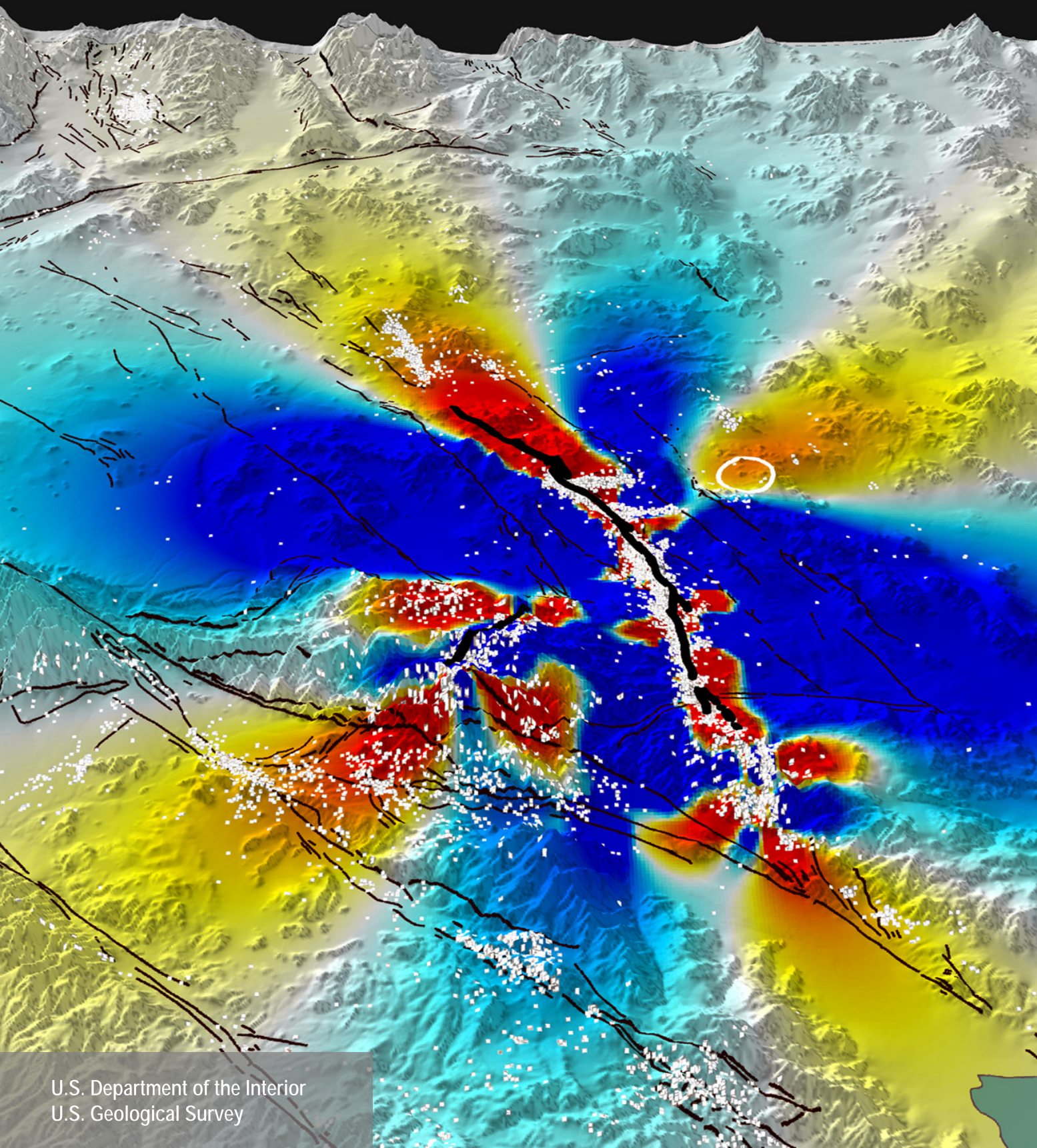


# Coulomb 3.3



**Graphic-Rich Deformation and Stress-Change Software**  
for Earthquake, Tectonic, and Volcano Research and Teaching—User Guide

Open-File Report 2011-1060





# **Coulomb 3.3 Graphic-Rich Deformation and Stress-Change Software for Earthquake, Tectonic, and Volcano Research and Teaching— User Guide**

By Shinji Toda, Ross S. Stein, Volkan Sevilgen, and Jian Lin

Open-File Report 2011–1060

**U.S. Department of the Interior  
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#### FRONT COVER

Coulomb stress change at 7.5 km depth imparted by the 1992 M=7.3 Landers, California,  
earthquake to the surrounding crust, together with the next 7 years of M≥2 aftershocks. The  
calculation is from King and others (1994). The Coulomb image has been draped over relief  
in ArcGIS by Serkan Bozkurt (AMEC/Geomatrix; formerly USGS).



# **Coulomb 3.3 Graphic-Rich Deformation and Stress-Change Software for Earthquake, Tectonic, and Volcano Research and Teaching— User Guide**

By Shinji Toda<sup>1</sup>, Ross S. Stein<sup>2</sup>, Volkan Sevilgen<sup>3</sup>, and Jian Lin<sup>4</sup>

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jlin@whoi.edu

Coulomb is intended for teaching and research. If you use Coulomb in research that you submit for publication, we ask only that you cite these two papers:

Toda, S., R. S. Stein, K. Richards-Dinger and S. Bozkurt, 2005, Forecasting the evolution of seismicity in southern California: Animations built on earthquake stress transfer, *Journal of Geophysical Research*, v. 110, B05S16, doi:10.1029/2004JB003415.

Lin, J. and R.S. Stein, 2004, Stress triggering in thrust and subduction earthquakes, and stress interaction between the southern San Andreas and nearby thrust and strike-slip faults, *Journal of Geophysical Research*, v. 109, B02303, doi:10.1029/2003JB002607.

## *What's New in Coulomb 3.3*

### • New Menu Features

“.inp” (rt.lat/reverse slip) and “.inr” (rake/net slip) input file options to define source and receiver faults

Coulomb now outputs to GMT using a command window plug-in script.

You can now digitize a fault from an image and quickly bring it into Coulomb.

Fault elements are now numbered, so it is easy to find the one you want to change. The number is located at the "start" end, so you can also more easily confirm the dip polarity is correct. These identification numbers can be turned off in the Preferences menu.

In making A-B cross sections, A no longer needs to be to the left of B. The cross-section parameters are saved; you can read them from the cross-section dialog box.

For “3D View” images with slip scaled by a color, you can change the color saturation on the fly.

Both horizontal and vertical GPS displacements can be plotted, with station identification numbers.

Coulomb now reads the fault element lines in the input file rather than using "#fixed," in the .inp.

Once the grid size or calculation depth is changed from Functions→Change parameters menu, the 2D (2-dimensional) map image is automatically refreshed.

You can now taper or subdivide a fault on the fly by clicking on it in map view, which brings up the "Change parameters" menu.

Coulomb now launches quickly without accessing the web database.

When calculating stress on nodal planes, you can now plot the stress change for the plane in each pair that is most positive or most negative, and you can save the graphic as a raster or vector image.

### • New Plug-in Functions (scripts that you type into the MATLAB Command Window)

**digitize\_faults:** This allows you to quickly but accurately digitize active faults and other elements from a .jpeg or .png image with a graphical user interface. The saved text file can be read from the Overlay→Active faults menu in Coulomb.

**another\_overlay:** If the map is changed to "lon & lat" format, simply draw lines on the main graphic window. This is useful to superimpose another fault database, country borders, and so on. User can set the line color and line width by an input dialog.

**more\_overlay\_plot:** This enables you to add numerous active fault files or other overlay material that has been saved as a text file.

**coulomb2gmt\_source:** This code converts the source fault image (as vector data) into the GMT formatted line data. It saves the files, "gmt\_fault\_calc\_depth.data", "gmt\_fault\_map\_proj.data" and "gmt\_fault\_surface.data".

**coulomb2gmt\_cout:** This converts the calculated Coulomb matrix data into the gmt text column data (lon, lat, Coulomb stress change), so that it can be plotted in GMT draped over a DEM as a raster image. It saves a file named "coulomb\_out.dat"

**seis\_rate\_change:** This allows you to read in a seismic catalog, choose the minimum magnitude (for example, Mc), select a smoothing radius, identify the date and time of the event (for example, a large earthquake), and then calculate the seismicity rate change associated with the event, with colors scaled by log (new rate/old rate). Two maps are produced, one to show the seismicity rate where it is defined, and the other to show the undefined areas. Earthquakes can be overlaid on the map.

Now changes to the **Preferences** are saved on the fly; you no longer have to quit and relaunch.

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## Chapter 1

## Introduction

### 1.1 Why Coulomb? The Rationale and Philosophy of This Program

Coulomb is intended both for publication-directed research and for college and graduate school classroom instruction. We believe that one learns best when one can see the most and can explore alternatives quickly. So the principal feature of Coulomb is ease of input, rapid interactive modification, and intuitive visualization of the results. The program has menus and check-items, and dialogue boxes to ease operation. The internal graphics are suitable for publication, and can be easily imported into Illustrator, GMT, Google Earth, or Flash for further enhancements.

Coulomb is designed to let one calculate static displacements, strains, and stresses at any depth caused by fault slip, magmatic intrusion, or dike expansion/contraction. One can calculate static displacements (on a surface or at GPS stations), strains, and stresses caused by fault slip, magmatic intrusion, or dike expansion. Problems, such as how an earthquake promotes or inhibits failure on nearby faults, or how fault slip or dike expansion will compress a nearby magma chamber, are germane to Coulomb. Geologic deformation associated with strike-slip faults, normal faults, or fault-bend folds is also a useful application. Calculations are made in an elastic halfspace with uniform isotropic elastic properties following Okada (1992)—see list of key papers in section 1.9.

There is substantial evidence to support the hypothesis that faults interact by the transfer of stress, both on the time scales of earthquake sequences and aftershocks and on longer time scales associated with the interevent time of the largest shocks that occur in a given region. There is also evidence that faults and magmatic systems interact as well, and that static stress changes influence intrusions and eruptions. Processes not included in Coulomb are also important, such as dynamic stresses, pore-fluid diffusion, and viscoelastic rebound. Further, elastic stiffness differences between basins and crustal layering modify the stresses in comparison to the elastic halfspace implemented in Coulomb. Nevertheless, we believe that a simple tool that permits exploration of a key component of earthquake interaction has great value for understanding and discovery.

### 1.2 Hardware/software requirements:

- **Macintosh OSX, Windows PC, or UNIX computer**
- **MATLAB 7.4 or higher is required.** There are a few MATLAB functions that work on PCs but not Macs. MATLAB 7.5 is not advised; it is full of bugs; there are strain problems with MATLAB 7.4.
- A color monitor of at least 600 x 400 pixel resolution. A laptop screen is fine.
- A text editor to modify ascii input files, and a spreadsheet to read tab-delimited text files. Some output files are created as .csv (Excel-friendly) files. Use a text editor that allows you to distinguish spaces from tabs, such as *BEdit* (*BEdit Lite* is free from <http://www.barebones.com/>) or *Notepad* on a Windows PC. Use a nonkerning (uniform-spacing) font, such as Monaco, so that numbers stay aligned.

### 1.3 Recommended extras:

- A vector illustration program, such as *Adobe Illustrator*, is strongly recommended.
- *Google Earth* (which is free)

### 1.4 Users Guide Alerts

1. **Important warnings in the manual are printed in red**
2. The images used in the manual to show you what you will see on the screen were captured at low resolution (72 dpi). *But don't worry:* you will save full-resolution vector files.



## 1.5 Help menu

This can be useful; there is a search command, but unlike this Guide, we have not kept it current.

