laser line scanner mounted on a 6DOF arm,
- 2) a multiple camera machine vision system in which one or more of the cameras are mounted on a 6DOF arm,
- 3) a structured light area scanner mounted on a 6DOF arm, or
- 4) a combination of laser line scanner, structured light area scanner and machine vision in which the object is manipulated with a gripper in order to present the object more favorably to one or more of the sensors.

Clutter: Object is 1) isolated or 2) there are other identical objects in the field-of-view of the sensor(s).

Background: Object is 1) on a flat surface or 2) in a bin.

Presentation: Object is presented to the sensor(s) 1) in a favorable orientation or 2) with important features occluded.

Using the above factors, a perception system may be described using four numbers. For example, *System 1111* means a perception system using a *laser line scanner* to determine the pose of an *isolated object* on a *flat surface* presented in a *favorable orientation*. Similarly, a *System 1221* means a perception system using a *laser line scanner* to determine the pose of an *object in a bin with other identical objects*, and presented in a *favorable orientation* (e.g., at the top of the pile anywhere in the bin with relevant features visible).

Assumptions

In order to gauge the difficulty of a certain perception system's ability to determine the pose of an object, several assumptions regarding the object, its environment, and the perception system itself were made.

These assumptions are presented below.

1. The object is stationary.
2. The object material, color, and texture are favorable to the technology being used.
3. Lighting conditions are favorable to the technology being used.
4. The environment is stable throughout the perception task.
5. Perception systems that are based on machine vision technologies have a higher resolution than those that are based on laser line scanning technologies and therefore, can more accurately measure the poses of smaller objects.
6. Perception systems that are based on laser scanning technologies can more accurately measure the pose of volumetric objects (i.e., objects with features in all three dimensions as opposed to flat objects) than perception systems that are based on machine vision technologies.
7. Perception systems that use structured light area scanning technologies or a combination of laser line scanning and machine vision inherit the best characteristics of the laser line scanning- and machine vision-based perception systems.
8. All the perception systems use optimized algorithms (e.g., data processing, filtering, fitting, etc.) in order to calculate the poses of objects using the raw sensor data.
9. Perception systems that use laser line scanning and structured light area scanning technologies yield more accurate poses of objects that are presented among many other identical objects (i.e., cluttered background) because it is easier to isolate (segment) the data from a single object among many identical objects using 3D data.

Placing the object in a bin with other identical parts and in a favorable orientation adds one level of difficulty to each kind of perception system used with the same object isolated on a flat surface.

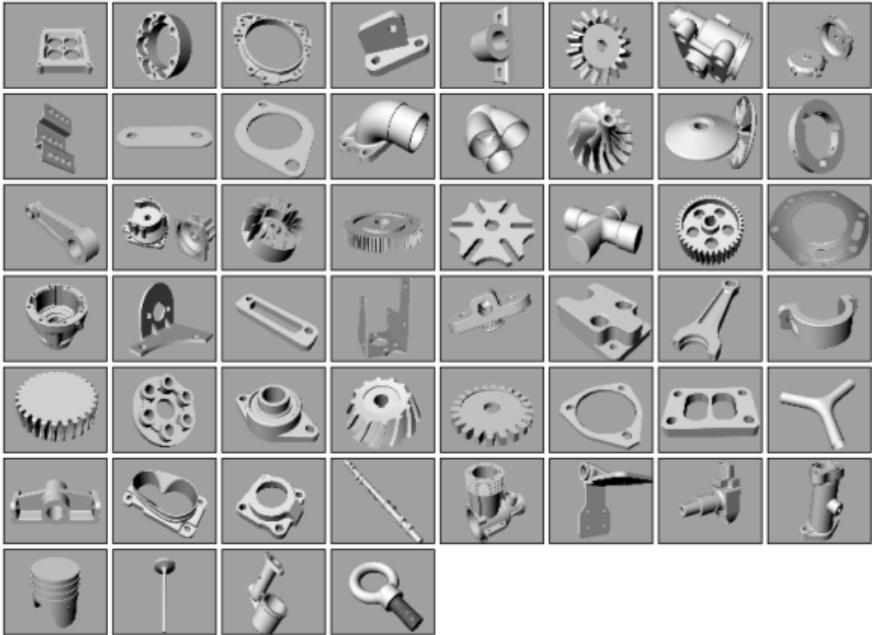
Theoretically, the above method can result in many possible combinations of factors, which could define a large number of perception systems. For the purposes of this classification, only six different *systems* (1111, 1221, 2111, 2221, 3111, and 3221) were considered. For Presentation, only the case of favorable orientation (represented by the fourth digit in the nomenclature with a value = 1) was used as the alternative of 2 (important features occluded) would yield numerous classifications depending on which features were occluded.

The classification for Systems 1111, 2111, and 3111 are given in Tables 6.2 to 6.4. Systems 1221, 2221, and 3221 are not shown as they are similar to Systems 1111, 2111, and 3111, respectively; the only change being the difficulty levels for 1221, 2221, and 3221 were increased by 1 (i.e., the classes increased

by 1). No difficulty level was higher than Class 5 – Very difficult. For example, for System 1111, two objects were placed in Class 5. For System 1221, this meant that the difficulty level would have been Class 6, but since Class 5 was the highest level, these two objects in Class 5 for System 1111 were placed into Class 5 for System 1221.

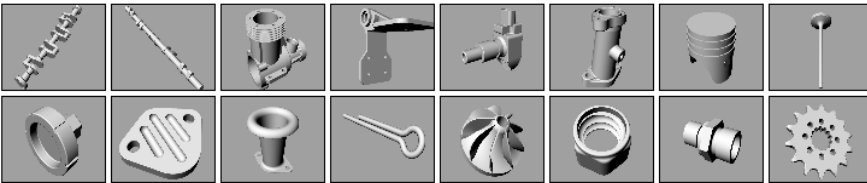
As mentioned earlier, High/Low observations were made based on bar plots of each of the metrics. However, in a couple of classes (System 1111 - Class 5 and System 3111 - Class 3), there were only two objects in that class. Therefore, the addition of one or more objects could potentially reverse or nullify the High/Low observations, i.e., these observations have a low level of confidence associated with them.

Table 6.2. Classification for System 1111: Technology = laser line scanner mounted on 6DOF arm, Clutter = isolated, Background = on flat surface, Presentation = favorable orientation.

System 1111: Class 1 – very easy 	HIGH: • surface area • volume • convex hull area • convex hull volume • compactness (max extent/min extent) • compactness (CH area³/CH volume²) • aspect ratio LOW: ---
System 1111: Class 2 – easy 	HIGH: • aspect ratio LOW: ---

System 1111: Class 3 - medium 	HIGH: --- LOW: ---
System 1111: Class 4 – hard 	HIGH: --- LOW: • surface area • volume • convex hull area • convex hull volume • compactness (volume/surface area) • compactness (max extent/min extent) • compactness (CH area³/CH volume²) • aspect ratio
System 1111: Class 5 – very hard 	HIGH: --- LOW: • surface area • volume • convex hull area • convex hull volume • compactness (volume/surface area) • compactness (max extent/min extent) • compactness (CH area³/CH volume²) • aspect ratio

Table 6.3. Classification for System 2111: Technology = multiple camera machine vision system in which one or more of the cameras are mounted on a 6DOF arm, Clutter = isolated, Background = flat surface, Presentation = favorable orientation.

System 2111: Class 1 – very easy	
	HIGH: • surface area • volume • convex hull area • convex hull volume • compactness (max extent/min extent) • compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) • flat • aspect ratio LOW: • ridge
System 2111: Class 2 - easy	
	HIGH: --- LOW: • compactness (volume/surface area)

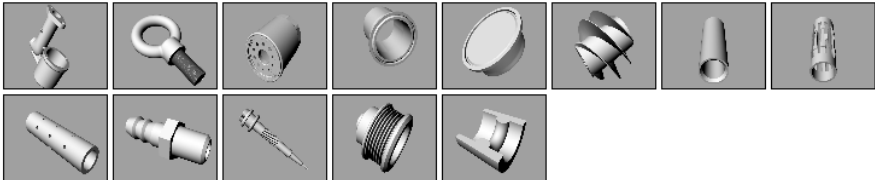
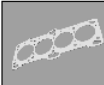
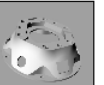
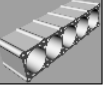
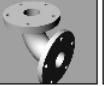
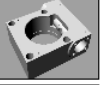
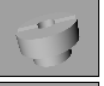
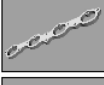
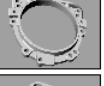
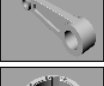
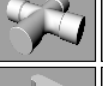
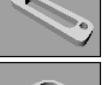
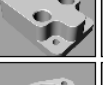
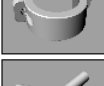
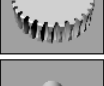
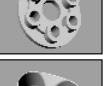
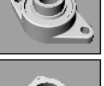
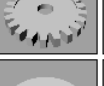
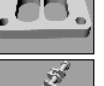
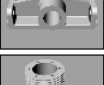
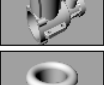
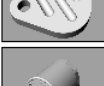
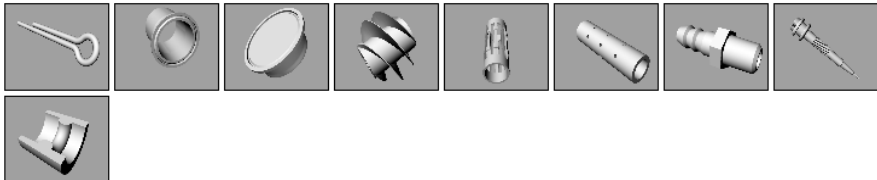
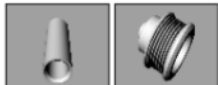
System 2111: Class 3 - medium 	HIGH: • cap • ridge LOW: • compactness (max extent/min extent) • compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) • flat • cup • aspect ratio
System 2111: Class 4 – hard No objects were placed in this class.	
System 2111: Class 5 – very hard No objects were placed in this class.	

Table 6.4. Classification for System 3111: Technology = structured light area scanner mounted on a 6DOF arm, Clutter = isolated, Background = flat surface, Presentation = favorable orientation.

(System 3111: Class 1 – very easy)								HIGH: • surface area • volume • convex hull area • convex hull volume • compactness (volume/surface area) • compactness (max extent/min extent) • compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) • flat • aspect ratio LOW: • ridge
								
								
								
								
								
								
								
								
								
								
								
								
								
								

System 3111: Class 2 - easy 	HIGH: --- LOW: • surface area • volume • convex hull area • convex hull volume • cup • aspect ratio
System 3111: Class 3 - medium 	HIGH: --- LOW: • surface area • volume • convex hull area • convex hull volume • compactness (max extent/min extent) • compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) • saddle • aspect ratio
System 3111: Class 4 – hard No objects were placed in this class.	
System 3111: Class 5 – very hard No objects were placed in this class.	

6.1.3 Vision-based Technology Approach

This approach attempts to classify the objects for vision-based perception systems using the following criteria for obtaining pose in the openCV (Bradski and Kaeber, 2008) and the Point Cloud Libraries (Rusu, 2011):

1. Quality and quantity of an object's perception features
2. Complexities of algorithms to compute those features
3. Uniqueness of those features from different perceptive views

Based on the above criteria, each object was placed into 10 levels. The criteria for the pose score are:

- Score 1 & 2: If all of the following are true:
 - the object has no unique features in all views;
 - it is difficult to obtain visual features of the object (e.g., small holes in the object);
 - the object features are quadratic or higher order.
- Score 3 & 4: if all of the following are true:

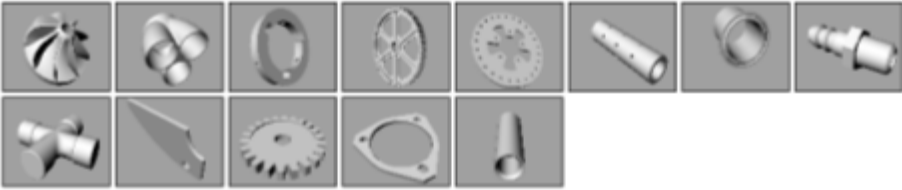
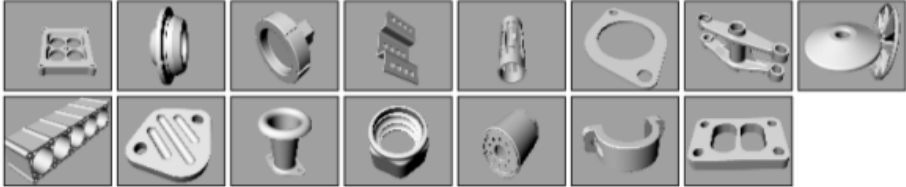
- o the object has at least one medium unique feature (e.g., feature cannot be easily detected) in one to two views;
 - o one to two linear features (e.g., line, edge, point, corner).
- Score 5 & 6: if all of the following are true:
 - o the object has at least one good unique feature (e.g., feature can easily be detected) in three to four views;
 - o three to four linear features.
- Score 7 & 8: if all of the following are true:
 - o the object has at least one excellent unique feature (e.g., feature is very easily detected) in five to six views;
 - o five to six linear features.
- Score 9 & 10: if all of the following are true:
 - o the object has several excellent unique features in all views;
 - o many linear features.