## 1.6 Cover images

The full-page cover was designed by Serkan Bozkurt (now at AMEC/Geomatrix) by importing Coulomb numerical output into ArcGIS. All of the images on the inside covers were made exclusively from Coulomb 3.3.

## 1.7 Acknowledgments

We thank many users for testing the functions, finding errors, and suggesting improvements. We are particularly grateful to Chris Rollins (University of Southern California) and Gavin Hayes (U.S. Geological Survey, National Earthquake Information Center).

## 1.8 Some useful papers that explain and explore the Coulomb hypothesis

(Most are downloadable from <http://profile.usgs.gov/rstein>)

*Introduction without jargon or math:*

Stein, R.S., 2003, Earthquake conversations: Scientific American, v. 288, no. 1, p. 72-79.

*Key review papers:*

Harris, R.A., 1998, Introduction to special section—Stress triggers, stress shadows, and implications for seismic hazard: Journal of Geophysical Research, v. 103, p. 24,347–24,358.

Stein, R.S., 1999, The role of stress transfer in earthquake occurrence: Nature, v. 402, p. 605–609.  
King, G.C.P., and Cocco, M., 2000, Fault interaction by elastic stress changes; new clues from earthquake sequences: Advances in Geophysics, v. 44, p. 1–36.

Freed, A., 2005, Earthquake triggering by static, dynamic, and postseismic stress transfer: Annual Review of Earth and Planetary Sciences, v. 33, p. 335–67, doi: 10.1146/annurev.earth.33.092203.122505

Steacy, S., Gomberg, J., and Cocco, M., 2005, Introduction to special section—Stress transfer, earthquake triggering, and time-dependent seismic hazard: Journal of Geophysical Research, v. 110, p. B05S01, doi:10.1029/2005JB003692.

*Coulomb stress change concepts (for strike-slip faults):*

King, G.C.P., Stein, R.S., and Lin, J., 1994, Static stress changes and the triggering of earthquakes: Bulletin of the Seismological Society of America, v. 84, no. 3, p. 935-953.

*Coulomb stress concepts (for thrust faults and interaction between thrust and strike-slip faults):*

T. Parsons, T., R.S. Stein, R. W. Simpson and P.A. Reasenber, 1999, Stress sensitivity of fault seismicity; a comparison between limited-offset oblique and major strike-slip faults: Journal of Geophysical Research, v. 104, p. 20183-20202.

Lin, J., and Stein, R.S., 2004, Stress triggering in thrust and subduction earthquakes, and stress interaction between the southern San Andreas and nearby thrust and strike-slip faults: Journal of Geophysical Research, v. 109, p. B02303, doi:10.1029/2003JB002607.

*Coulomb stress calculated on earthquake nodal planes*

Toda, S., J. Lin, and R.S. Stein, 2011, Using the 2011 M=9.0 Tohoku earthquake to test the Coulomb stress triggering hypothesis and to calculate faults brought closer to failure: *Earth Planets Space*, in press.

Ma, K.F., C.H. Chan and R. S. Stein, 2005, Response of seismicity to Coulomb stress triggers and shadows of the 1999  $M_w = 7.6$  Chi-Chi, Taiwan, earthquake: *Journal of Geophysical Research*, Vol. 110, B05S19, doi:10.1029/2004JB003389.

*Dislocation solution formulae:*

Okada, Y., 1992, Internal deformation due to shear and tensile faults in a half-space: *Bulletin of the Seismological Society of America*, v. 82, no. 2, p. 1018-1040.

*Application of Coulomb to seismic hazard:*

Toda, S., Stein, R.S., Reasenberg, P.A., and Dieterich, J.H., 1998, Stress transferred by the  $M_w=6.5$  Kobe, Japan, shock; effect on aftershocks and future earthquake probabilities: *Journal of Geophysical Research*, v. 103, p. 24,543-24,565.

Toda, S., and R.S. Stein, R.S., 2002, Response of the San Andreas fault to the 1983 Coalinga-Nuñez Earthquakes; an application of interaction-based probabilities for Parkfield: *Journal of Geophysical Research*, v. 107, p. 10.1029/2001JB000172.

Toda, S., Stein, R.S., Richards-Dinger, K., and Bozkurt, S., 2005, Forecasting the evolution of seismicity in southern California—animations built on earthquake stress transfer: *Journal of Geophysical Research*, v. 110, p. B05S16, doi:10.1029/2004JB003415.

*Application of Coulomb to dike inflation:*

Toda, S., Stein, R.S., and Sagiya, T., 2002, Evidence from the 2000 Izu Islands swarm that seismicity is governed by stressing rate: *Nature*, v. 419, p. 58-61.

*Application of Coulomb to earthquake-volcano interaction:*

Nostro, C., Stein, R.S., Cocco, M., Belardinelli, M.E., and Marzocchi, W., 1998, Two-way coupling between Vesuvius eruptions and southern Apennine earthquakes (Italy) by elastic stress transfer: *Journal of Geophysical Research*, v. 103, p. 24,487-24,504.

*Other papers cited in the User Guide:*

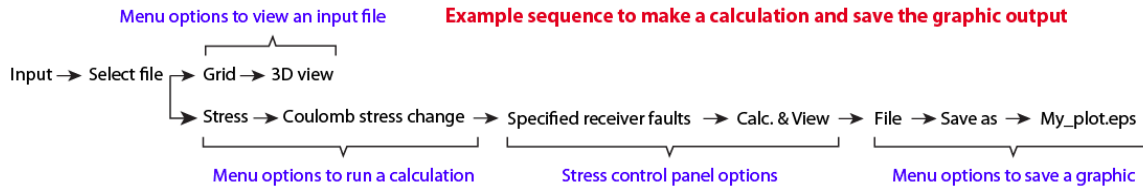
Aki, K., and P. G. Richards, 1980, *Quantitative Seismology*, 932 pp., W.H. Freeman & Co., New York.

Wells, D. L., and K. J. Coppersmith, 1994, New empirical relationships among magnitude, rupture length, rupture width, rupture area, and surface displacement: *Bulletin of the Seismological Society of America*, v. 84, p. 974-1002.

## Chapter 2

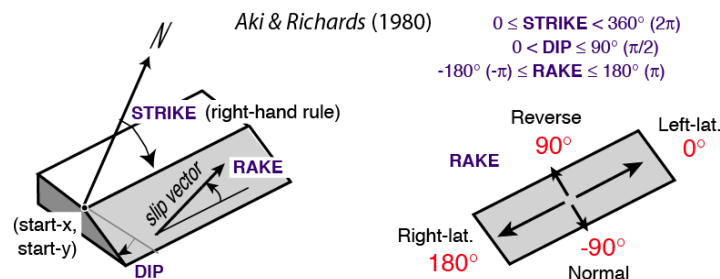
## The Keys to the City, and a Quick Tour

## 2.1 The most important things about Coulomb in one page!



- **Source vs. receiver faults** (Section 3.1)  
Sources have slip and impart stress; receivers do not have slip and receive stress
- **Coulomb failure hypothesis,  $\Delta\sigma_f = \Delta\tau_s + \mu' \Delta\sigma_n$**  (7.1)  
Failure is promoted when  $\Delta\sigma_f$  or  $\Delta CFF$  on the receiver fault caused by slip on the source fault(s) increases.  $\Delta\tau_s$  is the shear stress change (positive in the direction of receiver fault slip),  $\Delta\sigma_n$  is normal stress change (positive when the receiver fault is unclamped), and  $\mu'$  is the effective fault friction coefficient on the receiver fault.
- **How faults are defined in the input files** (4.1)  
Right-hand rule for start/fin points, positive dip, rt-lat/reverse (m) or rake°/net slip(m).
- **Coulomb stress on specified vs. optimally oriented planes** (7.1)  
Assumed slip directions vs. regional stress field; visualizing slip lines, principal axes.
- **Coulomb and MATLAB Figures** (5.4)  
“dead” editable vector .pdf files vs. “live” MATLAB 3D .fig files that can be spun.
- **“inp” vs. “mat” input files** (5.2)  
.inp is editable text; .mat is a binary file, but can include fault and quake overlays
- **Keep an eye on the command window**  
For calculation progress, input/output file names, input source moment, error reports.
- **Start simple, and add complexity if needed later**  
Start with idealized faults and develop intuition about the problem.
- **For classroom instruction, use Cartesian coordinates unless you want to use overlays**  
It’s quicker and easier.
- **How receivers are defined** (7.2)  
Specified faults via Aki-Richards, subdivided receivers, CMTs, and nodal planes:

## Convention for resolving stress and for focal mechanisms

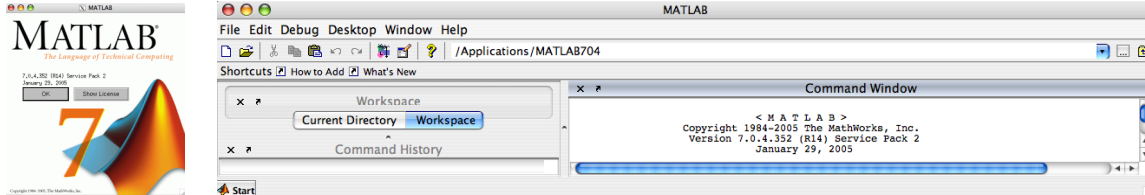





## 2.2 A quick tour of Coulomb 3.3

Here we just want you to learn the procedure to display and output graphics, and to save the results. We always recommend that you save all your current working documents frequently to prevent lost of files in the event of program crashes.

Menus and their pull-down items turn from light white to black as they become options. Here is the procedure to lunch Coulomb:



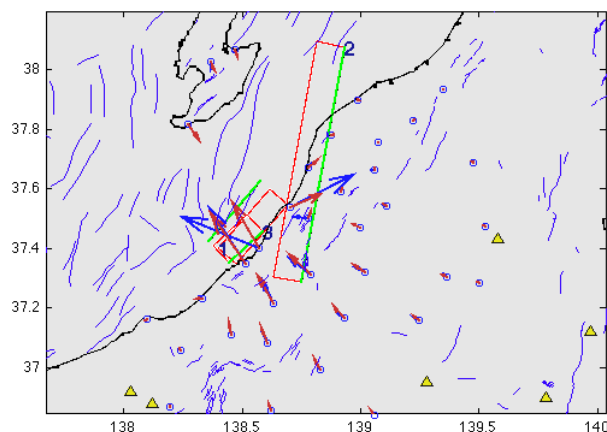
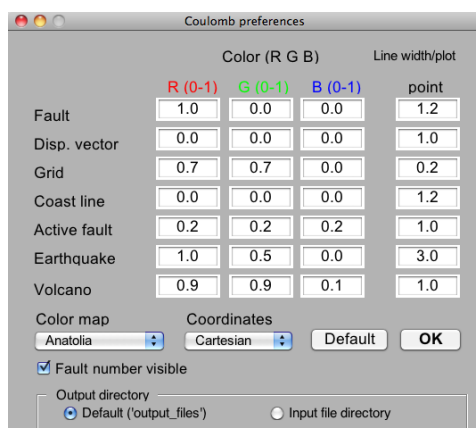
1. Launch MATLAB on your computer. In the MATLAB menu bar top line, click on the  icon to browse to the location of the “Coulomb 3.3 folder” in your computer. In the example shown below, the “Coulomb 3.3 folder” has a path of “/Users/jlin/Desktop/Coulomb folder”.



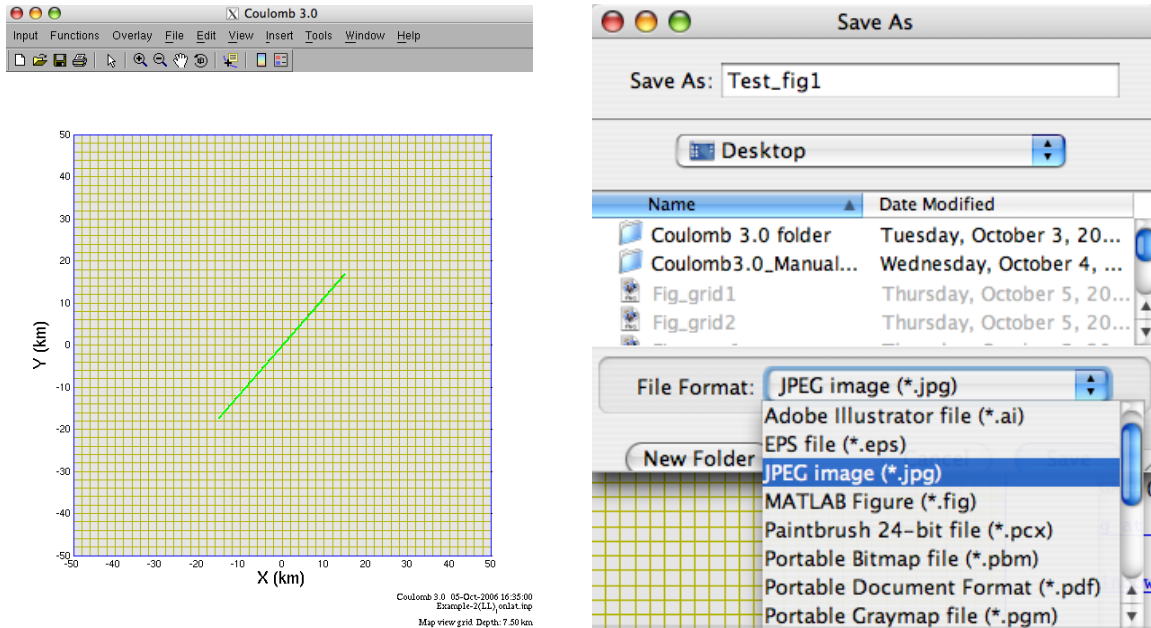
2. In the MATLAB Command Window, type “coulomb”. Coulomb will take 10 seconds or so to launch. Check the Coulomb website to check that you have the latest version. We recommend that you always migrate to the latest version.



```
>> coulomb
=====
Welcome to Coulomb 3.2.01
=====
Start from Input menu to read or build an input file.
```

3. Choose **Input > Preferences**. Colors, line widths, the “color map” (color gradient maps), and the output file folder can all be changed. For input files with lat/lon information, you can also choose to plot maps with lat/lon rather than km frame tics. For now, leave them in the default setting. Note that “Fault” refers to the source or receiver faults. Fault ID numbers can be unchecked. For volcanoes, “point” controls the size the triangles. Changing the Grid point size to 0 removes the grid lines for plots with many overlays, as you see on the right below.



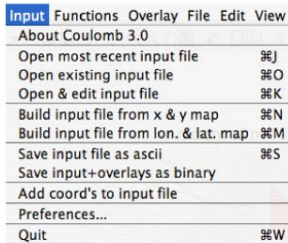
4. In the pop-up Coulomb 3.3 window, choose **Input > Open existing input file**. In the pop-up *Open input file* window, change to sub-directory “input\_files”. Choose the “Example-2(LL)\_lonlat.inp” from the dialog box, then hit <rtm>. The program will automatically plot the **2D map view** of the **Grid** menu in **Functions**.
5. Once you release the mouse button, the calculation is performed and the program displays the result in the *Coulomb 3.3* window. It's a simple grid with a NE-striking fault in the middle of the grid, as shown below. The bottom right corner also shows the version of the Coulomb program you are using, current date/time, name of the input file you are using, type of calculation for the image, and the calculation depth.



6. Now try **Functions > 3D grid**, and play with the zoom  and swivel  tools. If you want to save this image, choose **File > Save As**. Rename the file in the dialog box, and save it as a figure of one of the several types. Do not use “main\_menu\_window.fig” as the filename.
7. You also have the options to **Zoom In**, **Zoom Out**, **Pan**, and **Rotate** your image by clicking on the lower line on the Coulomb 3.3 menu bar. You can also perform these operations by choosing items in the **Tools** pull-down menu.
8. If you click **Functions > Displacements**, in addition to making an image on your Coulomb 3.3 window, a numerical output file called “Displacement.cou” will appear in the sub-folder you designated in the Preferences menu. Similarly, if you click **Functions > Stress**, a text output file called “dcff.cou” will be created and can be opened in Excel.
9. To close the Coulomb 3.3 window, click **Input > Quit**. Do not quit out of MATLAB if you want to continue with Coulomb. (If you wanted to quit MATLAB program, type “exit” in the MATLAB Command Window.)

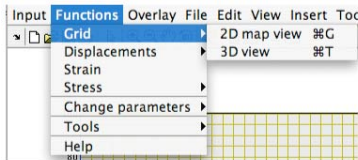
## Coulomb Menu Guide

### Input



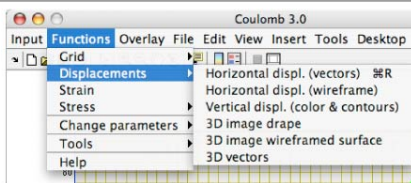
You can use ascii (.inp) or binary (.mat) files as an input file, in input file window you should specify the input file format to make it active.

### Functions > Grid

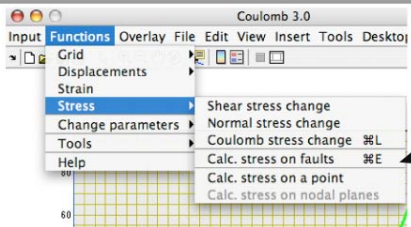


2D Map view is the default first plot for all input files.

### Functions > Displacements



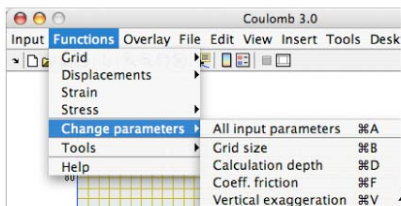
### Functions > Stress



Friction coefficient is 0.4 as a default value  
To modify use Functions > Change parameter > Coeff. friction

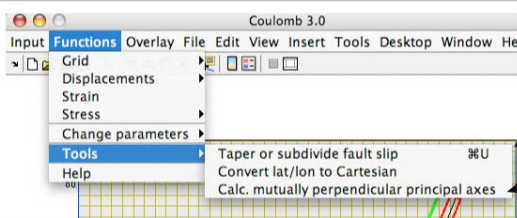
This is stress resolved on a plane in a given rake direction.

### Functions > Change Parameters



This is for displacement options

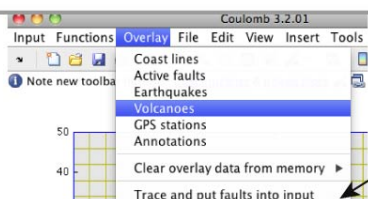
### Functions > Tools



These tools permit more realistic simple input files (taper) or variable slip tiles (subdivide).

Used to set regional stress needed for optimally oriented Coulomb stress change plot

### Overlay



You must clear overlays before replacing them with new ones  
You should save input as a .mat file so these overlays are kept.

This option builds input source or receiver faults by tracing them from the screen



## Chapter 3

## Concepts, Dimensions, and Sign Conventions

This chapter briefly explains the things you should understand to use the software correctly.

### 3.1 The crucial concept of source and receiver faults

**Source faults have slip**, and so they impart stress to the surrounding crust and faults. **Receiver faults (almost always) have no slip** (slip=0.0 m in the input files). Source and receiver faults otherwise look identical in the input files. The stresses imparted by source faults are resolved on the receiver faults through the command **Functions > Stress > Calc. stress on faults**. Further options for resolving the stress on the receiver fault are controlled by the **Stress on faults control panel**, which automatically appears.

### 3.2 Calculation procedure

1. Launch MATLAB; set the MATLAB path to working directory “Coulomb 3.3 folder”.
2. Type “coulomb” in MATLAB Command Window.
3. In Coulomb 3.3 window menu bar, choose **Input > Open existing input file**.
4. In Coulomb 3.3 window menu bar, choose **Functions > Grid, Displacements, Strain, or Stress**. Many of these selections trigger requests for additional input and let you modify the parameters in temporary windows. When you click “Calc. & view”, calculations are performed and a new image is displayed.
5. You can perform many operations to the image on the Coulomb 3.3 window, including **Zoom In, Zoom Out, Pan, Rotate 3D, Data Cursor, Insert Color Bar, Insert Color Legend**. You can choose these operations either by clicking the lower menu in the Coulomb 3.3 window or the **Tools** pull down menu bar. While the graphic plot is open, you **save** this plot.
6. To **print a plot**, save it as a pdf and then print the small vector file from *Acrobat Reader* or an illustration program. The File > Print cmd in MATLAB does not work properly.
7. After you have finished all calculations, quit MATLAB.

### 3.3 To change parameters interactively

Most of the settings and parameters can be changed either by modifying an input file using a text editor or by changing them interactively within Coulomb. Choose **Functions > Change parameters**. Parameters changed within the software interactively are transient and will not permanently modify the input file. Every time you select **Input > Save input file**, all current selections will be saved in an input file. Change the name of the file if you do not want it overwritten.

### 3.4 To save, print, or modify a plot

Choose **File > Save A**. We recommend you choose **eps**, a compact vector format; generally quality is lower when saved as **pdf**. **Rename the file from the default “main\_menu\_window.fig” or it will overwrite an important file**. You then print the pdf from *Preview* (Mac) or *Acrobat Reader*, or from an illustration program if you would like to spruce it up.

### 3.5 Coordinates, units, and sign conventions

Coulomb 3.3 calculates in the  $(x, y, z)$  Cartesian coordinate system. When the lat/lon of the corner grid points are specified in the input file, it can also plot in lat/lon. In the map view projection on the monitor,  $x$  is positive from left to right,  $y$  is positive from bottom to top,  $z$  is positive upwards for displacement. DEPTH is positive downwards from the Earth’s surface. We use the standard Aki and Richards (1980, 2002) sign conventions for fault geometry and slip.

**Input parameters and their dimensions** (think bars and meters)

PR1 Poisson's ratio: dimensionless, -1 to 0.5; 0.25 is typically used. 0.5 is an incompressible volume, and so can be used to make "balanced cross-sections" of structural geology.

E1 Young's modulus: [bars];  $8 \times 10^5$  bars is typically used.

FRIC Friction coefficient: [dimensionless; roughly 0-1]; 0.4 is often used; 0.65 is for dry Byerlee's law friction, 0.0-1.0 is typically considered the limits for the crust.