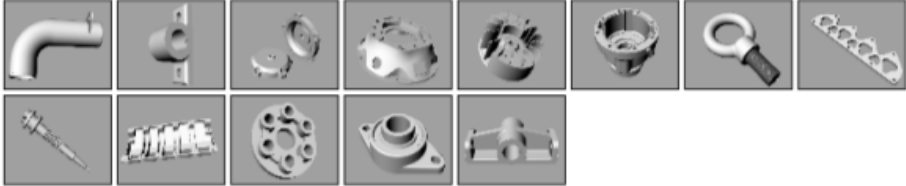
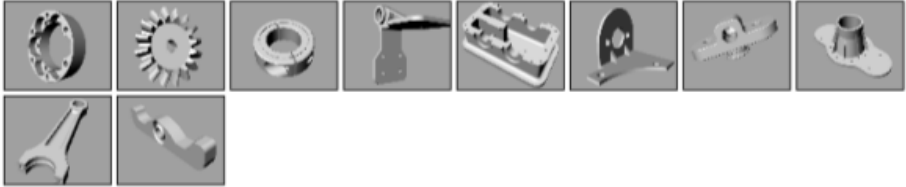
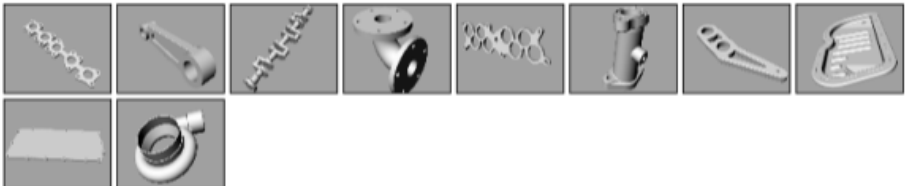
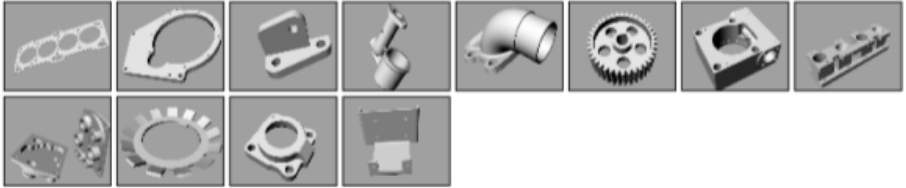
The following procedure to classify the 116 objects into 10 classes:

1. Load the CAD file of each object into MeshLab software
2. View the object from the top, bottom, left, right, front, and back. From these views, the quantity and quality of the features as well as their uniqueness were determined.
3. Based on Step 2, assign a pose score to the object.
4. Group objects with the same pose score into a class: Pose score 1 = Class 1, etc.

For objects in Classes 1 to 4, it would be very problematic for the perception systems to determine their poses. Perception systems would have very little problems in accurately measuring the poses of objects in Classes 7 to 10.

Table 6.5. Vision-based Perception System Classification Approach. Class 1 = very difficult, Class 10 = very easy.

Class 1 	HIGH: --- LOW: • surface area • volume • convex hull area • convex hull volume • rut
Class 2 	HIGH: --- LOW: • surface area • volume • convex hull area • convex hull volume • cup
Class 3 	HIGH: • cup LOW: ---
Class 4 	HIGH: --- LOW: ---

Class 5 	HIGH: cap LOW: ---
Class 6 	HIGH: --- LOW: - compactness (max extent/min extent) - compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) - aspect ratio
Class 7 	HIGH: --- LOW: ---
Class 8 	HIGH: --- LOW: cup
Class 9 	HIGH: --- LOW: ---

Class 10								HIGH: --- LOW: ---
								
								

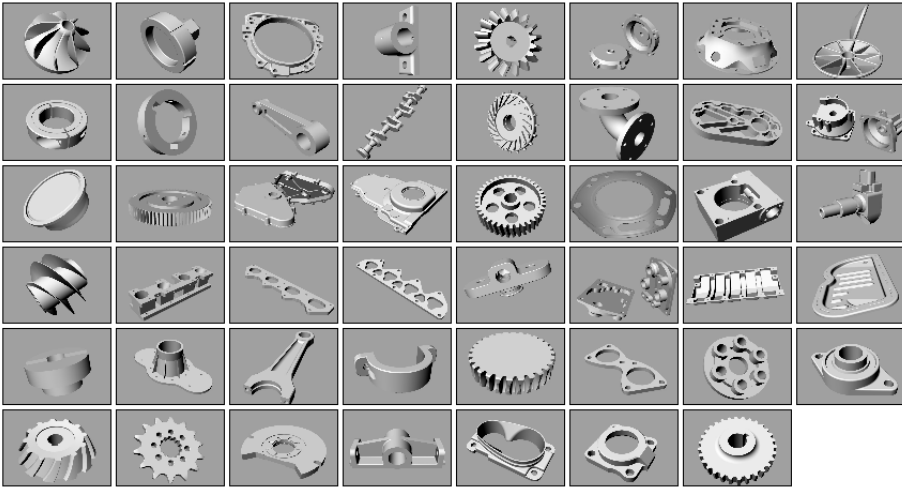
6.2 Classification based on Clustering

We used the metrics given in Table B1 for clustering. Clustering, in this work, is the process of organizing a set of 3D CAD models into groups in such a way that the 3D models within the group are more similar to each other than they are to other objects belonging to different groups. Clustering is also known as an unsupervised learning technique in the scientific literature. We use k -means cluster analysis (Teknomo and Kardi, 2006) along with the shape metrics and a user-defined number of clusters to classify the 3D CAD models. We assume that the models as represented by the shape metrics would allow us to distinguish one group from another.

The k -means algorithm is an algorithm to cluster n objects based on attributes into k partitions, $k < n$. It is similar to the expectation-maximization algorithm for mixtures of Gaussians in that they both attempt to find the centers of natural clusters in the data, where there are k clusters. In this work, we used $k = 5$, $k = 6$, and $k = 10$ as these were the number of classes used for the manual classifications. The results of the clustering based on $k = 5$, $k = 6$, and $k = 10$ are shown in Table 6.6, Table, 6.7, and Table 6.8, respectively.

The metrics we used for k -means clustering are only based on shape type (see Section 5, Table 5.1). The other metrics were not used since there is a large variation in the size of the different models and most of the other shape metrics are scale dependent.

Table 6.6. k -means clustering with $k = 5$ using the shape index metrics.

$k = 5$: Class 1 	HIGH: • flat • aspect ratio LOW: • cap • ridge • saddle
$k = 5$: Class 2 	HIGH: • aspect ratio LOW: ---
$k = 5$: Class 3 	HIGH: • ridge • cup LOW: • surface area • volume • convex hull area • convex hull volume • compactness (max extent/min extent) • compactness ($\text{CH area}^3 / \text{CH volume}^2$) • crumpliness • flat • cup

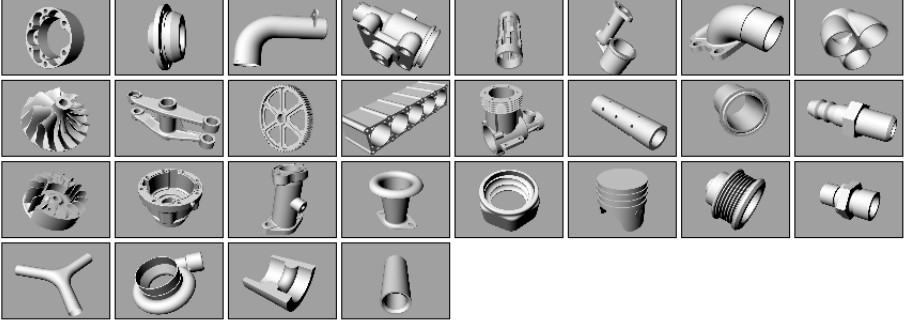
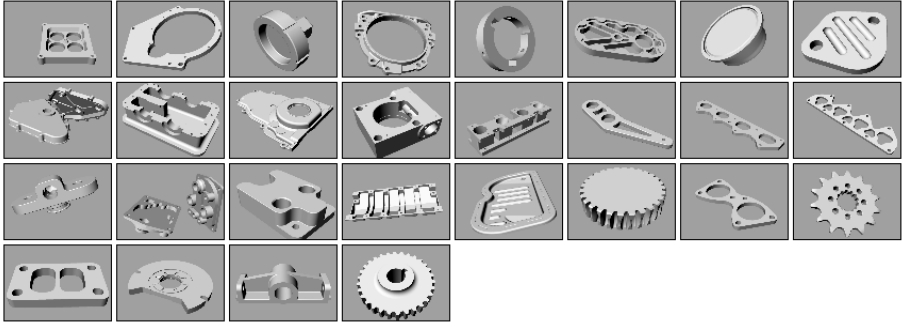
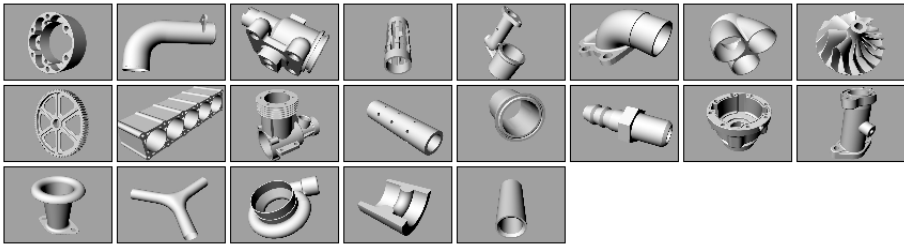
$k = 5$: Class 4 	HIGH: • rut LOW: • compactness (max extent/min extent) • compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) • aspect ratio
$k = 5$: Class 5 	HIGH: • cap • saddle LOW: • surface area • volume • convex hull volume • cup

Table 6.7. k -means clustering, $k = 6$ using the shape index metrics.

$k=6$: Class 1 	HIGH: --- LOW: ---
$k=6$: Class 2 	HIGH: • surface area • volume • convex hull area • convex hull volume LOW: ---
$k=6$: Class 3 [Subset of Class 4, $k=5$] 	HIGH: • surface area • convex hull volume • rut LOW: • compactness (volume/surface area) • compactness (max extent/min extent) • compactness ($CH\ area^3/CH\ volume^2$) • flat • aspect ratio

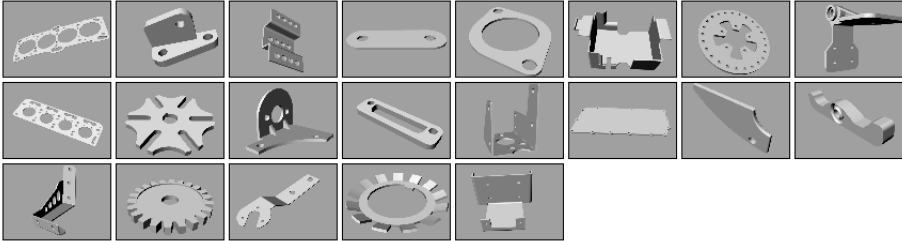
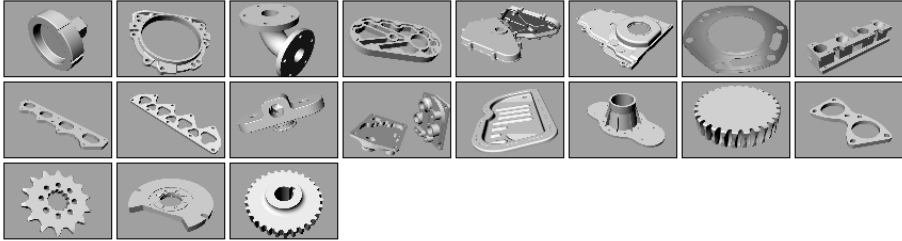
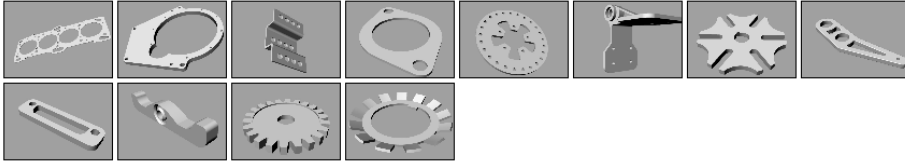
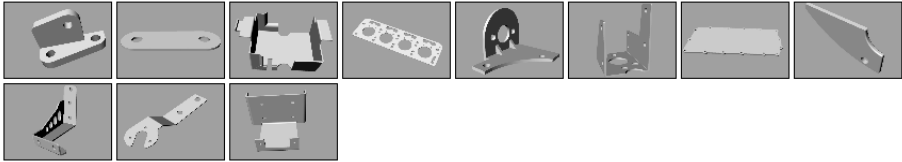
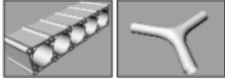
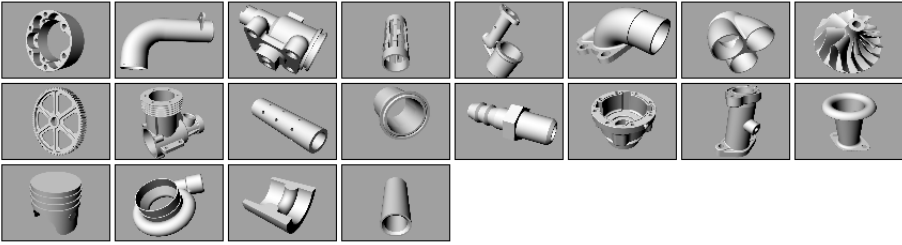
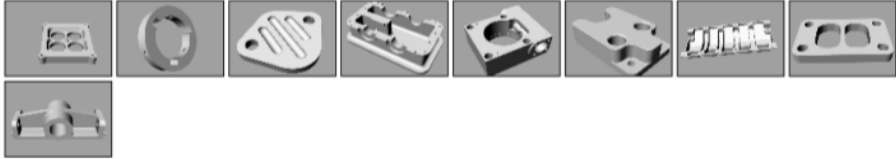
$k=6$: Class 4 [Same as of Class 3, $k=5$] 	HIGH: • ridge LOW: • surface area • volume • convex hull area • convex hull volume • crumpliness • flat • rut • cup • length of sharp edges • aspect ratio
$k=6$: Class 5 [Subset of Class 1, $k=5$] 	HIGH: • compactness (max extent/min extent) • compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) • flat • aspect ratio LOW: • cap • ridge • rut • cup
$k=6$: Class 6 [Same as of Class 5, $k=5$] 	HIGH: • compactness (max extent/min extent) • compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) • cap • saddle LOW: • rut • cup

Table 6.8. k -means clustering, $k = 10$ using the shape index metrics.

$k=10$: Class 1 [Subset of Class 5, $k=5$] 	HIGH: - cap - saddle LOW: - surface area - volume
$k=10$: Class 2 	HIGH: aspect ratio LOW: ---
$k=10$: Class 3 [Subset of Class 1, $k=5$] 	HIGH: - flat - aspect ratio LOW: - saddle - cup
$k=10$: Class 4 [Subset of Class 1, $k=5$] 	HIGH: - flat LOW: - compactness (volume/surface area) - ridge - saddle - rut - cup
$k=10$: Class 5 [Subset of Class 2, $k=5$] 	HIGH: - compactness (volume/surface area) - ridge LOW: ---

$k=10$: Class 6 [Subset of Class 4, $k=5$] 	HIGH: • rut LOW: • cap
$k=10$: Class 7 [Subset of Class 4, $k=5$] 	HIGH: • ridge • rut • cup LOW: • compactness (volume/surface area) • compactness (max extent/min extent) • compactness ($CH \text{ area}^3 / CH \text{ volume}^2$) • flat • aspect ratio
$k=10$: Class 8 	HIGH: --- LOW: • cap • ridge • saddle
$k=10$: Class 9 	HIGH: • cup LOW: ---

$k=10$: Class 10 [Same as Class 3, $k=5$]



HIGH:

- cap
- ridge

LOW:

- surface area
- volume
- convex hull area
- convex hull volume
- flat
- rut
- cup
- length of sharp edges
- aspect ratio

7 Discussion and Summary

7.1 Discussion

As can be expected, manual classifications will be subjective and will likely lack consistency as evidenced by the classifications in Section 6.1. The subjectivity and lack of consistency may be mitigated by training and developing guidelines/rules for performing the classification.

An objective method to classify objects could be one that is based on metrics characterizing an object. Advantages of such a method are objectivity and ease of implementation. The disadvantages of this method are:

1. Selection and determination of an appropriate set of metrics,
2. Classifications may change if different metrics were used. For example, given an object, the object may be placed in Class 1 using Metrics Set A or it may be placed in Class 2 if Metrics Set B were used,
3. Classifications may change if parts are added to or removed from the population of parts. Clustering methods are based only on the relative similarity of dataset attributes to an aggregate cluster average, and outliers and subsequent changes to the attribute space may cause shifts in cluster centroids,
4. Development of algorithms to quantify the metric. For example, quantifying symmetry is very difficult as discussed in Section 3. Others metrics that would be hard to quantify algorithmically include the number of stable of poses and the number of unique views, and
5. Requirement of a 3D model of the object.

The classifications using cluster analysis (Section 6.2) were performed using only the shape type metrics. For the algorithmic-based approach, the number of classes can be set to any number. To reduce the variables between the algorithmic and the manual approaches, the same number of classes, 5, 6, and 10 used in the manual approaches, were used in the algorithmic-based approach. However, since the criteria for the classifications were different (e.g., geometry based, technology based, shape type) the resulting classifications would not be expected to be similar.

Many methods for clustering are found in various communities. Besides the k -means cluster analysis, we also tried a very common approach to clustering called the hierarchical method (Johnson, 1967), also known as Agglomerative clustering. This method is very popular in areas of data mining and bioinformatics. In hierarchical clustering, we do not need to know the number of clusters/groups ahead of time; i.e., the 3D CAD models are not divided into predefined numbers of clusters. We then use a Dendrogram, which is a visual representation of hierarchical data to show the clusters. The Dendrogram tree starts at the root, which is at the top for a vertical tree (the nodes represent clusters). Figure 7.1 shows the Agglomerative clustering based on the shape type metrics only with the number of clusters $k = 30$.

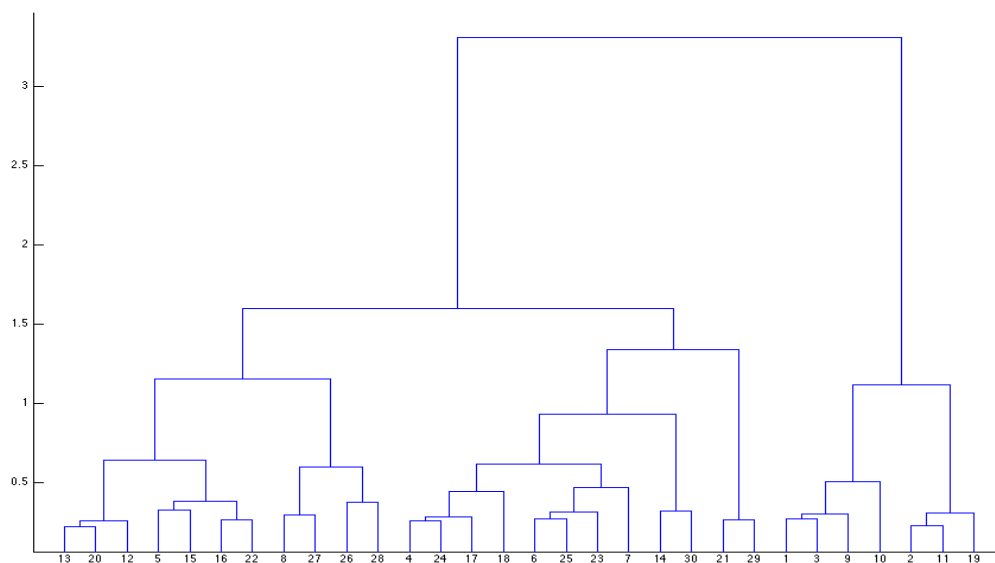


Figure 7.1 Agglomerative clustering based on model shape type metrics (number of clusters $k = 30$).

In Fig. 7.1, the number of clusters will vary depending on the y value selected. Figure 7.2 shows the clusters for $y \approx 1.1$.

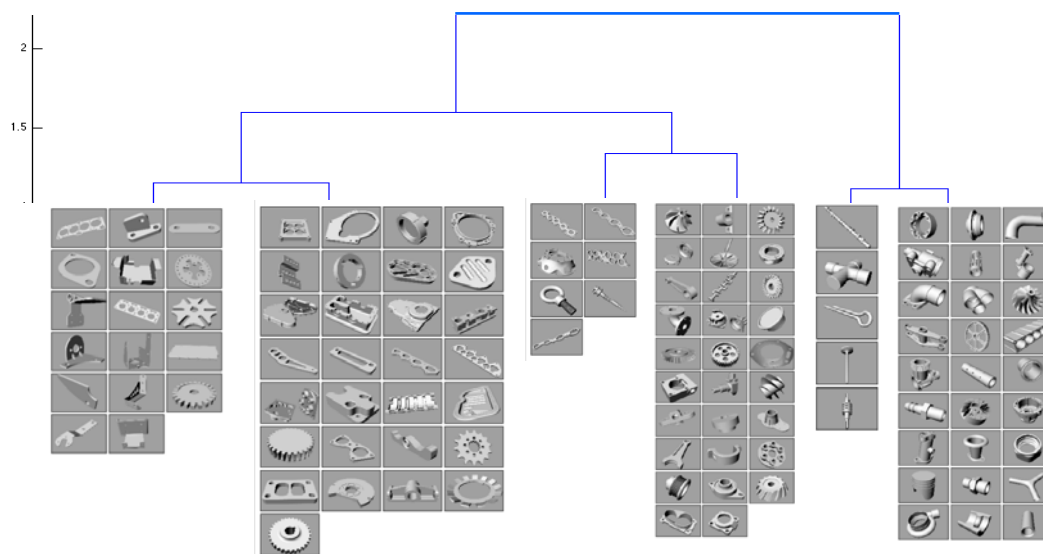


Figure 7.2. Agglomerative clusters for $y \approx 1.1$.

One other approach for classification is to use a classifier such as a Support Vector Machine (SVM) (Hearst et al., 1998) classifier that is trained by human-generated training examples to classify a test dataset. Other possible classifiers that can be used for classification include neural networks (Funahashi, 1989), naive Bayes classifiers (Kohavi, 1996), and boosted decision stumps (Qu et al., 2002).

The High/Low observations in Section 6 seem to indicate that the density, crumpliness, crinkliness, and length of sharp edges metrics may not be useful as distinguishing/discriminating metrics for the set of objects used in this effort. The area, aspect ratio, cap, compactness, convex hull area, convex hull volume, cup, flat, ridge, and volume metrics may be useful as distinguishing/discriminating metrics.

7.2 Summary and Future Work

This study documented the process to develop a classification system for objects. The purpose of the classification system was to support the evaluation of perception systems used for identifying and locating static manufacturing parts. The existence of a robust object classification system may eventually lead to the development of standard reference artifacts of objects in the various classes. A literature review indicated that many of the classification systems developed were for object retrieval and manufacturing systems/process and a classification system such as that envisioned for this study does not exist.

In this study, two approaches, manual and algorithm-based, were used to develop a classification system. Three manual approaches for the classifications were developed where the criterion for one was object geometry and the criteria for the other two were based on the perceived difficulty that a perception system, laser-based and vision-based, would encounter when measuring the pose of the object. The algorithmic approach involved using cluster analysis to classify the objects based on a set of metrics.

A review of metrics used by other researchers was conducted and a set of metrics was selected for use in this study. Commercially or publicly available algorithms were used to calculate the metrics. A database of objects was created where the objects in the database were narrowed down to mainly automotive engine parts and where a 3D CAD model of the object was freely available. In addition to the three manual classifications, *k*-means clustering was used to generate an additional three classifications where *k* was set equal to 5, 6, and 10 using the calculated metrics for shape type.

Based on this work, developing a classification system such as that proposed in this effort will not be easily accomplished as the problem involves a huge, multidimensional parameter space. However, the experience gained from this work with metrics, algorithms to calculate the metrics, file formats, and object databases will benefit future efforts in dealing with smaller object spaces for more defined applications. Also, the experience will inform other efforts to design artifacts and experiments for object identification and pose estimation.

The next step for this study would be the determination of whether the classification systems in Section 6 are good or bad through experimental testing using various perception systems. A good classification would be one that groups objects into classes for which perception systems would yield similar results for a given class. For example, a classification system could group a set of objects into three classes where the measured positional error for the objects would range from (0 to 10) mm, (11 to 20) mm, and (21 to 30) mm for Class 1, 2, and 3, respectively. An ideal classification system would yield positional errors

that are within the specified bounds for all objects in that class and for all perception systems. A good classification system would yield positional errors that are within the specified bounds for most of the objects in that class and for most perception systems. A bad classification system would yield positional errors that are outside the specified bounds for the majority of the objects in a given class and for all classes. That is, for more than 50 % of the objects in Class 1, the errors would be greater than 10 mm and similarly for objects in Classes 2 and 3.

Evaluation of a classification system requires a set of objects and a perception system. For a given set of objects and a given perception system, the classification system may be deemed good. However, robustness of the classification system is of critical importance – would the classification system fail if other objects were added or if another perception system were used? Also, as stated earlier, metrics for symmetry and the number of significant features were not used in the cluster analysis in this effort. A next step would be to calculate these metrics (and/or other metrics such as number of unique views or color) and determine how the classifications would change and to evaluate the classification system through experimental testing.