Sym Obsolete legacy from Coulomb 1.0; ignore it

Directions, angle, and dip: [degrees; **dip must be positive!!**]

Grid and fault positions ( $x, y$ ): [km]

Depth: [km] downward is positive

Displacements: [m]

Faults: Right-lateral is positive, and reverse slip is positive [m]

Dikes: Opening displacement is positive [m]

Point Source: Inflation is positive [ $\text{m}^3$ ]

Regional stress tensor, S1, S2, S3: positive in compression [bars]

**Output parameters and their dimensions**

Displacement: [m] North, East, and Up are positive

Shear Strain: [dimensionless] Right-lateral is positive

Principal Strain: [dimensionless] Extension is positive (*tensor notation*)

Dilatational Strain: [dimensionless] Dilatation is positive

Stress: [bars] Right-lateral and unclamping are positive

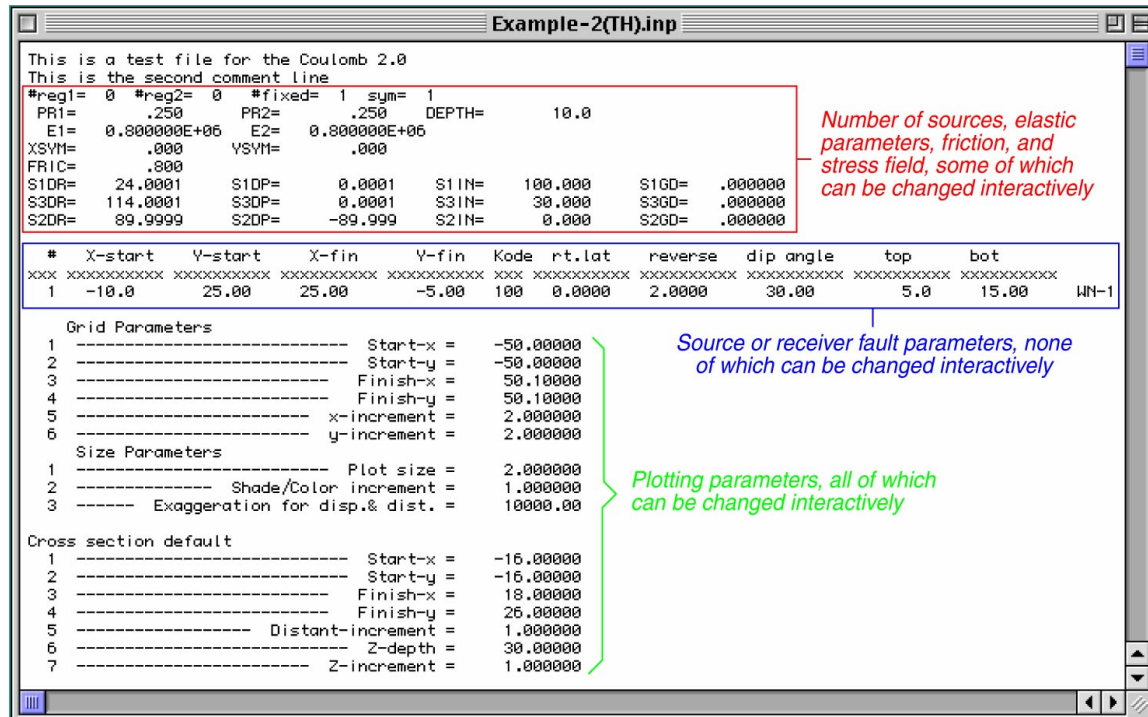
**Shear modulus,  $G$ .** Young's modulus  $E$  and Poisson's Ratio  $PR$  are specified in the input file.

$G = E/[2(1+PR)]$ . So the shear modulus  $G$  for  $PR=0.25$  and  $E=8 \times 10^5$  bars, is  $3.3 \times 10^5$  bars or  $3.3 \times 10^{11}$  dyne-cm<sup>-2</sup>.

## Chapter 4

## Building Input Files

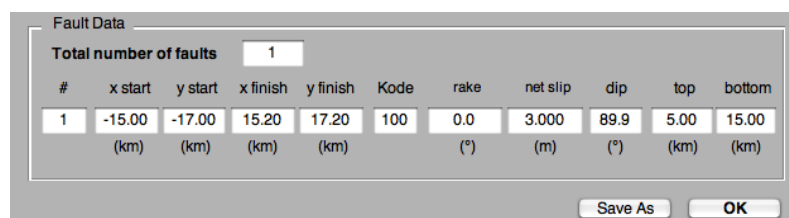
All Coulomb calculations require input files; some require successive information for which you will be prompted. If an input file is improperly formatted (for example, it has tabs, or the number of faults is inconsistent with the “#fixed=”, a warning dialog will appear, but the input file will still be correctly read. If it is a text (.inp) file, you must modify the input using text editor. If it is a binary (.mat) file you cannot use it. You can also create an input file interactively or modify an existing file in Coulomb. Open this input file in a text editor:

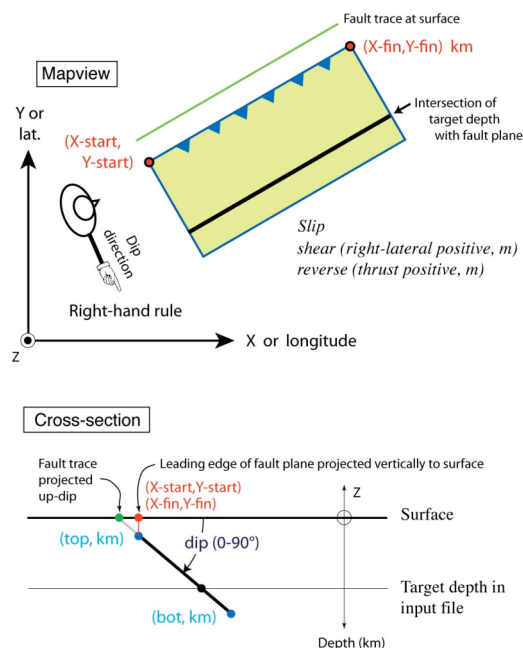


All numbers need a decimal point, except for the line starting “#reg1=” and the first three characters of the source parameters marked “#”. All format statements are shown at the end of this chapter. Right-lateral and reverse slip are reckoned positive (negative values denote left-lateral and normal slip); dip must always be positive. “#reg2=” is an obsolete inheritance from Coulomb 1.0; ignore it.

## 4.1 “.inp” (rt.lat/reverse slip) and “.inr” (rake/net slip) input file options

There are two input formats. The first (.inp) specifies the source slip by right-lateral and reverse slip (left lateral or normal slip are negative). The second is an alternate (.inr) input format specifies rake (°) and net slip, which permits one to calculate the stress change on receivers (faults without slip) in their rake directions, where, for example, a left-lat. stress increase would inhibit failure on a right-lateral fault. Try **Input > Open & edit input file > “Example-2(LL)rake.inr”** to see this:





### 4.3 Working in lat/lon coordinates

Coulomb can read and display lat/lon's if you include the lat/lon of the grid borders and the (0, 0 km) point in the input file, as seen here from "Example-SFBayArea.inp"

```

Cross section default
1 ----- Start-x = -36.00000
2 ----- Start-y = 36.00000
3 ----- Finish-x = 36.00000
4 ----- Finish-y = -36.00000
5 ----- Distant-increment = 1.000000
6 ----- Z-depth = 30.00000
7 ----- Z-increment = 1.000000

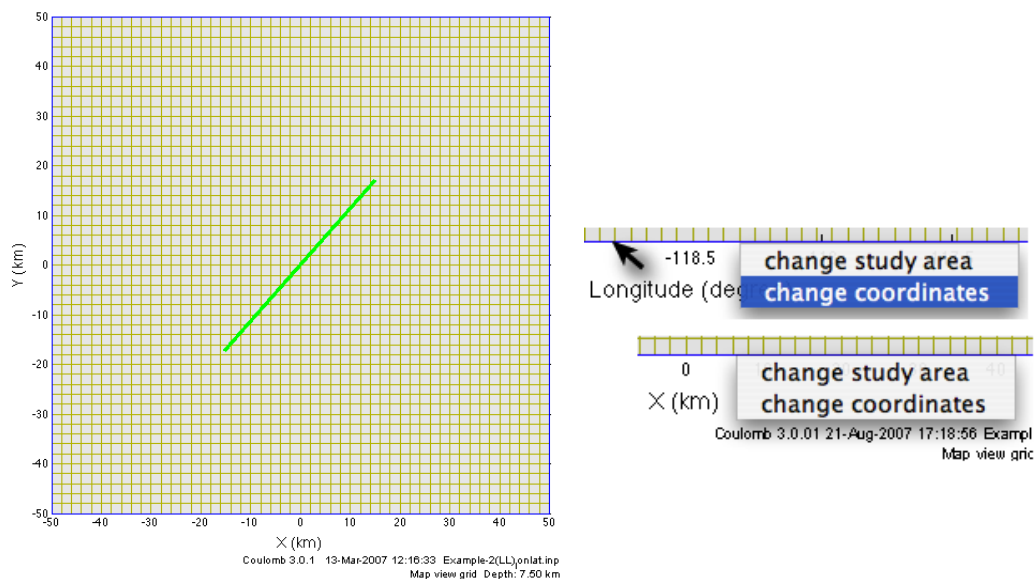
Map information
1 ----- min. lon = -123.0000
2 ----- max. lon = -121.0000
3 ----- zero lon = -122.0000
4 ----- min. lat = 36.0000
5 ----- max. lat = 38.0000
6 ----- zero lat = 37.0000

```

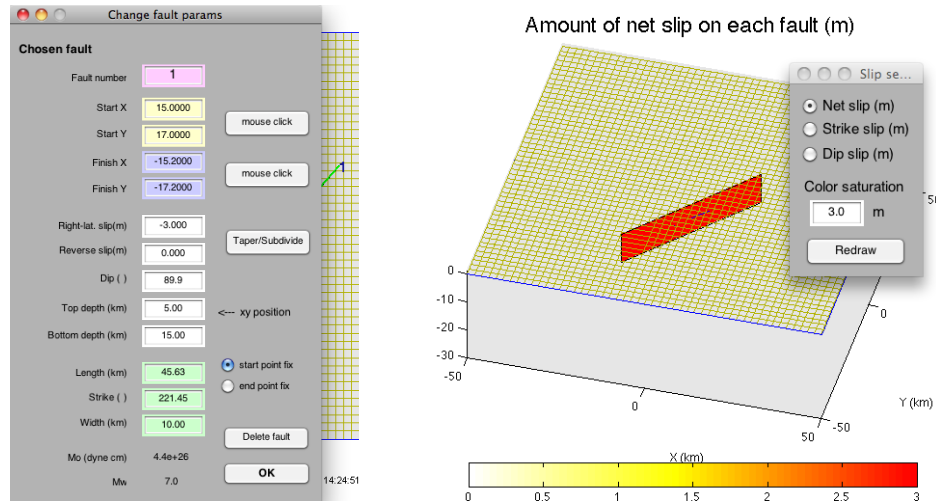
If you have lat/lon information for a source, you can convert it to Coulomb (x, y) input format by selecting **Functions > Tools > Convert lat/lon to Cartesian**, which brings up a calculator window.

### 4.4 To open, display and modify existing input file interactively

1. **Input > Open existing input file** > Example-2(LL)-lonlat.inp in the "input\_files" sub-folder within the "Coulomb 3.3" folder.
2. The graphic on the left below appears in the Coulomb 3.3 window. You can see the undistorted grid (yellow) and the surface projection of the source fault (green).



3. To show the same plot with lat/lon tic marks, put the cursor on the frame numbers and make a right mouse-click (above right). Choose "change coordinates" and make a left mouse-click. Alternatively, from the menu, **Input > Preferences** and change **Coordinates** from "Cartesian to Lon. & Lat.", click OK, and then choose Input > Open most recent input file.
4. To modify, subdivide, or tile a source or receiver fault, click on the fault with the right mouse-click, and it will open the "change fault params" window (below left). You can do the same thing to the blue study area border to change the study area boundaries. If you have multiple faults or a variable slip model, you can see the total seismic moment of all patches in the Command window.



#### 4.5 To display the undistorted grid in 3D view

1. Choose **Functions > Grid > 3D view**. The graphic above right appears in the Coulomb 3.3 window. You can see the undistorted grid in 3D view (yellow) and the fault patches colored by their input slip. You can color the slip by its components, change the color saturation in the Slip menu, and change the viewing angle by clicking on the swivel tool.

#### 4.6 Editing existing input files within Coulomb

Choose **Input > Open & Edit Input File**. The “All input parameters” window will appear as shown below. You can modify all values without any formatting worries. If the “Total number of faults” is greater than 1, enter the order number of a specific fault patch that you wish to modify below “#”. Then click “OK”, properties of that particular source will appear.