If a classification system is deemed bad, the reasons for its failure need to be determined; reasons such as (1) were the metrics not the appropriate ones? and (2) was the classification system only valid for a particular type of perception system technology?

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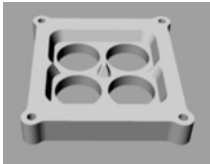
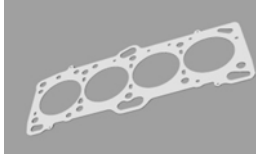
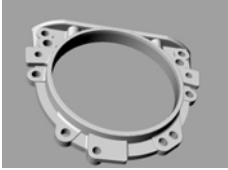
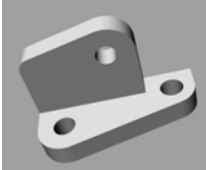
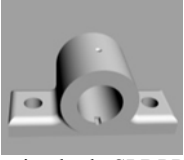
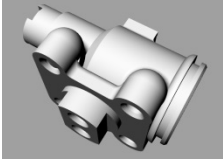
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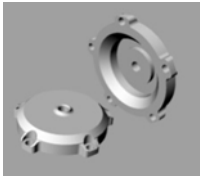
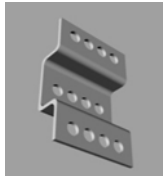
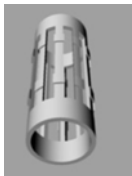
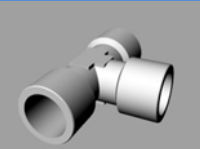
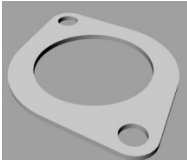
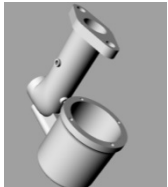
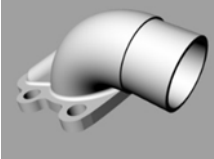
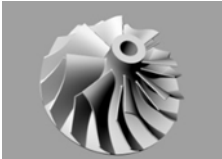
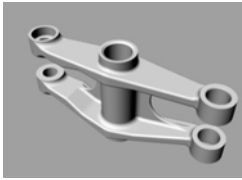
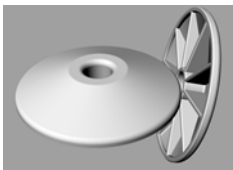
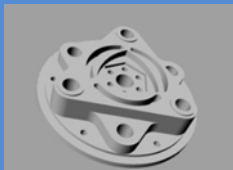
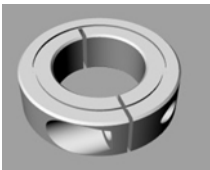
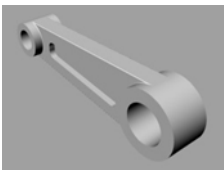
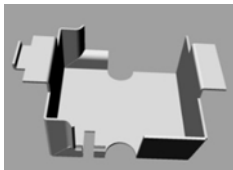
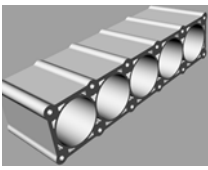
Appendix A: Objects Used in Classification Systems

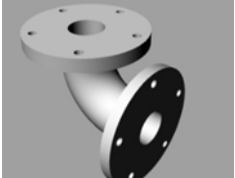
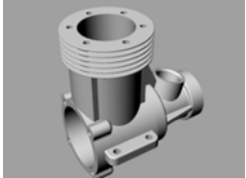
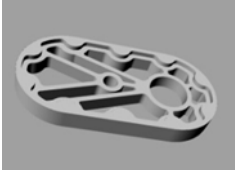
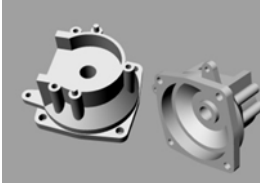
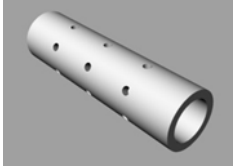
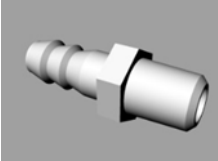
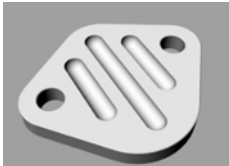
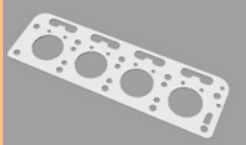
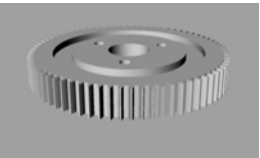
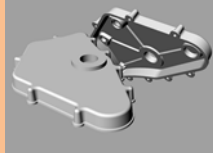
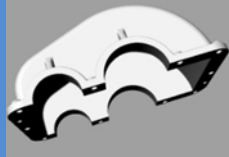
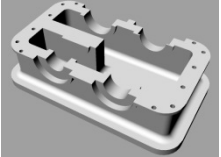
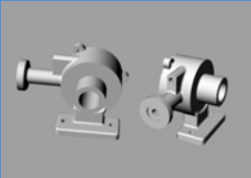
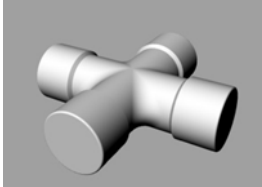
The objects selected for use in the classification system were downloaded from www.GradCAD.com and images of these objects are given in the table below. The object file names are given below each image, and they indicate the format of each file: SLDPRT = SolidWorks; STP/STEP = Step; IGS/IGES = IGES; 3DM = Rhino; DWG = AutoCAD.

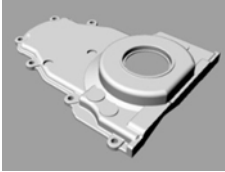
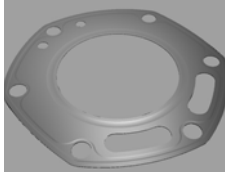
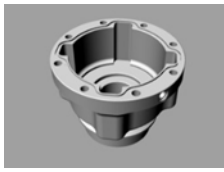
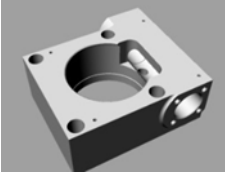
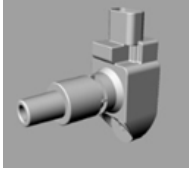
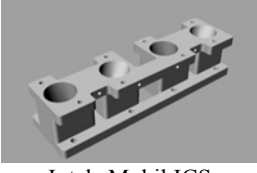
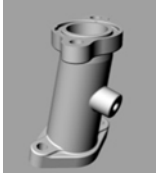
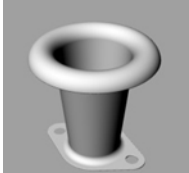
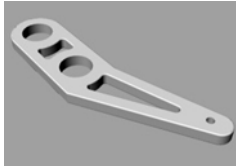
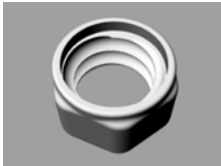
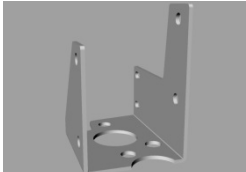
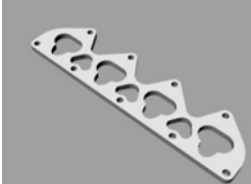
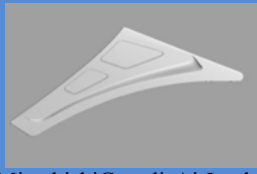
The objects in red and blue shaded cells were not included in the classification. The cells shaded in red could not be meshed. The curvature metrics for objects in cells shaded in blue could not be calculated. There are some known bugs in the curvature algorithm and further debugging of the algorithm was not pursued as this was beyond the scope of the task. The orange shaded cells were objects which had at least one dimension greater than 50 cm.

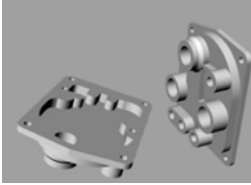
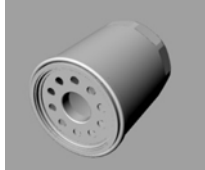
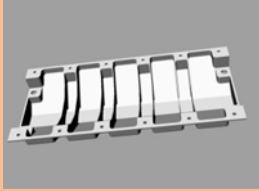
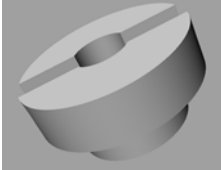
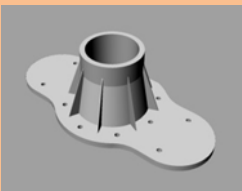
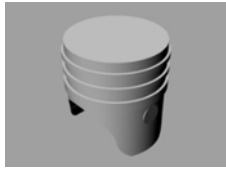
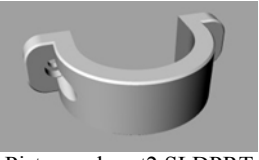
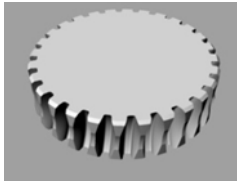
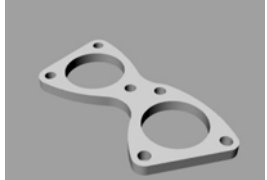
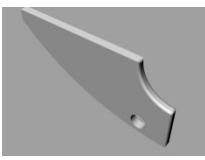
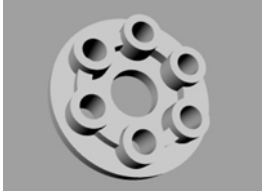
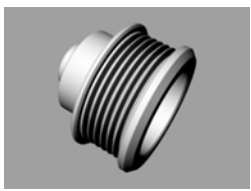
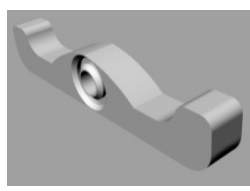
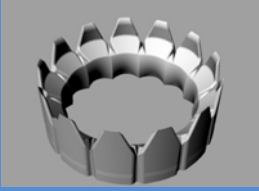
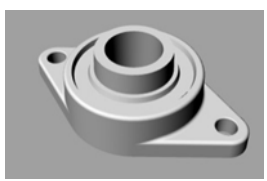
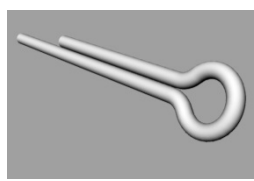
Table A.1. Objects used in the classification systems.

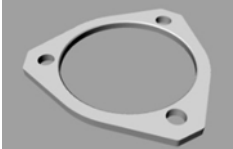
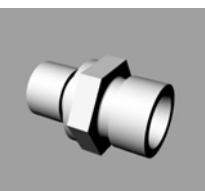
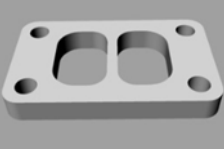
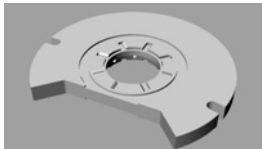
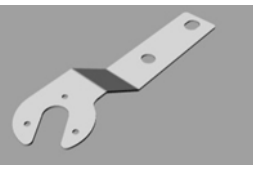
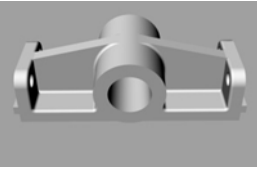
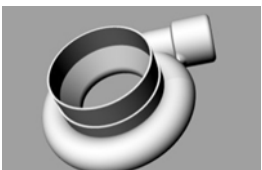
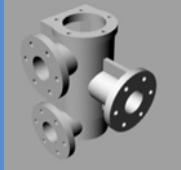
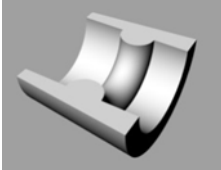
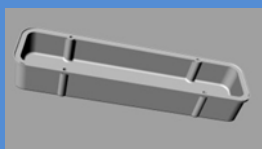
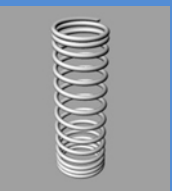
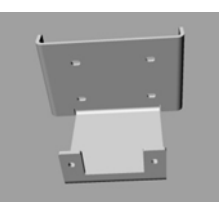
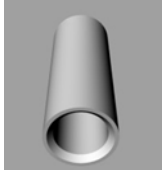
 1 inch Carb Spacer.SLDPRT	 4 cylinder engine head gasket.SLDPRT	 944 Bellhousing Base.SLDPRT	 944to911 Outer CV Adapter.SLDPRT
 9 Blade Impeller.SLDPRT	 9 Inch Pin Support.SLDPRT	 Alum PIPE.SLDPRT	 Audi 20V Exhaust Flange.SLDPRT
 Audi bearing retainer tool.SLDPRT	 Audi-VW Rear crank plate.IGS	 Base Bracket.SLDPRT	 bearing body.SLDPRT
 Bevel Gear.SLDPRT	 Big Block Chevy Flange.igs	 Block.dwg	 boltnew.SLDPRT

 BOVTop-2.SLDPRT	 BRACKET.SLDPRT	 brake_shoe.igs	 BRE 1.4L I4 Needle Sleeve Bearing Body.SLDPRT
 BSP Tee.IGS	 Bus Bar 2 cells 40152S.SLDPRT	 Cam retainer.stp	 camshaft.SLDPRT
 Carburator Body.IGS	 CastAluminumIntake.SLDPRT	 CastExhaustCollector.SLDPRT	 CetrifugallImpeller.igs
 ChevyHeader Flange.SLDPRT	 ClutchCover.SLDPRT	 ClutchPlate1.igs	 ClutchPlate2.SLDPRT
 Collar 1in Shaft.stp	 Collar Shaft.SLDPRT	 Connecting rod.SLDPRT	 Cover_Plate.SLDPRT
 CrankGear.SLDPRT	 Crankshaft.SLDPRT	 Cylinder Block 5cyl.SLDPRT	 Diffuser.dwg

 DISC PLATE.SLDPRT	 ElbowCastIron.SLDPRT	 EngineAirIntake.SLDPRT	 EngineBlock.stp
 EngineBottomPlate.igs	 EngineFrontCover.SLDPRT	 Engine Gudgeon Pin.SLDPRT	 Ferrule 2Inch Clamp Tube OD w Seal Groove_pt1.3dm
 Ferrule 2Inch Clamp Tube OD w Seal Groove_pt2.3dm	 fitting.3dm	 Flange.igs	 Fly wheel.SLDPRT
 Ford GT40 intake spacer.SLDPRT	 Fuel Pump Delete Plate.stp	 fuelpumpR1.dwg	 gasket.SLDPRT
 Gear.SLDPRT	 Gear1.dwg	 GearboxCasing.SLDPRT	 GearBoxPart2.SLDPRT
 GearBoxTophousing.SLDPRT	 GearHousing.SLDPRT	 Geneva Cam.SLDPRT	 GM 3R U-Joint.stp

 GMLS6FrtCover.SLDPRT	 Helical gear wheel.STEP	 HondaNSR125CylinderHead Gasket.IGS	 Housing.SLDPRT
 HousingSquare.SLDPRT	 IgnitionCoilMazda13B.SLD PRT	 Impeller.SLDPRT	 IntakeManifold.3dm
 IntakeMobil.IGS (IntakeMobilPart1.stl)	 IntakeMobil.IGS (IntakeMobilPart2.stl)	 IntakePipeComponent.igs	 IntakeTrumpet.igs
 Jetta_Actuator Bracket.SLDPRT	 link.IGS	 LockNuts.SLDPRT	 LowerControlArm.stp
 LowerThermostatHousing spacer GM.SLDPRT	 M20LiftingEyeBolt.SLDPR T	 ManifoldPlate.stp	 MasterCylinder Bracket.3dm
 Miata16IntakeFlange.SLDP RT	 MitsubishiEVOMAPadapter. SLDPRT	 MitsubishiGrandisAirIntake. stp	 Needle valve screw.SLDPRT

 Oerlikon Brake valve.SLDPRT	 OilCoolerBypassCover Plate for VW.stp	 OilFilter.dwg	 OilPan.SLDPRT
 OilPanModel2.IGS	 OldhamCoupling.SLDPRT	 Parametric Flange.igs	 Piston.stp
 Piston rod_part1.SLDPRT	 Piston rod part2.SLDPRT	 Pitch2.SLDPRT	 PlenumPlate.IGS
 Porsche968Flange.SLDPRT	 Porsche968IntakeFlange.SLDPRT	 PorscheStrutBarTopBrace.SLDPRT	 Pressure plate.SLDPRT
 PulleyForAlternator.stp	 RockerArm.stp	 SerratedIntake.SLDPRT	 SkidPlateBracket.SLDPRT
 Socket.SLDPRT	 SpiralBevelGear.SLDPRT	 SplitPin.igs	 Sproket.SLDPRT

 SpurGear.SLDPRT	 SteeringKnuckleFlange Spacer.IGS	 StraightScrewJoint.stp	 T3DividedTurboInlet Flange.SLDPRT
 ThreeTubeJoint.igs	 Thrust bearing-disc.SLDPRT	 TowbarElectrics Bracket.SLDPRT	 Truss Bearing.SLDPRT
 Turbo housing.SLDPRT	 Valve.igs	 ValveChest.igs	 ValveClip.SLDPRT
 ValveCover2.igs	 VariablePitchSpring.SLDPRT	 VW Golf Inlet Flange.SLDPRT	 W05Lockwasher.SLDPRT
 WheelBearingHousingFor a VW.stp	 WINCH MTG BRK.SLDPRT	 WormGearDesign.SLDPRT	 WormGear.SLDPRT
 wrist pin.SLDPRT	EMPTY	EMPTY	EMPTY

Appendix B: Calculated Metrics for Objects in Appendix A.

Table B1. Calculated Metrics

FileName	Object ID	Surface Area [cm ²]	Vol [cm ³]	Extent			Convex Hull Area [cm ²]	Convex Hull Vol [cm ³]	Compactness Vol/Surface Area [cm]	Compactness Max/Min Extent	Compactness CHarea ³ /CHvol ²	Density 1 – Vol/ChVol
				DX [cm]	DY [cm]	DZ [cm]						
1inchCarbSpacer	1	603	331	15	3	16	639	615	0.549	6.38	688.44	0.46
4cylinderEngineHeadGasket	2	641	44	40	0	17	1308	97	0.069	269.86	238461.05	0.54
944BellhousingBase	3	1307	830	37	2	34	2065	1773	0.635	19.25	2800.11	0.53
944to911OuterCVAdapter	4	373	121	4	11	11	300	338	0.324	2.87	235.50	0.64
9BladeImpeller	5	1	0	1	0	1	1	0	0.024	1.87	178.78	0.45
9InchPinSupport	6	779	549	17	7	17	588	1092	0.705	2.27	170.33	0.50
AlumPIPE	7	1517	301	27	11	17	1080	2470	0.198	2.51	206.58	0.88
Audi20VExhaustFlange	8	558	143	43	9	1	796	287	0.256	53.75	6108.84	0.50
AudiBearingRetainerTool	9	211	94	8	6	8	183	194	0.447	1.38	163.36	0.51
AudiVWRearCrankPlate	10	291	62	15	2	13	379	240	0.214	9.56	938.77	0.74
BaseBracket	11	405	269	14	9	7	387	467	0.664	2.13	265.91	0.42
BearingBody	12	968	908	10	11	23	833	1611	0.938	2.30	222.29	0.44
BevelGear	13	250	116	3	11	11	211	185	0.462	3.94	276.91	0.37
BigBlockChevyFlange	14	488	138	48	8	1	779	324	0.283	50.69	4493.55	0.57
Block	15	271	80	9	6	6	177	187	0.296	1.50	158.12	0.57
BOVTop2	16	153	38	8	2	8	128	73	0.251	4.75	392.98	0.48
BRACKET	17	398	75	10	3	15	394	353	0.188	4.69	491.85	0.79
BRE14LI4NeedleSleeve BearingBody	18	43	2	2	2	5	35	14	0.045	2.66	217.75	0.86
BusBar2Cells40152S	19	25	2	6	0	2	25	2	0.067	40.73	5254.05	0.06
CamRetainer	20	32	2	7	5	0	51	4	0.066	44.69	8937.25	0.46
camshaft	21	404	193	4	51	4	516	385	0.477	12.50	925.38	0.50

CarburatorBody	22	974	282	9	18	18	725	1378	0.290	2.07	200.83	0.80
CastAluminumIntake	23	525	99	15	10	10	389	499	0.189	1.52	236.53	0.80
CastExhaustCollector	24	361	34	9	6	8	245	291	0.093	1.41	174.61	0.88
CetrifugalImpeller	25	185	21	7	3	7	97	66	0.114	2.10	207.82	0.68
ChevyHeaderFlange	26	554	142	21	5	10	512	646	0.256	4.67	321.56	0.78
ClutchCover	27	1340	248	24	6	24	1130	2028	0.185	4.00	351.20	0.88
ClutchPlateI	28	562	132	15	15	3	390	281	0.235	6.00	754.82	0.53
Collar1inShaft	29	55	12	4	4	1	48	20	0.212	3.50	281.39	0.41
CollarShaft	30	67	14	6	1	6	75	28	0.211	6.00	536.16	0.50
ConnectingRod	31	284	101	18	3	5	264	211	0.355	6.07	412.31	0.52
CoverPlate	32	1454	210	25	11	19	1305	3306	0.144	2.36	203.14	0.94
CrankGear	33	11864	9378	78	7	78	11315	34789	0.790	10.67	1196.91	0.73
Crankshaft	34	759	305	5	9	40	840	1102	0.402	7.99	488.22	0.72
CylinderBlock5cyl	35	7361	3062	49	16	12	3115	9465	0.416	4.12	337.37	0.68
Diffuser	36	1197	511	6	21	21	880	1570	0.427	3.38	276.40	0.67
DISCPLATE	37	692	202	22	1	22	784	279	0.292	28.33	6189.29	0.28
ElbowCastIron	38	2978	2488	23	26	26	2214	7295	0.836	1.17	204.07	0.66
EngineBlock	39	645	132	8	11	11	362	538	0.205	1.46	164.36	0.75
EngineBottomPlate	40	524	162	2	20	10	460	357	0.309	10.00	762.94	0.55
EngineFrontCover	41	264	77	9	9	5	207	225	0.293	1.73	176.55	0.66
EngineGudgeonPin	42	40	4	5	1	1	25	8	0.091	3.57	265.98	0.52
Ferrule2InchClampTubeO DwSealGroovePt1	43	208	19	6	6	6	158	152	0.089	1.12	170.49	0.88
Ferrule2InchClampTubeO DwSealGroovePt2	44	101	45	2	6	6	94	57	0.451	3.01	250.53	0.21
fitting	45	33	4	5	2	2	24	8	0.108	2.71	203.28	0.56
Flange	46	322	73	8	13	12	378	510	0.227	1.68	207.52	0.86
FlyWheel	47	348	92	9	4	9	218	228	0.265	2.34	200.38	0.60
FordGT40IntakeSpacer	48	410	95	34	1	9	638	267	0.232	35.31	3636.82	0.64
FuelPumpDeletePlate	49	61	12	6	5	1	56	14	0.201	10.00	853.14	0.15
gasket	50	2795	390	80	25	0	4036	596	0.140	266.67	184956.67	0.35

Gear	51	563	244	14	14	2	416	325	0.433	7.20	679.26	0.25
GearboxCasing	52	6386	3046	66	45	8	5254	14064	0.477	8.72	733.23	0.78
GearBoxTophousing	53	5946	6377	48	28	12	4105	14760	1.072	4.00	317.42	0.57
GenevaCam	54	317	107	14	15	1	367	161	0.338	14.54	1911.01	0.33
GM3RUJoint	55	154	94	9	9	3	187	170	0.611	3.22	227.41	0.45
GMLS6FrtCover	56	1708	401	32	27	5	1527	2184	0.235	6.18	745.99	0.82
HelicalGearWheel	57	779	225	14	14	4	483	615	0.289	3.50	298.25	0.63
HondaNSR125Cylinder HeadGasket	58	93	1	10	10	0	153	2	0.012	328.54	659909.64	0.53
Housing	59	644	209	11	11	8	390	601	0.325	1.34	164.57	0.65
HousingSquare	60	971	575	15	14	6	702	1144	0.592	2.47	264.25	0.50
IgnitionCoilMazda13B	61	194	73	4	9	9	164	142	0.375	2.60	221.13	0.49
Impeller	62	288	63	8	6	8	175	208	0.218	1.33	123.36	0.70
IntakeMobilPart1	63	1819	1014	33	9	8	1230	2270	0.557	4.41	361.16	0.55
IntakePipeComponent-1	64	176	32	6	5	8	142	122	0.183	1.59	194.76	0.74
IntakeTrumpet	65	82	3	4	4	4	64	42	0.032	1.06	153.80	0.94
JettaActuatorBracket	66	106	15	8	6	5	122	78	0.137	1.52	297.09	0.81
link	67	727	402	40	13	2	835	670	0.553	20.21	1298.01	0.40
LockNuts	68	12	1	2	2	1	9	2	0.063	1.75	168.47	0.64
LowerThermostatHousing SpacerGM	69	103	24	12	3	1	110	39	0.233	12.83	876.92	0.38
M20LiftingEyeBolt	70	167	58	7	12	3	157	117	0.349	4.03	282.70	0.50
ManifoldPlate	71	430	149	33	7	1	507	250	0.347	27.54	2081.82	0.40
MasterCylinderBracket	72	559	88	13	9	13	627	1037	0.157	1.48	229.36	0.92
Miata16IntakeFlange	73	483	137	34	9	1	629	264	0.284	36.22	3586.81	0.48
MitsubishiEVOMAPadapter	74	58	13	6	2	3	47	24	0.233	2.52	191.90	0.43
NeedleValveScrew	75	5	0	1	3	1	5	1	0.064	4.70	309.13	0.47
OerlikonBrakeValve	76	1606	812	18	6	24	1126	2008	0.505	4.29	354.10	0.60
OilCoolerBypasCover PlateForVW	77	217	111	9	6	3	184	144	0.512	3.50	300.79	0.23
OilFilter	78	1533	2768	12	15	12	710	1535	1.806	1.26	152.17	-0.80 ¹
OilPan	79	4452	1217	51	8	24	3097	6854	0.273	6.43	632.10	0.82