The 'All input parameters' dialog box contains the following sections:

- Comment lines:**
  - This is a test file for the Coulomb 3.0
  - This file is prepared to check mainly thrust faulting calculation
- Half space parameters:**
  - Poisson's ratio: 0.25
  - Young modulus: 800000.0 bar
  - Calculation depth: 7.50 km
  - Coeff. friction: 0.4
- Regional stress (only used for optimum stress calc.):**

	strike°	dip°	surface stress	vertical gradient
S1	19.0	-0.0	100.0 bar	0.0 bar/km
S2	90.0	90.0	30.0 bar	0.0 bar/km
S3	109.0	-0.0	0.0 bar	0.0 bar/km
- Study area (grid):**
  - X axis: start -50.00 km, finish 50.10 km, increment 2.00 km
  - Y axis: start -50.00 km, finish 50.10 km, increment 2.00 km
- Fault Data:**

#	x start (km)	y start (km)	x finish (km)	y finish (km)	Kode	rt.lat slip (m)	dip slip (m)	dip (°)	top (km)	bottom (km)
1	15.00	17.00	-15.20	-17.20	100	-3.000	0.000	89.9	5.00	15.00

#### 4.7 Modifying an existing file in a text editor

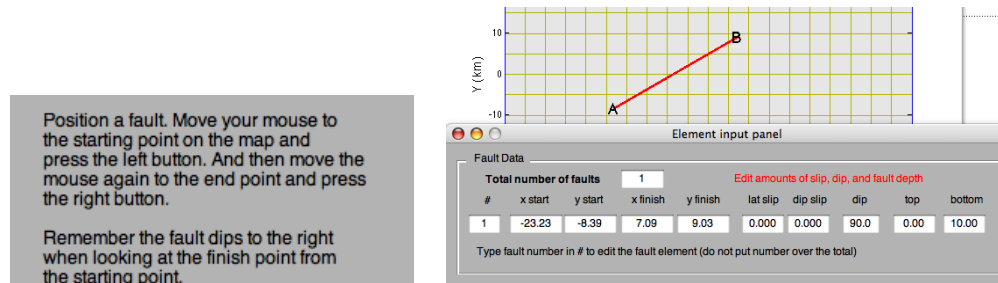
1. Click one of the example files we prepared for tutorials.
2. To duplicate it, type “d” holding command key (command + D), or drag the icon holding option key, and rename it.



3. Launch an editor and open the file using **File > Open** (command + O).
4. Use a non-kerning font, such as Monaco or Courier. Change the numbers you want, checking the units and format. To add source or receiver faults, add a new row. Use your editor's "show invisibles" option to make sure that there are no tabs. Save the file.

## 4.8 Building an input file from a simple X,Y map

To build an input file from map, you can select from menu **Input > Build Input File from x & y Map**; you can add as many faults as you like. You can add lon/lat information of your study area by clicking the "Add lon.lat. info" button in the "Grid input setting" window. Don't worry about the regional stresses for now.



Note that you must close the above cursor message at left before specifying a fault on the following map. Click "OK" and the fault color will turn to green.

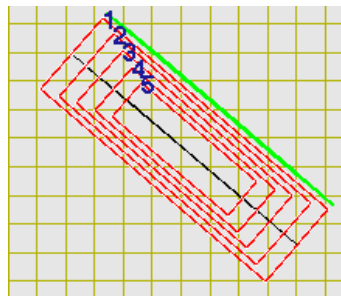
## 4.9 Tapering a source fault and subdividing the slip on a source or receiver

**Tapered Slip.** To remove unrealistic stress concentrations at the edges of a fault, you can taper the slip in Coulomb. Choose **Input > Open an existing file** and choose "Example-2(TH).inp". Then right-click on the fault frame and hit the "Taper/Subdivide" button (or choose **Functions > Tools > Taper or subdivide fault slip**). When the "Element input panel" appears, choose "Linear tapering". The tapered slip is built by nested rectangles. Choose 10 km along strike, 5 km downdip, and 5 nested patches, and hit OK. Save the tapered input file by **Input > Save input file as ascii** with a new name. In an editor you'll see the 5 nested coplanar sources, as shown below. The tapered fault has the same moment as its uniform-slip version.

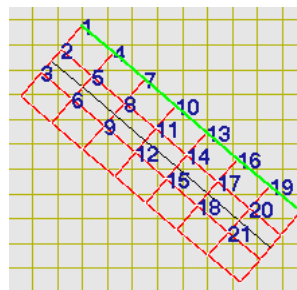
#	X-start	Y-start	X-fin	Y-fin	Kode	rt.lat	reverse	dip angle	top	bot
1	-8.6771	22.7019	22.5266	-4.0441	100	0.0000	0.8664	45.0000	0.8839	14.1161
1	-7.3542	20.4039	20.0533	-3.0882	100	0.0000	0.8664	45.0000	1.7678	13.2322
1	-6.0312	18.1058	17.5799	-2.1323	100	0.0000	0.8664	45.0000	2.6517	12.3483
1	-4.7083	15.8077	15.1065	-1.1765	100	0.0000	0.8664	45.0000	3.5355	11.4645
1	-3.3854	13.5096	12.6332	-0.2206	100	0.0000	0.8664	45.0000	4.4194	10.5806

Notice that the patches get successively smaller on down the list, and that each patch has the same slip. The larger the number of patches, the smoother the stress. The patches with their ID numbers are shown below.

*Tapered slip (for sources only)*



*Subdivided slip (for sources and receivers)*



**Splitting or subdividing a source or receiver.** As you did before, choose **Input > Open an existing file** and choose “Example-2(TH).inp”. Then right-click on the fault frame and hit the “Taper/Subdivide” button as you did before. This time, when the “Element input panel” appears, click on “splitting.” Now choose a 7 x 3 patch subdivision, and hit OK, and you will see the right picture on the previous page. Save the tiled input file by **Input > Save input file as ascii** with a new name, and open it in an editor to see the 21 adjacent coplanar sources (above right), all with the same slip as the initial input file. You can now change the slip on each patch by hand. The input folder contains several examples of these (such as the 1992 M=7.3 Landers, California, and 1995 M=6.9 Kobe, Japan, shocks).

#	X-start	Y-start	X-fin	Y-fin	Kode	rt.lat	reverse	dip angle	top	bot
1	-10.0000	25.0000	-5.0000	20.7143	100	0.0000	2.0000	45.0000	0.0000	5.0000
1	-13.2540	21.2037	-8.2540	16.9180	100	0.0000	2.0000	45.0000	5.0000	10.0000
1	-16.5079	17.4074	-11.5079	13.1217	100	0.0000	2.0000	45.0000	10.0000	15.0000
1	-5.0000	20.7143	0.0000	16.4286	100	0.0000	2.0000	45.0000	0.0000	5.0000
1	-8.2540	16.9180	-3.2540	12.6323	100	0.0000	2.0000	45.0000	5.0000	10.0000
1	-11.5079	13.1217	-6.5079	8.8360	100	0.0000	2.0000	45.0000	10.0000	15.0000
1	0.0000	16.4286	5.0000	12.1429	100	0.0000	2.0000	45.0000	0.0000	5.0000
1	-3.2540	12.6323	1.7460	8.3466	100	0.0000	2.0000	45.0000	5.0000	10.0000
1	-6.5079	8.8360	-1.5079	4.5503	100	0.0000	2.0000	45.0000	10.0000	15.0000
1	5.0000	12.1429	10.0000	7.8571	100	0.0000	2.0000	45.0000	0.0000	5.0000
1	1.7460	8.3466	6.7460	4.0609	100	0.0000	2.0000	45.0000	5.0000	10.0000
1	-1.5079	4.5503	3.4921	0.2646	100	0.0000	2.0000	45.0000	10.0000	15.0000
1	10.0000	7.8571	15.0000	3.5714	100	0.0000	2.0000	45.0000	0.0000	5.0000
1	6.7460	4.0609	11.7460	-0.2249	100	0.0000	2.0000	45.0000	5.0000	10.0000
1	3.4921	0.2646	8.4921	-4.0211	100	0.0000	2.0000	45.0000	10.0000	15.0000
1	15.0000	3.5714	20.0000	-0.7143	100	0.0000	2.0000	45.0000	0.0000	5.0000
1	11.7460	-0.2249	16.7460	-4.5106	100	0.0000	2.0000	45.0000	5.0000	10.0000
1	8.4921	-4.0211	13.4921	-8.3069	100	0.0000	2.0000	45.0000	10.0000	15.0000
1	20.0000	-0.7143	25.0000	-5.0000	100	0.0000	2.0000	45.0000	0.0000	5.0000
1	16.7460	-4.5106	21.7460	-8.7963	100	0.0000	2.0000	45.0000	5.0000	10.0000
1	13.4921	-8.3069	18.4921	-12.5926	100	0.0000	2.0000	45.0000	10.0000	15.0000

If you are tapering or subdividing a vertical fault, you can still see the nested or tiled patches by choosing **Functions > Grid > 3D view**. Then you can use the swivel tool to view it on its side. 3D view is also valuable because the patches are colored by their slip, rather than being translucent. Notice the rake vectors with tiny arrowheads; the vectors are rooted to the center of each patch.

#### 4.10 The seismic moment is calculated every time an input file is loaded

Every time you launch an input file, Coulomb calculates the total seismic moment of the sources in the input file, using the fault area, slip, Young’s modulus, E, and Poisson’s ratio, PR, from the input file. The seismic moment (in dyne-cm) and the equivalent  $M_w$  appears in the MATLAB window:

```
-----
User selected/Users/Toda/AFRC project IV/coulomb30/input_files/Example-1.inp
No lat. & lon. information is included in the input file.
Total seismic moment = 7.60e+26 dyne cm (Mw = 7.19)
---> To calculate deformation, select one of the submenus from 'Functions'.
```





For the seismic moment of individual sources, click on the source with the right mouse-click. You can also type “**seis\_moment**” into the Command Window at any time to see the total moment of all input sources.

#### 4.11 Using variable slip source models from the NEIC or university websites

Many large sources have “variable slip” (also called “finite fault”) models with numerous small patches of slip. You might also want to subdivide a receiver fault so that you can assess the variations in stress imparted by a nearby earthquake.

The NEIC now routinely publishes variable slip models of large global earthquakes in Coulomb .inp format. Go to the USGS NEIC Earthquake Event page, <<http://earthquake.usgs.gov/earthquakes>>, click ‘scientific & Technical,’ then “Finite Fault Model”:

**Scientific & Technical Information**

-  [USGS Centroid Moment Tensor Solution](#)
-  [USGS Body-Wave Moment Tensor Solution](#)
-  [USGS WPhase Moment Tensor Solution](#)
-  [Historic Moment Tensor Solutions](#)
- [Finite Fault Model](#)
- [Phase Data](#)
- [Theoretical P-Wave Travel Times](#)
- [Energy and Broadband Solution](#)

**Magnitude 7.0 - SOUTH ISLAND**

2010 September 03 16:35:46 UTC

Details
Summary
Maps
Scientific & Technical

**Slip Distribution**

- [SUBFAULT FORMAT](#)
- [CMTSOLUTION FORMAT](#)
- [COULOMB INPUT FORMAT](#)
- [GOOGLE KML FORMAT](#)

Prof. Chen Ji (U.C. Santa Barbara) also publishes variable slip models in Coulomb .inp format. Go to

[http://www.geol.ucsb.edu/faculty/ji/big\\_earthquakes/home.html](http://www.geol.ucsb.edu/faculty/ji/big_earthquakes/home.html)

Choose an earthquake and scroll down to the bottom of the explanatory page and you will see:

### Slip Distribution

[SUBFAULT FORMAT](#)

[COULOMB FORMAT](#)

[CMTSOLUTION FORMAT](#)

Prof. Martin Mai (King Abdullah Univ. of Science and Technology) has built the SRCMOD (source model) database of over 150 variable-slip input files from the literature, which can be read in as Coulomb input files. Some of these files can have hundreds to thousands of slip patches, and so calculations, particularly “3D view” and “calc. stress on faults”, can be very slow. Also, SRCMOD has not been updated since 2007, and the most recent earthquake was in 2005.

Go to <http://www.seismo.ethz.ch/static/srcmod/Homepage.html> and click on “Downloads”. Then download the most recent .mat file for MATLAB 7 (the top file below left) to the Coulomb33 folder. Make sure you “Save as” a binary “.mat” file, not a “.txt” file.

[SRCMOD\\_JUL07\\_v7.mat](#) (binary for MATLAB 7, with all source models, 2.9 MB)

[SRCMOD\\_JUL07\\_v6.mat](#) (binary for MATLAB 6, with all source models, 6.2 MB)

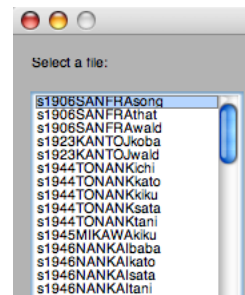
[References](#) (pdf-file with references to published source models)

[Zip-file containing all \\*SLP ascii-files](#) with simple slip-model representation (300 KB)

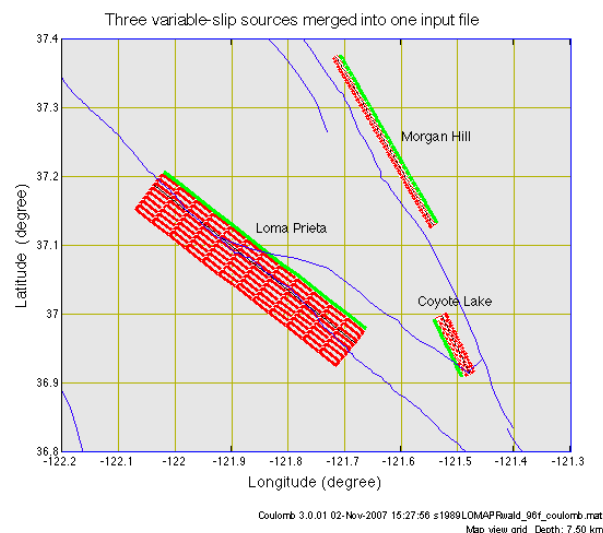
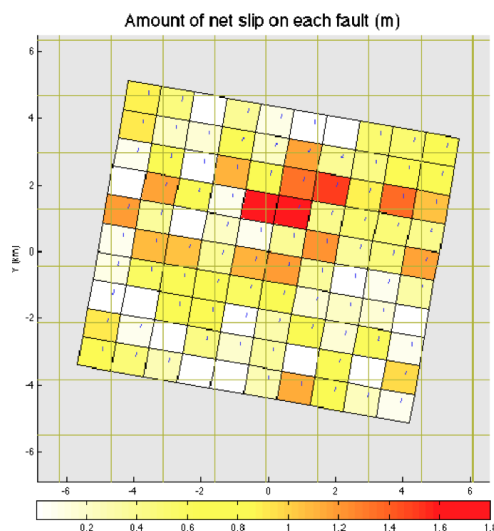
[Zip-file containing all \\*FSP ascii-files](#) with complete rupture-model description (1.3 MB)

[Zip-file containing all \\*PNG figures](#) (6.4 MB)

[Zip-file containing all \\*FIG files](#), usable for viewing and modification in MATLAB (4.6 MB)



In the MATLAB command window, type the plugin ‘**srcmod2coulomb**’. You will then see the file selection window (above right). The selected file will automatically be saved into the input file folder as an .mat input file. The file name will also indicate the number of sources (“100f\_” means 100 slip patches). Then, **Input > Open existing input file > Grid > 3D view**. The example below left is “1987WHITTIhart\_100f\_coulomb.mat”, the 1987  $M_w=6$  Whittier Narrows shock:



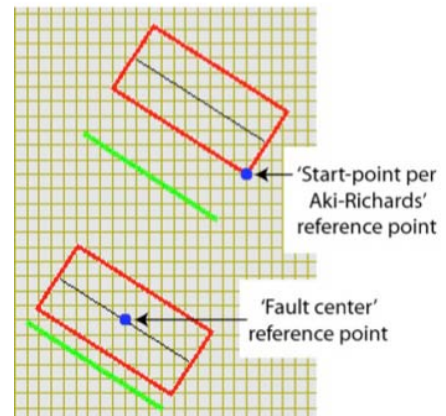
## 4.12 Merging several variable-slip models to one input file (“merge\_input\_files” plugin)

Here’s how to take many variable-slip input files and merge them into one .mat input file:

1. Open an existing input file. Type “**merge\_input\_files**” into the MATLAB command window. You are then requested to choose the second input file. This process is repeated until you have included all files that you want.
2. Save the combined file with any name you would like.

## 4.13 Making realistically scaled source faults from Global CMT or focal mechanism data

1. Choose **Input > Build input file from lon. & lat. map**. The “Build input from CMT or focal mech. data” calculator will appear. Button sequence: 1) - 2) - 3) - 4)



2. Press “1) Calc.” in the “study area” box (above left) to calculate boundaries and grid increments of the study area (the yellow fields). Then hit “2) Add to map” to apply changes to Coulomb window, which will create the grid. If you do not have the MATLAB Mapping Toolbox, and your grid spans more than one UTM zone, Coulomb will warn you that it is making simplified distance calculations.
3. To create the source fault from the CMT information, drop down to the “Fault element” box (above left). You can choose the “Fault center” (this is the geometrical center of the rectangle, so make sure the top of the fault is at or below the ground surface), or the ‘start-point per Aki-Richards’ (this is the Coulomb start-x, start-y position), and then input the  $M_w$ , strike, dip, and rake from a CMT file. In this example, just change  $M_w$  to 6.8 and change the dip to  $20^\circ$ .

4. If you would like to use the Wells and Coppersmith (BSSA, 1994) empirical magnitude-area relations to estimate appropriate fault lengths and widths, press the “From empirical relations” button, and the “empirical relations...” box will appear (above right). Choose the type of fault (here, reverse) and hit “Calc.” To accept the length and width values, hit the “Apply” button, and then close the “empirical relations” window. You will now see the “length” and “width” information changed in the “Fault elements” box. Notice, however, that these relations permit the fault width in great strike-slip events to get too deep.
5. Now press “3) Calc.” in the “Fault element” window to calculate fault position, and press “4) Add to map” to apply the fault to the Coulomb window. A portion of the resulting map is shown above at right. Notice that the blue dot is the fault reference point you selected. To save the input file you just created, choose “save input file as ascii” in the Input menu, and name it, replacing the comment lines.
6. If you would like to add more sources, after you have hit “4) Add to Map”, just increment the “ID number” to 2 and put in the new values into the “Fault elements” window, and so forth.

## Chapter 5

## Earthquake, Fault, Coastline Overlays, and Seismicity Rate Changes

### 5.1 Overlays (coastlines, active fault traces, seismicity)

1. It is enormously valuable to plot your map with lat/lon tic marks and to overlay geographic or seismic catalog information. This is easy to do as long as the input file (.inp, .inr, or .mat) has lat/lon information, which is the last item in the input file, such as

```

Map information
1 ----- min. lon = -123.0000
2 ----- max. lon = -121.0000
3 ----- zero lon = -122.0000
4 ----- min. lat = 36.0000
5 ----- max. lat = 38.0000
6 ----- zero lat = 37.0000

```

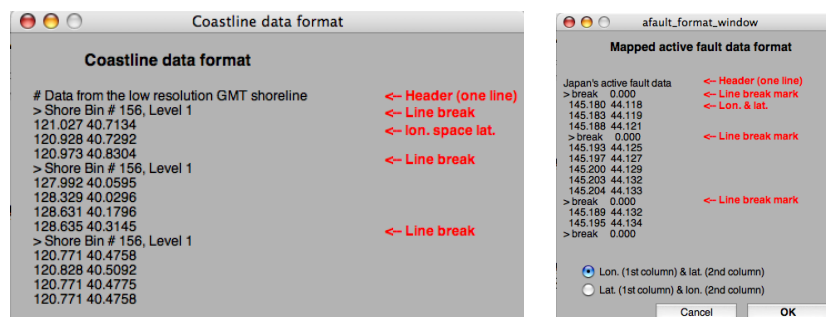
To plot with lat/lon tic marks, **Input > Preferences > Coordinates > lon. & lat.** and then launch the input file. (If you do not have this information, you can calculate it using the Coulomb tools: **Functions > Tools > Convert lat/lon to Cartesian**, which opens a calculator window that will create your input file for you.)

2. **Use of the National Geophysical Data Center Coastline Extractor.** Go to [http://www.ngdc.noaa.gov/mgg\\_coastline/](http://www.ngdc.noaa.gov/mgg_coastline/) and input the boundary coordinates, or use “Java Map for lat/lon”, zooming in as needed. We recommend the Medium Resolution (1:70,000) Coastline database. Select the MATLAB Format, choose no compression, and preview it with a GMT plot. Hit the “SUBMIT” button. Save the resulting “.dat” file in the Coulomb “coastline\_data” folder, and rename it if you like. Open the file in your editor; if there are “nan” lines in the file, use a “replace” command in your editor to change to “>” symbols.

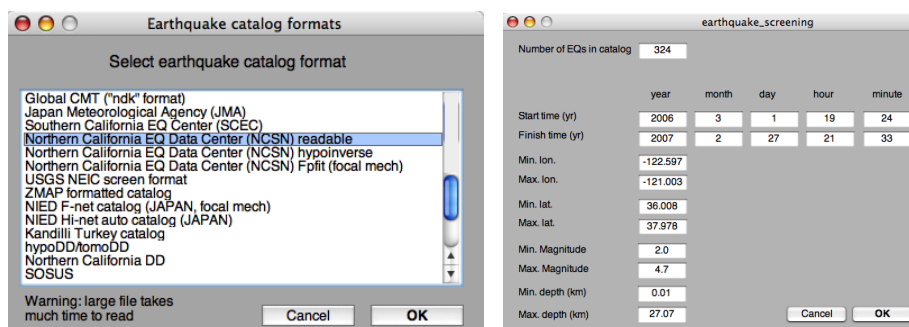
### 5.2 How to use overlays in 2D and 3D plots

1. Launch “Example-SFBayArea.inp”. Now, **Overlay > Coastlines**. Open the “coastline data” folder in the Coulomb33 folder, and select “california\_coastline\_di\_pos.dat”. The “di” refers to intermediate resolution; there is also a high resolution “dh” file in the folder. Answer the pop-up question, “no”. Some datasets treat western longitudes as negative; others do not. The coastline will appear on your plot. Now try **Overlay > Active faults**. (You could load folds or roads or anything you like; the formats are explained in a pop-up window.) Choose “California faults\_lonlat\_dat”. It’s a large file but will plot on your map. The “Coastline data format” and “active fault format” windows are shown below:



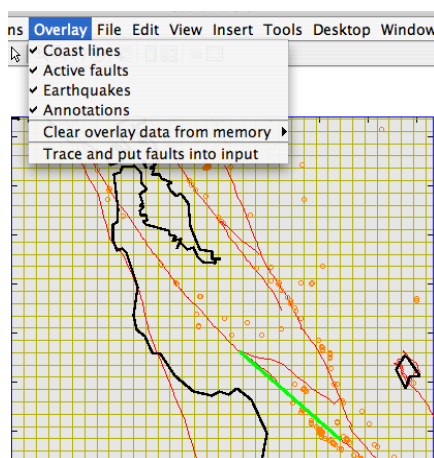


- Now choose **Overlay > Earthquakes**, and choose the “(NCSN) readable” format in the “Earthquake catalog formats” menu below left. Then select the “readable” format of the actual data file in the data folder. It is only important that the format chosen matches the format of the dataset you are opening. Fifteen catalog formats are supported by Coulomb from global data, the United States, Japan, and Turkey.