OilPanModel2	80	1546	123	19	3	34	1259	1043	0.080	13.45	1835.42	0.88
OldhamCoupling	81	775	850	15	8	15	638	1221	1.097	1.96	174.25	0.30
ParametricFlange	82	23526	42614	135	68	43	19839	167630	1.811	3.18	277.87	0.75
piston	83	655	420	11	11	11	480	850	0.642	1.05	153.62	0.51
PistonRodPart1	84	196	57	6	17	2	221	121	0.294	11.50	741.03	0.52
PistonRodPart2	85	145	47	11	6	3	165	130	0.322	3.67	264.93	0.64
pitch2	86	108	40	6	6	2	86	46	0.371	3.82	304.58	0.13
PlenumPlate	87	1409	418	40	1	18	1466	444	0.297	63.19	16026.04	0.06
Porsche968Flange	88	202	52	17	8	1	291	118	0.257	18.35	1769.83	0.56
Porsche968IntakeFlange	89	573	186	46	2	7	715	447	0.325	28.94	1832.44	0.58
PorscheStrutBarTopBrace	90	87	18	11	1	5	89	19	0.207	21.79	1966.39	0.05
PressurePlate	91	176	41	8	2	8	126	80	0.236	4.00	310.38	0.48
PulleyForAlternator	92	286	63	6	7	7	161	174	0.221	1.17	137.78	0.64
RockerArm	93	758	695	4	36	7	801	951	0.916	9.00	568.10	0.27
SkidPlateBracket	94	495	71	16	19	12	649	918	0.144	1.52	324.72	0.92
socket	95	280	153	14	8	4	232	234	0.549	3.38	226.56	0.35
SpiralBevelGear	96	269	175	11	3	11	245	217	0.652	3.67	313.46	0.19
SplitPin	97	2	0	0	3	1	3	0	0.031	25.08	1225.96	0.49
sproket	98	0	0	0	0	0	0	0	0.008	8.54	862.56	0.42
SpurGear	99	449	154	15	15	2	411	256	0.343	9.82	1058.35	0.40
SteeringKnuckleFlangeSpacer	100	155	98	14	14	1	294	85	0.631	22.07	3541.99	-0.15 ¹
StraightScrewJoint	101	28	4	3	2	2	21	8	0.154	1.58	158.40	0.42
T3DividedTurboInletFlange	102	181	56	11	1	7	185	90	0.311	8.50	771.25	0.38
ThreeTubeJoint	103	137	51	14	12	2	258	203	0.375	5.65	418.39	0.75
ThrustBearingDisc	104	71	11	6	5	1	69	16	0.160	11.82	1290.09	0.28
TowbarElectricsBracket	105	311	29	8	30	4	440	282	0.094	8.27	1070.98	0.90
TrussBearing	106	817	495	21	7	9	634	1025	0.606	3.05	242.18	0.52
TurboHousing	107	4828	1970	37	16	34	2806	10953	0.408	2.28	184.07	0.82
valve	108	35	7	4	4	10	78	41	0.191	2.91	281.38	0.84
ValveClip	109	2	0	1	1	0	2	0	0.044	2.00	238.07	0.47

VWGolfInletFlange	110	207	40	11	7	3	202	158	0.192	4.52	331.82	0.75
W05Lockwasher	111	17	1	4	4	0	29	4	0.040	13.40	1809.52	0.82
WheelBearingHousingForAVW	112	237	61	9	9	3	208	175	0.259	3.41	292.83	0.65
WINCHMTGBRK	113	1644	484	25	15	21	1875	5308	0.294	1.63	234.10	0.91
WormGear	114	437	271	6	6	28	405	484	0.620	4.67	284.50	0.44
WormGearDesign	115	2075	3160	28	28	10	1718	4758	1.523	2.80	224.13	0.34
WristPin	116	84	13	2	2	6	56	28	0.151	2.70	225.81	0.54
†The density value should be a positive a value as the volume of the convex hull of an object cannot be less than the volume of the object. It appears that some of the normals for these meshes were not pointed in the correct direction. These negative values were omitted in the analysis.												

Table B1. Calculated Metrics (continued)

FileName	Smoothness: Hull Crumpliness Surface Area/ CHarea	Smoothness: Crinkliness Ratio of surface area to surface area of sphere with same volume as object	Cap	Ridge	Flat	Saddle	Rut	Cup	Normalized Length of Sharp Edges	DX/DY	DX/DZ	DY/DZ
1inchCarbSpacer	0.94	2.60	0.012	0.125	0.598	0.059	0.199	0.007	13.02	5.91	0.93	0.16
4cylinderEngineHeadGasket	0.49	10.58	0.019	0.174	0.697	0.110	0.000	0.000	8.58	269.86	2.37	0.01
944BellhousingBase	0.63	3.06	0.008	0.172	0.624	0.056	0.139	0.000	5.99	19.25	1.07	0.06
944to911OuterCVAdapter	1.24	3.16	0.017	0.367	0.129	0.062	0.407	0.018	13.40	0.35	0.35	1.00
9BladeImpeller	1.49	2.60	0.022	0.272	0.370	0.050	0.284	0.001	11.89	1.87	1.00	0.54
9InchPinSupport	1.32	2.40	0.027	0.367	0.275	0.080	0.233	0.016	16.51	2.27	1.00	0.44
AlumPIPE	1.40	6.98	0.111	0.358	0.016	0.103	0.331	0.082	3.76	2.51	1.54	0.61
Audi20VExhaustFlange	0.70	4.23	0.104	0.180	0.351	0.322	0.040	0.004	9.57	4.89	53.75	11.00
AudiBearingRetainerTool	1.15	2.11	0.018	0.281	0.543	0.012	0.144	0.002	3.74	1.37	1.00	0.73
AudiVWRearCrankPlate	0.77	3.84	0.030	0.224	0.495	0.110	0.128	0.013	12.52	9.56	1.18	0.12
BaseBracket	1.05	2.01	0.011	0.114	0.772	0.018	0.085	0.000	5.26	1.51	2.13	1.41

BearingBody	1.16	2.14	0.010	0.287	0.366	0.069	0.266	0.001	7.18	0.89	0.43	0.49
BevelGear	1.18	2.18	0.033	0.487	0.330	0.019	0.124	0.007	12.08	0.25	0.25	1.00
BigBlockChevyFlange	0.63	3.77	0.122	0.231	0.287	0.318	0.043	0.000	7.30	6.34	50.69	8.00
Block	1.53	3.01	0.090	0.369	0.193	0.079	0.256	0.014	13.94	1.50	1.50	1.00
BOVTop2	1.19	2.78	0.040	0.234	0.392	0.071	0.249	0.013	9.83	4.75	1.04	0.22
BRACKET	1.01	4.63	0.003	0.153	0.668	0.030	0.146	0.000	7.98	3.13	0.67	0.21
BRE14LI4NeedleSleeve BearingBody	1.24	5.68	0.022	0.546	0.130	0.070	0.232	0.001	27.26	1.01	0.38	0.38
BusBar2Cells40152S	0.97	3.64	0.033	0.105	0.825	0.029	0.008	0.000	4.50	40.73	3.10	0.08
CamRetainer	0.62	3.99	0.042	0.154	0.696	0.092	0.016	0.000	5.51	1.41	44.69	31.67
camshaft	0.78	2.50	0.122	0.682	0.058	0.136	0.002	0.000	5.32	0.08	1.00	12.50
CarburatorBody	1.34	4.68	0.055	0.384	0.141	0.072	0.318	0.029	7.34	0.49	0.48	0.99
CastAluminumIntake	1.35	5.07	0.106	0.308	0.128	0.069	0.331	0.058	5.72	1.47	1.52	1.03
CastExhaustCollector	1.47	7.15	0.099	0.352	0.006	0.035	0.502	0.006	5.46	1.41	1.07	0.76
CetrifugalImpeller	1.91	5.02	0.006	0.267	0.209	0.115	0.396	0.007	8.76	2.10	1.00	0.48
ChevyHeaderFlange	1.08	4.21	0.030	0.281	0.264	0.127	0.287	0.011	4.70	4.67	2.10	0.45
ClutchCover	1.19	7.02	0.013	0.238	0.301	0.222	0.202	0.024	17.60	4.00	1.00	0.25
ClutchPlate1	1.44	4.48	0.013	0.421	0.395	0.037	0.125	0.008	12.95	1.00	6.00	6.00
Collar1inShaft	1.16	2.22	0.037	0.312	0.316	0.062	0.268	0.005	11.17	1.00	3.50	3.50
CollarShaft	0.88	2.36	0.001	0.173	0.581	0.016	0.227	0.000	6.84	6.00	1.00	0.17
ConnectingRod	1.08	2.71	0.045	0.322	0.357	0.062	0.204	0.011	6.17	6.07	3.64	0.60
CoverPlate	1.11	8.51	0.012	0.136	0.799	0.011	0.042	0.000	6.84	2.36	1.33	0.56
CrankGear	1.05	5.52	0.067	0.364	0.154	0.133	0.261	0.022	26.32	10.66	1.00	0.09
Crankshaft	0.90	3.46	0.147	0.329	0.344	0.118	0.062	0.000	11.61	0.53	0.13	0.24
CylinderBlock5cyl	2.36	7.22	0.013	0.156	0.165	0.093	0.573	0.000	12.10	3.09	4.12	1.33
Diffuser	1.36	3.87	0.033	0.271	0.405	0.071	0.193	0.027	21.33	0.30	0.30	1.00
DISCPATE	0.88	4.15	0.008	0.093	0.735	0.085	0.079	0.000	9.63	28.33	1.00	0.04
ElbowCastIron	1.34	3.35	0.080	0.236	0.413	0.080	0.153	0.039	8.08	0.87	0.86	0.98
EngineBlock	1.78	5.14	0.033	0.317	0.215	0.057	0.364	0.013	12.21	0.72	0.68	0.95
EngineBottomPlate	1.14	3.64	0.014	0.230	0.574	0.034	0.145	0.004	15.18	0.10	0.20	2.00

EngineFrontCover	1.28	3.01	0.017	0.321	0.331	0.039	0.286	0.006	12.63	1.00	1.73	1.73
EngineGudgeonPin	1.61	3.52	0.015	0.519	0.022	0.050	0.394	0.000	4.84	3.57	3.57	1.00
Ferrule2InchClampTubeO DwSealGroovePt1	1.32	6.14	0.016	0.465	0.077	0.030	0.409	0.004	8.86	0.89	0.89	1.00
Ferrule2InchClampTubeO DwSealGroovePt2	1.08	1.64	0.024	0.374	0.515	0.029	0.056	0.001	6.23	0.33	0.33	1.00
fitting	1.40	2.93	0.051	0.432	0.132	0.040	0.345	0.000	5.42	2.71	2.35	0.87
Flange	0.85	3.81	0.001	0.075	0.722	0.024	0.171	0.007	8.66	0.60	0.67	1.13
FlyWheel	1.59	3.53	0.038	0.346	0.246	0.056	0.276	0.039	18.84	2.34	1.00	0.43
FordGT40IntakeSpacer	0.64	4.07	0.127	0.147	0.222	0.355	0.145	0.003	10.13	35.31	3.66	0.10
FuelPumpDeletePlate	1.09	2.37	0.017	0.134	0.633	0.026	0.160	0.030	4.99	1.19	10.00	8.43
gasket	0.69	10.83	0.009	0.111	0.755	0.125	0.000	0.000	12.37	3.20	266.67	83.33
Gear	1.35	2.98	0.057	0.280	0.402	0.082	0.176	0.004	33.64	1.00	7.20	7.20
GearboxCasing	1.22	6.28	0.057	0.172	0.485	0.099	0.158	0.029	8.39	1.46	8.72	5.97
GearBoxTophousing	1.45	3.58	0.032	0.107	0.587	0.054	0.201	0.018	15.82	1.71	4.00	2.33
GenevaCam	0.86	2.90	0.009	0.111	0.706	0.052	0.121	0.000	7.92	0.95	13.88	14.54
GM3RUJoint	0.82	1.54	0.056	0.663	0.136	0.132	0.013	0.000	1.56	1.00	3.22	3.22
GMLS6FrtCover	1.12	6.50	0.054	0.184	0.497	0.083	0.163	0.019	7.45	1.20	6.18	5.14
HelicalGearWheel	1.61	4.35	0.019	0.210	0.421	0.046	0.299	0.005	34.08	1.00	3.50	3.50
HondaNSR125Cylinder HeadGasket	0.61	18.16	0.007	0.301	0.451	0.049	0.191	0.001	7.92	1.07	328.54	306.94
Housing	1.65	3.78	0.022	0.272	0.202	0.111	0.354	0.039	18.09	1.00	1.34	1.34
HousingSquare	1.38	2.91	0.003	0.063	0.487	0.052	0.382	0.013	13.20	1.09	2.47	2.27
IgnitionCoilMazda13B	1.18	2.30	0.029	0.405	0.363	0.039	0.154	0.010	8.08	0.39	0.38	0.98
Impeller	1.65	3.77	0.009	0.283	0.407	0.104	0.197	0.000	11.36	1.33	1.00	0.75
IntakeMobilPart1	1.48	3.73	0.001	0.253	0.582	0.050	0.108	0.007	11.55	3.54	4.41	1.25
IntakePipeComponent-1	1.24	3.60	0.022	0.427	0.104	0.073	0.368	0.007	5.56	1.14	0.72	0.63
IntakeTrumpet	1.27	8.99	0.081	0.335	0.057	0.140	0.323	0.063	0.41	1.00	0.94	0.94
JettaActuatorBracket	0.87	3.69	0.003	0.091	0.832	0.031	0.042	0.001	6.48	1.36	1.52	1.12
link	0.87	2.76	0.029	0.196	0.606	0.051	0.118	0.000	1.70	3.14	20.21	6.43
LockNuts	1.33	3.00	0.053	0.235	0.221	0.046	0.227	0.218	9.72	1.00	1.75	1.75
LowerThermostatHousing SpacerGM	0.94	2.56	0.019	0.199	0.664	0.035	0.083	0.000	6.64	3.59	12.83	3.57

M20LiftingEyeBolt	1.06	2.30	0.377	0.150	0.031	0.433	0.007	0.003	36.22	0.59	2.39	4.03
ManifoldPlate	0.85	3.16	0.026	0.178	0.534	0.133	0.122	0.007	7.39	4.95	27.54	5.56
MasterCylinderBracket	0.89	5.85	0.004	0.099	0.837	0.030	0.029	0.001	7.48	1.46	0.99	0.68
Miata16IntakeFlange	0.77	3.75	0.041	0.196	0.469	0.190	0.103	0.000	9.27	3.98	36.22	9.09
MitsubishiEVOMAPadapter	1.21	2.11	0.075	0.232	0.435	0.075	0.176	0.007	8.05	2.52	2.45	0.97
NeedleValveScrew	1.01	2.16	0.302	0.401	0.106	0.172	0.018	0.000	13.51	0.21	1.00	4.70
OerlikonBrakeValve	1.43	3.82	0.021	0.227	0.534	0.041	0.165	0.011	18.49	3.21	0.75	0.23
OilCoolerBypassCover PlateForVW	1.18	1.94	0.010	0.137	0.609	0.048	0.175	0.022	8.50	1.44	3.50	2.42
OilFilter	2.16	1.61	0.060	0.592	0.227	0.052	0.055	0.014	11.58	0.79	1.00	1.26
OilPan	1.44	8.07	0.014	0.159	0.568	0.074	0.165	0.021	12.66	6.43	2.14	0.33
OilPanModel2	1.23	12.92	0.038	0.232	0.507	0.039	0.160	0.024	3.62	7.35	0.55	0.07
OldhamCoupling	1.22	1.79	0.004	0.375	0.435	0.023	0.163	0.000	5.61	1.96	1.00	0.51
ParametricFlange	1.19	3.99	0.003	0.271	0.454	0.050	0.219	0.004	15.48	1.99	3.18	1.60
piston	1.36	2.41	0.016	0.500	0.228	0.032	0.219	0.004	17.14	1.00	0.95	0.95
PistonRodPart1	0.88	2.72	0.027	0.170	0.382	0.090	0.311	0.020	7.65	0.35	4.00	11.50
PistonRodPart2	0.88	2.31	0.041	0.320	0.328	0.034	0.265	0.012	6.39	1.97	3.67	1.86
pitch2	1.25	1.91	0.016	0.241	0.476	0.144	0.095	0.027	10.85	1.00	3.82	3.82
PlenumPlate	0.96	5.21	0.023	0.059	0.866	0.051	0.001	0.000	4.97	63.19	2.20	0.03
Porsche968Flange	0.69	3.00	0.024	0.211	0.468	0.092	0.202	0.004	7.27	2.06	18.35	8.89
Porsche968IntakeFlange	0.80	3.64	0.093	0.198	0.249	0.224	0.236	0.001	7.79	28.94	6.87	0.24
PorscheStrutBarTopBrace	0.97	2.61	0.004	0.112	0.845	0.023	0.015	0.000	3.05	21.79	2.14	0.10
PressurePlate	1.40	3.03	0.024	0.295	0.364	0.062	0.252	0.003	12.14	4.00	1.00	0.25
PulleyForAlternator	1.78	3.73	0.080	0.287	0.287	0.051	0.286	0.009	7.45	0.85	0.85	1.00
RockerArm	0.95	2.00	0.019	0.162	0.682	0.027	0.106	0.004	5.58	0.11	0.57	5.14
SkidPlateBracket	0.76	5.96	0.010	0.154	0.753	0.052	0.031	0.001	6.33	0.84	1.28	1.52
socket	1.21	2.02	0.030	0.342	0.369	0.042	0.212	0.005	7.13	1.72	3.38	1.96
SpiralBevelGear	1.10	1.77	0.012	0.403	0.474	0.015	0.095	0.002	11.15	3.67	1.00	0.27
SplitPin	0.79	2.74	0.122	0.795	0.004	0.079	0.000	0.000	0.21	0.04	0.22	5.58
sproket	0.99	2.80	0.043	0.130	0.464	0.122	0.240	0.000	10.23	8.38	0.98	0.12

SpurGear	1.09	3.23	0.008	0.140	0.741	0.024	0.085	0.002	15.40	1.00	9.82	9.82
SteeringKnuckleFlangeSpacer	0.53	1.51	0.006	0.213	0.702	0.031	0.044	0.003	3.25	1.03	22.07	21.33
StraightScrewJoint	1.36	2.20	0.029	0.385	0.282	0.050	0.248	0.006	10.28	1.37	1.58	1.15
T3DividedTurboInletFlange	0.98	2.55	0.009	0.122	0.652	0.044	0.173	0.000	7.77	8.50	1.62	0.19
ThreeTubeJoint	0.53	2.05	0.000	0.000	0.011	0.187	0.792	0.009	0.00	1.15	5.65	4.90
ThrustBearingDisc	1.03	2.90	0.026	0.204	0.541	0.088	0.113	0.027	18.59	1.17	11.82	10.10
TowbarElectricsBracket	0.71	6.79	0.029	0.154	0.744	0.051	0.021	0.000	4.73	0.25	2.07	8.27
TrussBearing	1.29	2.70	0.013	0.203	0.547	0.030	0.205	0.002	8.17	3.05	2.39	0.79
TurboHousing	1.72	6.35	0.171	0.302	0.014	0.130	0.248	0.135	7.33	2.28	1.10	0.48
valve	0.45	2.04	0.097	0.648	0.160	0.095	0.000	0.000	0.30	1.00	0.34	0.34
ValveClip	1.02	1.98	0.010	0.489	0.177	0.103	0.219	0.003	4.87	1.23	2.00	1.62
VWGolfInletFlange	1.02	3.68	0.027	0.230	0.333	0.080	0.324	0.005	5.24	1.74	4.52	2.60
W05Lockwasher	0.57	4.48	0.035	0.207	0.669	0.030	0.057	0.001	8.02	1.00	13.40	13.35
WheelBearingHousingForAVW	1.14	3.15	0.020	0.222	0.379	0.090	0.271	0.018	14.21	1.08	3.41	3.15
WINCHMTGBRK	0.88	5.52	0.006	0.147	0.769	0.020	0.057	0.000	6.37	1.63	1.18	0.73
WormGear	1.08	2.16	0.130	0.545	0.201	0.090	0.033	0.001	9.00	1.00	0.21	0.21
WormGearDesign	1.21	1.99	0.025	0.184	0.469	0.152	0.170	0.000	15.55	1.00	2.80	2.79
WristPin	1.51	3.20	0.007	0.565	0.007	0.017	0.405	0.001	2.73	1.00	0.37	0.37

Appendix C: Extended List of Metrics

Table C1. Potential List of Metrics to Characterize an Object

Feature/ Descriptor	Local or Global	2D / 3D / Both	Shape/Su rface	Description	Relevant (R) Non-Relevant (NR)	Algorithm/ software needed (Y/N), available?	Source
Spin images	Local	3D	Shape	Histogram of local point locations given offset from center, oriented point.	R	Y, available	Johnson and Hebert 1999
Intrinsic Spin Image (ISIs)	Local	3D	Shape	A generalization of spin images to use arbitrary subspaces rather than basic x,y, rectangular coordinate system	NR		
SURF	Local	2D	Surface (texture)	Speeded Up Robust Features (SURF). Local image feature detector and descriptor based on Haar wavelet response. Scale/rotation invariant.	R	Y, available	Bay et al., 2006
Color histograms	Local/ Global	2D	Surface	Histogram of color values in appropriate color space (RGB, HSB)	R		Zivkovic and Krose, 2004
HOG (PHOG)	Local	2D	Surface	Histogram of Oriented Gradients (HOG). Local image feature descriptor. A histogram of local gradient orientations computed on subcells in a region, and normalized by intensity over a larger block.	R	Y, available	Dalal and Triggs, 2005
Self-similarity	Local	2D	Surface	Log-polar histogram descriptor of local point features.	R		Shechtman and Irani, 2007
SIFT	Local	2D	Surface	Scale Invariant Feature Transform (SIFT). Local feature vector computed from histogram of local gradients and intensities.	R	Y, available	Lowe, 2004
2.5D SIFT	Local		Shape + surface	Generalization of SIFT to 2.5D range images.	R		Lo and Siebert, 2009

Feature/ Descriptor	Local or Global	2D / 3D / Both	Shape/Su rface	Description	Relevant (R) Non-Relevant (NR)	Algorithm/ software needed (Y/N), available?	Source
Shape context	Local	Both	Shape + surface (pattern)	Shape context. 2D and 3D point feature computed as log-polar histogram of points, typically along boundaries. Can be generalized to 3D.	R	Y, available	Malik et al., 2001
LESH	Local	2D	Surface	Local Energy Based Shape Histogram (LESH). Local image feature descriptor based on 128-dimensional compact spatial histogram. Scale invariant.	NR		Sarfraz and Hellwich, 2008
MSER	Local	2D	Surface	Maximally Stable Extremal Regions (MSER), A local 2D image detector and descriptor that uses image morphology to find blob patterns.	NR	Y, available	Matas et al, 2002
GLOH	Local	2D	Surface	Gradient Location and Orientation Histogram (GLOH). Enhancement of the SIFT operator to use more spatial regions.	NR		Mikolajczyk and Schmid, 2005
Autocorrelation	Local	2D	Surface	Standard technique for correlating images – power spectrum will indicate whether image region is distinctive and suitable for matching.	NR		Deng et. al, 2007
PCBR	Local	2D	Surface	Principal Curvature-Based Region (PCBR) region detector. A structure based, affine invariant detector that finds curvature maximums in scale space.	NR		Deng et. al, 2007
Corner detectors	Local	2D	Surface	Many versions (described in review article Mikolajczyk et al.) All are local image feature detectors that are sensitive to high curvature, high gradients, and other distinctive image extrema.	R	Y, available	Mikolajczyk et al 2005
ART (ang. Radial)	Global	2D	Surface	Angular Radial Transform (ART). Feature descriptor based on angular decomposition of B&W image to set of radially symmetrical basis functions.	NR		Bober, 2001
RIFT	Local	2D	Surface	Rotation-Invariant Feature Transform (RIFT). Rotational invariant version of SIFT detector.	NR		Lazebnik et al, 2005

Feature/ Descriptor	Local or Global	2D / 3D / Both	Shape/Su rface	Description	Relevant (R) Non-Relevant (NR)	Algorithm/ software needed (Y/N), available?	Source
Shock Scaffold	Global	3D	Shape	The shock scaffold is a hierarchical organization of the medial axis in 3D consisting of special medial points, and curves connecting these points, thereby forming a geometric directed graph	R		Laymarie and Kimia, 2001
3D Zernike Descriptors	Global	3D	Shape	A vector of 3D shape descriptors based on affine invariant moments of 3D point cloud based on Zernike polynomials, which are orthogonal on the unit sphere.	R	Y, available	Novotni and Klein, 2003
Radius-based Surface Descriptor (RSD)	Global	3D	Shape	Symmetric model fitting from point cloud data, using sample consensus to fit generalized cylinders (the approximate radius of the smallest fitting curve to a local neighborhood.)	R	Yes, in ROS/PCL	Marton et al, 2010
PC (Principal Curvature)	Local	3D	Shape	Local shape descriptor of principle curvature of local points. Very general descriptor, generally not useful by itself.	R		Rusu and Cousins, 2011
FPFH (Fast Pt. Ft. Hist.)	Local	3D	Shape	6D pose invariant local shape descriptor that generalizes mean curvature by encoding neighborhood properties in histogram of local normal differential features.	NR		Rusu, Blodow, Beetz, 2009
Global FPFH	Global	3D	Shape	A global shape descriptor that uses the FPFH classification of local nodes in the creation of pairwise histograms between feature points. A ray between each pair of ft. pts. is intersected with nodes and a histogram generated for that pair of the classes of intersecting nodes.	NR		Rusu, Hozbach, Beetz, Bradski, 2009
3D Shape Context	Local	3D	Shape	A local shape descriptor computed by a spherically indexed histogram of local point position around a given point, the north pole given by the surface normal at the given point.	R		Tombari et al, 2010
VFH (Viewpt. Ft. Hist.)	Local	3D	Shape	A local shape descriptor based on the FPFH that integrates the viewpoint normal into the histogram calculations.	R		Rusu, Bradski, Thibaux, Hsu, 2010
Point Signature	Local	3D	Shape	Point descriptor [Chua and Jarvis [CJ97]] used a similar sampling, but recorded the distance from the contour to a plane fit to the contour and passing through the point.	R		Chua and Jarvis, 1997