An “earthquake\_screening” window (shown above right) will appear that lets you filter the time, location, depth, and magnitude of earthquakes you would like to plot. If it is a large catalog, this can take time. For the CMT “ndk” format, go to <http://www.globalcmt.org/cmtfiles.html>.

- For this exercise, just click “OK” to plot all 324 earthquakes that occurred in the grid and are defined in the input file, and you should see the image below. The default colors appear below, but the colors of all overlays can be changed in the Preferences panel.



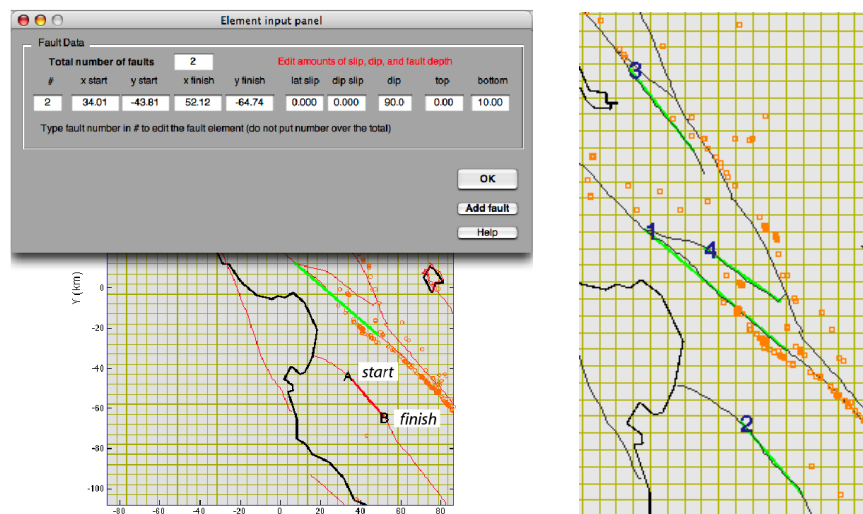
You can remove any overlay by **Overlay > Clear overlay from memory**, if you want to use a different dataset instead, or you can toggle on/off any overlay by unchecking it. Note that coastlines are continuous lines; by editing them in Adobe Illustrator, you can fill the land or sea area. Faults are line segments.

4. Save an input file with all of the overlays by **Input > Save Input + Overlays as .mat**. Name it uniquely. This will create a compact binary file that you can use in the future—a great time savings—although it cannot be opened in an editor.

### 5.3 Adding source or receiver faults by tracing active faults (or folds)



It is fast and easy to build source or receiver faults by tracing the active faults on the map. Starting from where you left off in the previous exercise, **Overlay > Trace and put faults into input**. Instructions pop up to remind you that you use your left mouse button for the **Start** end of the fault and your right mouse button for the **Finish** end. **Remember that the right-hand rule means that for non-vertical sources, the Start-Finish order determines which direction the fault dips: the fault dips to the right when you are looking toward the Finish from the Start** (see the Aki-Richards (1980) diagram in the “Keys to the City”).

The “Element input panel” appears (below) with the Start-Finish coordinates you moused on the map. Now, add the slip and top/bottom depth and hit “OK”. Remember that if the fault is blind, it will be offset from the trace as a function of its dip and upper depth (refer to the “Map Positioning” figure in Chapter 4 to see this). The new fault appears in red (below left); when you hit OK, it turns green to indicate it is now the trace of a source or receiver. If you save the input file, the new source or receivers will be included. When saved, each source will get assigned its element number, which will be seen at the Start end (below right).

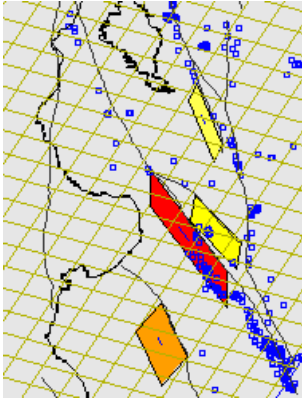


### 5.4 3D source and seismicity (.fig) figures that you can spin and roll

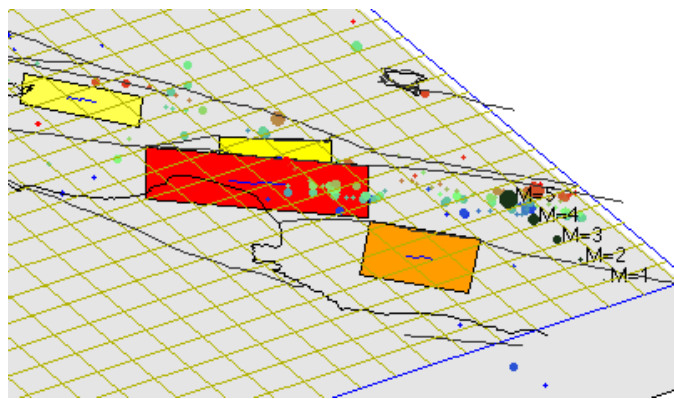
MATLAB lets you create very compact “.fig” files that can be manipulated in 3D to see, for example, if your coseismic source fault is properly located with respect to its aftershocks.

1. **Input > Preferences > Cartesian**. Open an input file, add the coastline and earthquake catalog overlays. Now, **Functions > Grid > 3D view** (see below left).
2. Switch to the MATLAB command window, and type the plug-in, “**earthquake\_plot3**”. You will be asked on screen if you would like the earthquake magnitude scaled by circle size and depth scaled by color (choose Y) or by circles or filled disks (choose N).
3. You can use the  tool to blow up the area of interest, but the file will still contain the full data. Now use the  to spin and roll the view. A portion is shown below, at right. With this tool selected, a right mouse-click lets you to reset to a regular map, side, or depth view. The source slip is scaled by its color.
4. You can save this file and re-open it later. **File > Save as > “yourname.fig.”** It’s an amazingly small file.
5. If you simply double-click on this figure, it opens in MATLAB (not Coulomb) and can again be manipulated.

**3D view in Grid**  
(using swivel tool)



**3D view using “earthquake\_plot3” plugin**  
(different view, quakes scaled by size and depth)

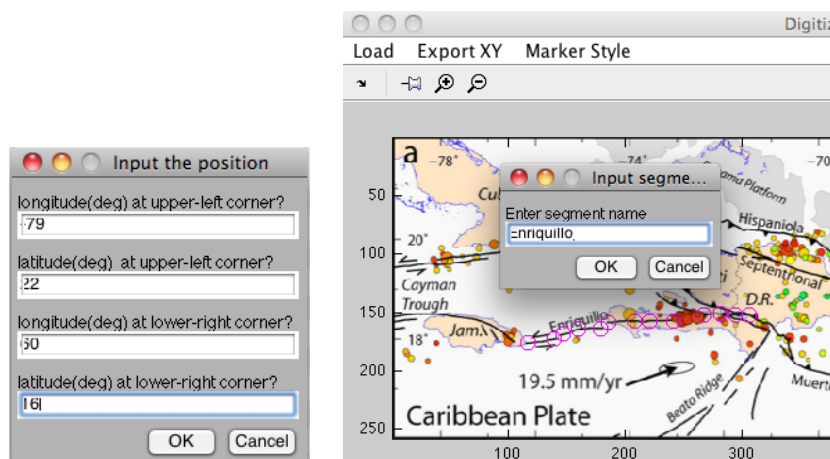


## 5.5 Volcano overlays

Active volcanoes appear as triangles if you choose **Overlay > volcanoes**. Their size and color are controlled in the Preferences menu. An example from Japan is shown in Chapter 2.2. Global volcanoes are stored in “volcanoes\_NGDC\_NOAA.mat” in the plug\_ins folder; you do not need to load them in. If, when you select volcanoes, none appear, then there are not any in your grid area.

## 5.6 Digitizing faults from maps and images

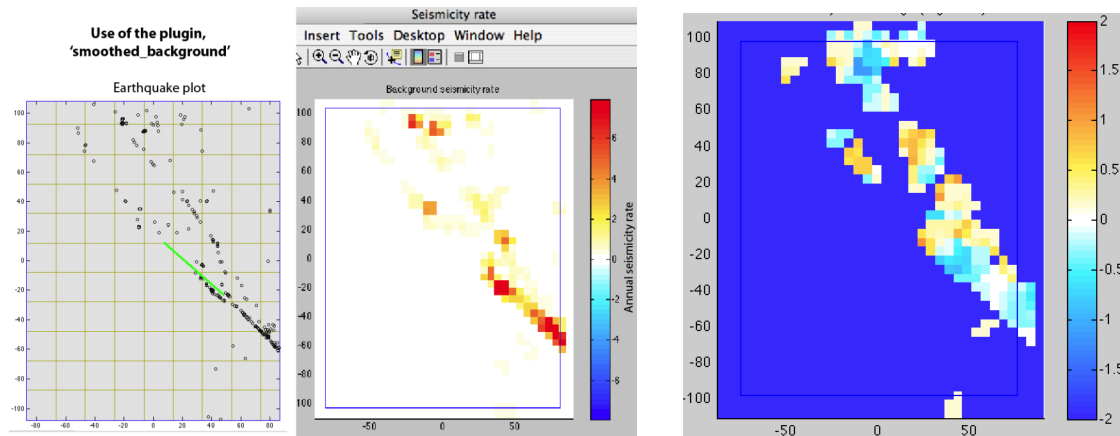
Save the fault map you would like to digitize as a .jpg or .png (raster) file, cropping it so the boundaries of the image lie at identified lat/lon coordinates. Type “**digitize\_faults**” in the MATLAB Command Window, and browse to your image, enter its upper left and lower right coordinates in the pop-up panel (below left). Then, click on the push-pin icon and use the left mouse button to digitize a fault, ending with the right mouse button. Each time you click the right mouse button you will be asked to name the fault or fault section. Then choose “Export XY” and save it as a .dat file into the active\_fault\_data folder in the Coulomb33 folder.



The vertical 50-250 scale and horizontal 0-300 scale numbers seen at left are simply the raster image pixel numbers; they are not kilometers. You can use the zoom tool while digitizing. Here we chose large magenta circles as the digitizing bread crumbs; they can be changed in the Marker Style menu.

## 5.7 Making smoothed seismicity density plots

Rather than showing earthquakes, you might want to plot seismicity density smoothed over some radius. This can be accomplished by plotting an earthquake catalog in a 2D Grid view, and then typing in the plugin, “**smoothed\_background**”. You choose a smoothing radius, and it will plot the seismicity density over a box reduced in size to the original so that the smoothing kernel can use all cells, as shown below.



## 5.8 Making smoothed seismicity rate change plots

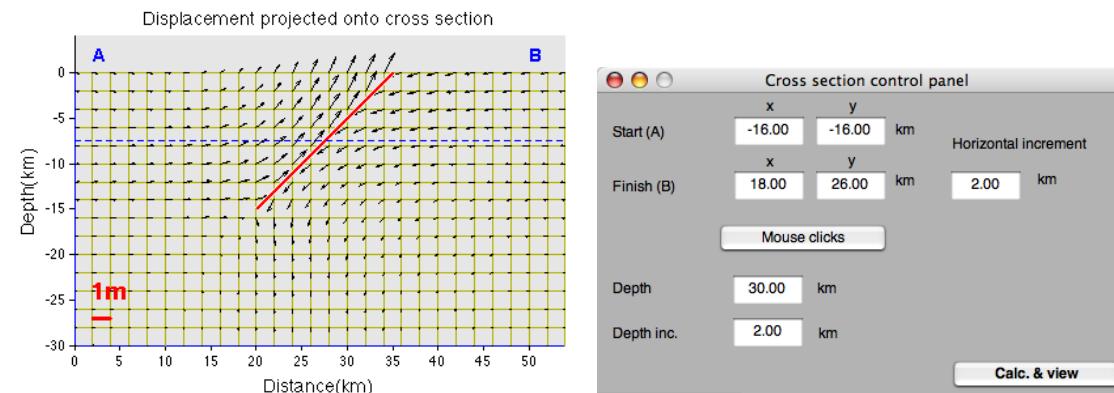
This plug-in allows you to plot the seismicity rate change associated with an earthquake or volcanic event. Just type “**seis\_rate\_change**” into the Command Window. This allows you to read in a seismic catalog, choose the minimum magnitude (for example,  $M_c$ ), select a smoothing radius, identify the date and time of the event (for example, a large earthquake in the catalog), choose a color saturation value, and then calculate the rate change, which is scaled by  $\log[\text{new rate}/\text{old rate}]$ . Two maps are produced, one to show the seismicity rate where it is defined (above right; the dark blue areas are undefined because there are not a sufficient number of earthquakes), and the other to show the undefined areas. Earthquakes can be overlaid on the log seismicity rate change map.