Feature/ Descriptor	Local or Global	2D / 3D / Both	Shape/Su rface	Description	Relevant (R) Non-Relevant (NR)	Algorithm/ software needed (Y/N), available?	Source
Intrinsic Shape Signatures	Local	3D	Shape	Local 3D measure based on local support compute the Eigen Value Decomposition (EVD) of the scatter matrix of the points belonging to the support. ISS uses as distinctiveness the magnitude of the smallest eigenvalue and the ratio between two successive eigenvalues.	R		Zhong, 2009
Heat Kernel Signatures	Local	3D	Shape	Local measure based on eigenvalue decomposition of heat kernel. Invariant to isometric transformation. Represents decomposition into eigenvalues and eigenfunctions of Laplace-Beltrami operator.	R	Y, available	Bronstein and Kokkinos, 2010
GPS	Global	3D	Shape	A deformation invariant representation of surfaces, the GPS embedding, is introduced using the eigenvalues and eigenfunctions of the Laplace-Beltrami differential operator. It is based on objects of global character, the obtained representation is robust to local topology changes. The GPS embedding captures enough information to handle various shape processing tasks as shape classification, segmentation, and correspondence.	R		Rustamov, 2007
CVFH (Clustered ViewPt. Ft. Hist.	Semi- global	3D	Shape	Local 3D shape descriptor of stable regions using a local reference frame, building a histogram of angles to other points, including Shape Distribution Component (SDC).	R		Aldoma et al, 2012
NARF	Local	3D	Shape	Normal Aligned Radial Feature is a local 3D shape detector and descriptor for point cloud data, a histogram of curvature changes along radial directors.	R		Steder et al., 2010
HK Segmentation	Local	3D	Shape	Gaussian (K) and mean (H) curvature measures computed for each local point.	R	Y, available	Besl and Jain, 1986
SC Shape Index	Local	3D	Shape	A revised version of H and K that decouples the shape characteristic (nature of curvature) and shape strength (magnitude of curvature.)	R	Y, available	Koenderink and van Doorn, 1992
Degree of symmetry/Bilateral or radial symmetry	Global	Both	Shape	Some number which shows how symmetric an object is.	NR		

Feature/ Descriptor	Local or Global	2D / 3D / Both	Shape/Su rface	Description	Relevant (R) Non-Relevant (NR)	Algorithm/ software needed (Y/N), available?	Source
Chirality	Global	Both	Shape	Chirality is a property of asymmetry important in several branches of science. An object or a system is chiral if it is not identical to its mirror image, that is, it cannot be superposed onto it.	NR		
Compactness	Global	Both	Shape	The compactness measure of a shape, sometimes called the shape factor, is a numerical quantity representing the degree to which a shape is compact The compactness measure of a shape, sometimes called the shape factor, is a numerical quantity representing the degree to which a shape is compact	R	Y, available	MacEachren, 1985
Convexity	Global	Both	Shape	Definition 1. For a given 3D closed mesh M, where the convex hull of M is CH(M), we define its convexity measure C1(M) as $C1(M) = \text{Volume}(M) / \text{Volume}(\text{CH}(M))$ Definition 2. For a given 3D closed mesh M, where the convex hull of M is CH(M), we define its convexity measure C2(M) as $C2(M) = \text{SurfaceArea}(M) / \text{SurfaceArea}(\text{CH}(M))$	R	Y, available	Žunić, J. and Rosin, P. L., 2004
Ellipticity	Global	Both	Shape	How elliptical is the 3D model?	NR		Aktaş and Žunić, 2011
Rectangularity	Global	Both	Shape	How rectangular is the 3D model?	NR		Rosin, 2003
Rectilinearity	Global	Both	Shape	How rectilinear is the 3D model?	NR		Žunić, J. and Rosin, P. L., 2003
Triangularity	Global	Both	Shape	How triangular is the 3D model	NR		Rosin, 2003
Roundness	Global	3D	Shape	Roundness is the degree of smoothing due to abrasion of sedimentary particles. It is expressed as the ratio of the average radius of curvature of the edges or corners to the radius of curvature of the maximum inscribed sphere.	R	Y, available	Wadell, 1932

Feature/ Descriptor	Local or Global	2D / 3D / Both	Shape/Su rface	Description	Relevant (R) Non-Relevant (NR)	Algorithm/ software needed (Y/N), available?	Source
Sphericity	Global	3D	Shape	Sphericity is a measure of how spherical (round) an object is. As such, it is a specific example of a compactness measure of a shape.	NR	Y, available	Mora and Kwan, 2000
Volume	Global	3D	Shape	Volume of model	R	Y, available	Corney et al., 2002
Surface area	Global	3D	Shape	Surface area of model	R	Y, available	Corney et al., 2002
Volume/Surface Area	Global	3D	Shape	Volume/Surface Area of model	R	Y, available	Corney et al., 2002
Bounding box aspect ratio	Global	3D	Shape	Ratio of the longest edge to the shortest edge.	R	Y, available	Corney et al., 2002
Crinkliness	Global	3D	Shape	Defined as the surface area of the model divided by the surface area of a sphere having the same volume as the model.	NR		Jayanti et al., 2006
Hull compactness	Global	3D	Shape	Non-dimensional ratio of convex hull's surface area cubed to volume of convex hull squared	NR		Corney et al., 2002
Number of facets	Global	3D	Shape	Number of facets on the model	NR		Corney et al., 2002
Number of holes	Global	3D	Shape	No of holes in a 3D model	R		Corney et al., 2002
Hull crumpliness	Global	3D	Shape	Ratio of object surface area to surface area of its convex hull	NR		Corney et al., 2002
Hull packing	Global	3D	Shape	% of convex hull volume not occupied by original object and is equal to: $1 - \frac{V_{model}}{V_{hull}}$	NR		Corney et al., 2002
D1	Global	3D	Shape	Histogram of radius	R	Y, available	Osada, R., Funkhouser, T., Chazelle, B. and Dobkin, D

Feature/ Descriptor	Local or Global	2D / 3D / Both	Shape/Su rface	Description	Relevant (R) Non-Relevant (NR)	Algorithm/ software needed (Y/N), available?	Source
D2 Shape distribution	Global	3D	Shape	A histogram of distances between pairs of points on the surface	R	Y, available	Osada, 2001 (in Shilane et al., 2006)
Moments	Global	3D	Shape	Moment (Hu, Zernike, etc) of models	R	Y, available	Novotni and Klein, 2003
Extended Gaussian images (EGI)	Global	3D	Shape	Spherical function giving the distribution of surface normals	R		Horn, 1984 (in Shilane et al., 2006)
Shape histograms - SHELLS	Global	3D	Shape	Histogram of distances from the center of mass to points on the surface	R		Ankerst et al., 1999 (in Shilane et al., 2006)
Shape histograms - SECTORS	Global	3D	Shape	A spherical function giving the distribution of model area as a function of spherical angle	R		Ankerst et al., 1999 (in Shilane et al., 2006)
Spherical harmonic descriptor (SHD)	Global	3D	Shape	A rotation invariant representation of the GEDT obtained by computing the restriction of the function to concentric spheres and storing the norm of each (harmonic) frequency	R	Y, available	Kazhdan et al. 2003 (in Shilane et al., 2006)
Spherical extent function (EXT)	Global	3D	Shape	A spherical function giving the maximal distance from center of mass as a function of spherical angle	R		Saupe and Vranic, 2001 (in Shilane et al., 2006)
Radialized spherical extent function (REXT)	Global	3D	Shape	A collection of spherical functions giving the maximal distance from center of mass as a function of spherical angle and radius	R		Vranic 2003 (in Shilane et al., 2006)
3D Wavelet descriptor	Global	3D	Shape	They propose the usage of spherical wavelet transform as a tool for the analysis of 3D shapes represented by functions on the unit sphere. We introduce three new shape descriptors extracted from the spherical wavelet coefficients, namely: (1) a subset of the spherical wavelet coefficients, (2) the L1 and, (3) the L2 energies of the spherical wavelet sub-bands.	R		Laga H. et al., 2006
Skeleton descriptor	Global	3D	Shape	Skeleton descriptor	R		Li, Chunyuan, 2013
Reeb graph descriptor	Global	3D	Shape	Skeleton descriptor	R		Li, Chunyuan, 2013

Feature/ Descriptor	Local or Global	2D / 3D / Both	Shape/Su rface	Description	Relevant (R) Non-Relevant (NR)	Algorithm/ software needed (Y/N), available?	Source
Light field descriptor (LFD) – View base	Global	3D	Shape	A representation of a model as a collection of images rendered from uniformly sampled positions on a view sphere. The distance between two descriptors is defined as the minimum L1-difference, taken over all rotations and all pairings of vertices on two dodecahedra.	R	Y, available	Chen et al., 2003 (in Shilane et al., 2006) [10]
DESIRE	Global	3D	Shape	Composite 3D-shape feature vector (DESIRE), which is formed using depth buffer images, silhouettes, and ray-extents of a polygonal mesh.	R	Y, available	Vranic, D. V
View based with 2D Polar-Fourier coefficients, Zernike moments and Krawtchouk moments, 2D Discrete Wavelet coefficients	Global	3D	Shape	View based method, based on Polar-Fourier coefficients, Zernike moments and Krawtchouk moments, 2D Discrete Wavelet coefficients	R		Daras and Axenopoulos (2009) and Papadakis,, et al., 2010
Convex Hull Histogram (CHH)	Global	3D	Shape	Compute the 3D convex hull for a given model using the Quickhull [Barber et al., 1996] algorithm. Then build a histogram of the pairwise distances based on the points obtained from the convex hull [Boutin and Kemper, 2004, Kalyanaraman et al. 2005]. This method is identical to the basic idea described in [Rea et al, 2005] which presents a detailed study analyzing the merits of this method.	R		Jayanti et al., 2006
3D shape histogram—Solid Angle Histogram	Global	3D	Shape	A histogram based on the Solid Angle between random points	R		Ankerst, M., et al. 1999
Similarity metrics (L1, L2, etc), Bag of words approach, Sparse coding, classifier, etc		Both	Both	General purpose tools	R	Y, available	Ohbuchi, et. al., 2008
Harmonic shape context	Local	3D	Shape	Harmonic shape contexts (HSC) local features are invariant to translation, scale, and 3D rotation.	R	Y, available	Frome, et al., 2007

Feature/ Descriptor	Local or Global	2D / 3D / Both	Shape/Su rface	Description	Relevant (R) Non-Relevant (NR)	Algorithm/ software needed (Y/N), available?	Source
Blowing bubbles (L1)	Local	3D	Shape	Blowing bubbles intersects the surface with a set of concentric spheres and extracts information about the surface in two steps. First, they simply count the number of closed contours, ignoring curves that are far away.	NR	Y, available	Heider, et al., 2011
Geodesic fans (L5)	Local	3D	Shape	Geodesic fans sample a metric (such as curvature) on the mesh using concentric geodesic rings instead of spheres. Geodesic fans re-sample the metric into evenly spaced samples in the radial and angular direction.	NR	Y, available	Heider, et al., 2011
Splash descriptor (L2)	Local	3D	Shape	3D mesh descriptor that computes normal information along 3D curves of maximum curvature and converts to 2D curve that encodes local curvature and torsion	NR		Stein and Medioni, 1992
Point descriptor (l7)	Local	3D	Shape	Point descriptor [Chua and Jarvis] used a similar sampling, but recorded the distance from the contour to a plane fit to the contour and passing through the point	NR	Y, available	Chua and Jarvis
Normal Distribution	Local	3D	Shape	It is a local feature based on the normal distribution.	R	Y, available	Heider, et al., 2011
Curvatures: mainly four curvature values, Mean, Gaussian, Shape and Curvature index (SI, CI) [L2]	Local	3D	Shape	Based on the Curvatures values the following features are calculated: Mean, Gaussian, Shape and Curvature index.	R	Y, available	Heider, et al., 2011
Geodesics, heat and diffusion	Local	3D	Shape	Geodesic and Heat diffusion: The techniques in this class do not directly measure the geodesics, but instead measure a diffusion process flowing along the geodesics.	R	Y, available	Bronstein, 2011

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