## 5.9 Transferring Coulomb files to the GMT mapping software

There are two plug-ins used to convert the vector-based source and receiver fault information, and the raster-based Coulomb stress gradient map, into GMT. After you have created the map view figure in Coulomb, type this into the Command Window: **coulomb2gmt\_source**. It saves the files, “gmt\_fault\_calc\_depth.data”, “gmt\_fault\_map\_proj.data” and “gmt\_fault\_surface.data”. Then type this into the Command Window: **coulomb2gmt\_cout**. This converts the calculated Coulomb matrix data into the GMT text column data (lon, lat, Coulomb stress change), so that it can be plotted in GMT and draped over a DEM as a raster image. It saves a file named “coulomb\_out.dat”



- To make a displacement cross-section, choose **Input > Open existing input file > “Example-2(TH).inp.”** Next, **Functions > Displacements > Horizontal displ (vectors)**. In the “Displacement” control panel, choose “Cross section”. This is a reverse fault; the dashed blue line in the plot below is the depth of the horizontal vectors in the map view plot. The cross-section line was included in the input file (this optional information is shown above right). You can change the cross-section line interactively in the *Cross section control panel*. Change the increments to 2 km by 2 km (below left). Use the left mouse button to click the start (A) point, and the right mouse button to click the end (B) point. If you do not have a two-button mouse, use ctrl+click for the right button. To save the changes, choose **Input > Save input file as ascii** with a new file name.



For displacement plots, the dip of the cross section is always vertical. Within the “Cross section control panel”, you can choose items on the menu bars to **Zoom In**, **Zoom Out**, **Pan**, and **3D Rotate**.

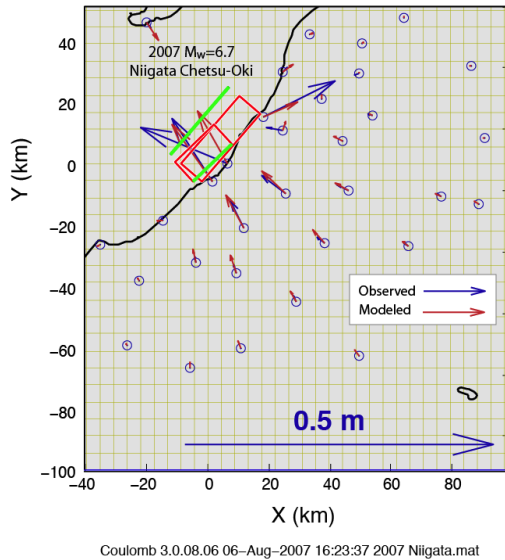
## 6.2 To display observed and modelled GPS vectors

- You can create a GPS file with five columns: lon.°, lat.°, dx, dy, dz (m), in space-delimited format. If easier, prepare the file in Excel and then save as “Formatted text (space delimited)”. An example of the format is shown below. Also, see “gps\_example.dat” in the GPS\_data folder.

Lon.	Lat.	Easting(m)	Northing(m)	Upwarding(m)
138.5744	37.3977	-.14310	0.0597	0.000
138.5164	37.3485	-.06670	0.1019	0.000
138.7069	37.5358	.11680	0.0597	0.000
138.7900	37.3113	-0.0404	0.0301	0.000
138.7805	37.6675	0.0054	0.0073	0.000

- After you have plotted a figure, choose **Overlay > GPS stations**, and select the file you created. If you did not set “Depth” in the input file to zero, choose **Functions > Change Parameters > Calculation depth**. If the input file has a source fault, you will see a plot like the one below for the observed and modelled vectors (the circles mark the stations; they are not error ellipses) and a vector scale bar. Here we saved the file as a pdf and added the legend in Illustrator.
- To output a numerical file of the observed and modelled displacements, follow the instructions in the Command Window (reproduced below). The GPS\_DATA file can be opened in Excel for calculation of residuals. The example below uses the input “Niigata-Chuetsuoki-2007.mat” and “Niigata-Chuetsuoki-2007-GPS.dat”.



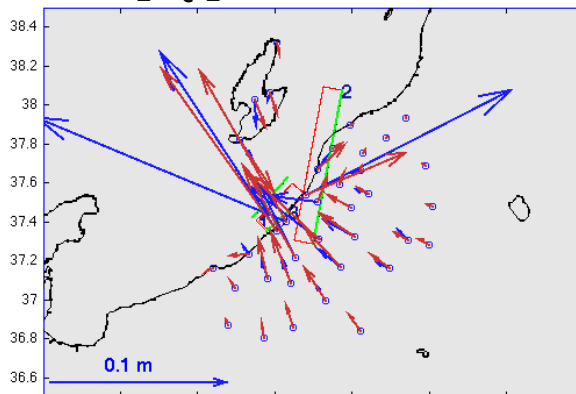


```
----- GPS data -----
User selected/Users/ross/Desktop/coulomb30/GPS_data/niigata2007.dat
GPS_output.csv is saved in /Users/ross/Desktop/coulomb30/output_files

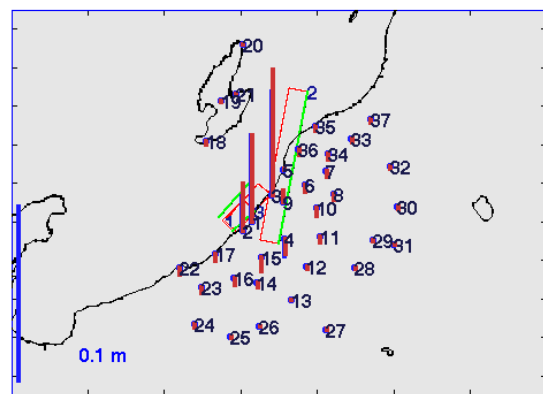
* To save the GPS data as binary, use the following command
* in the Command Window.
* save filename GPS_DATA (e.g., save mygps.mat GPS_DATA)
* To read the .mat formatted GPS data, use 'File -> Open...' menu later.
```

- To plot the vertical GPS vectors, type **GPS\_FLAG = 'vertical'** into the Command Window. If you would also like stations labelled by their sequence number, type **GPS\_SEQN\_FLAG = 'on'**. You will then see a plot like the one below right. Observed displacements are blue; if you are running a model, its predictions will be red.

**Default**  
**Command window entries:**  
(GPS\_FLAG = "horizontal")  
and GPS\_SEQN\_FLAG = "on"



**setting**  
GPS\_FLAG = "vertical"



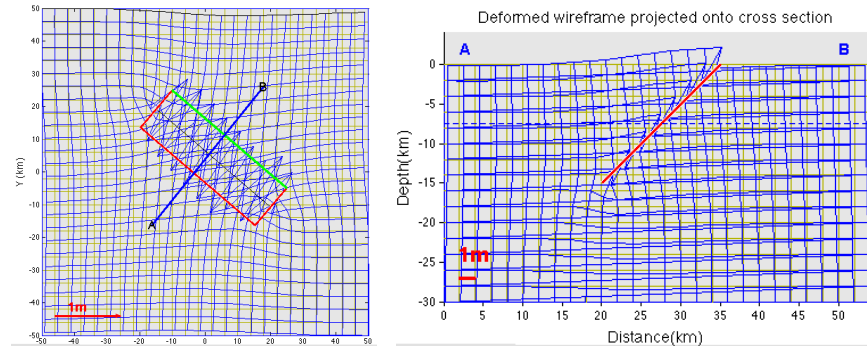
### 6.3 To display crustal deformation as wireframe images

- Using Example-2(TH).inp, Choose **Functions > Displacements > Horizontal displ. (wireframe)**. The undistorted grid is in yellow and the distorted grid in blue. For a cross-section, use the default cross-section line, but change the horizontal and depth increments to 2 km in the "Cross section" control panel to see the images below. These cross-sections can be made to conserve area (they are "retrodeformable" in geological jargon) if you set Poisson's ratio to 0.5 by **Functions > Change Parameters > All input parameters**:

Half space parameters

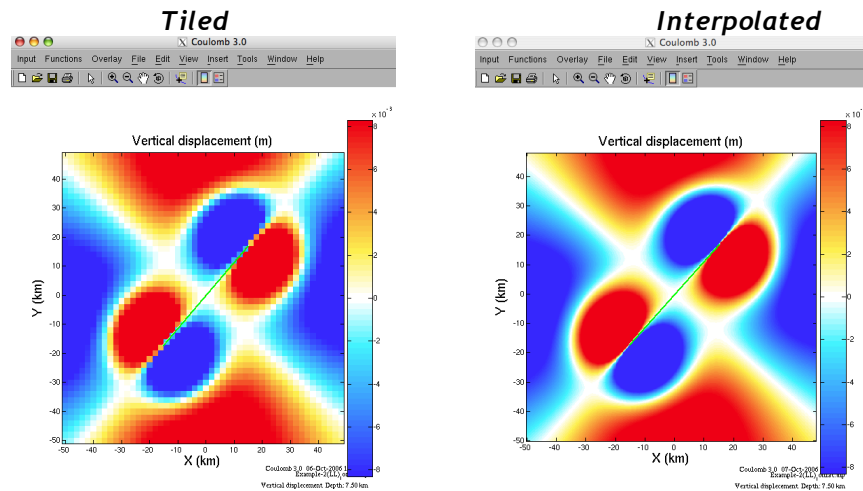
Poisson's ratio	0.50
Young modulus	800000.0 bar

- The wireframe cross-sections are useful to illustrate deformed strata associated with thrust and normal faults and ramp-thrusts. You can pop them into Illustrator and color the layering so it appears like strata.



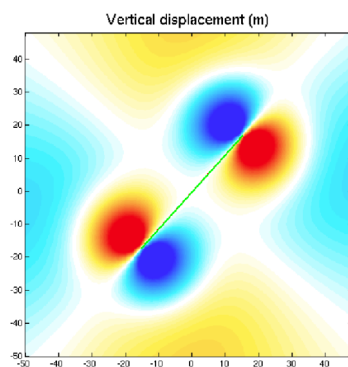
## 6.4 To display the vertical displacement by color gradients and contours

- Choose **Input > Open an existing file** “Example-2(LL).inp”; then **Functions > Displacements > Vertical displ. (color & contours)**. You will see the following left image in the Coulomb 3.3 window.

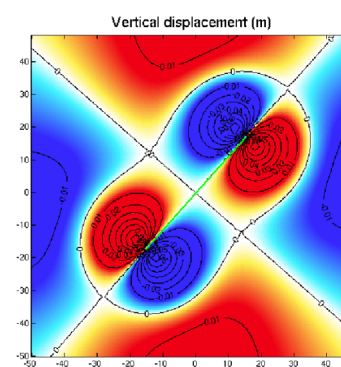


- Data smoothing and color scale options: In the “Vertical displ.” control panel, you can choose un-interpolated data (left above) or “Interp.”, that is, interpolated (right above). Color saturation: You can adjust color scale by moving the slider bar under “Color saturation” or type the value in the box, hit return, and then click “Calc. & View” in the Displacement control panel (below left).

**Under-Saturated**



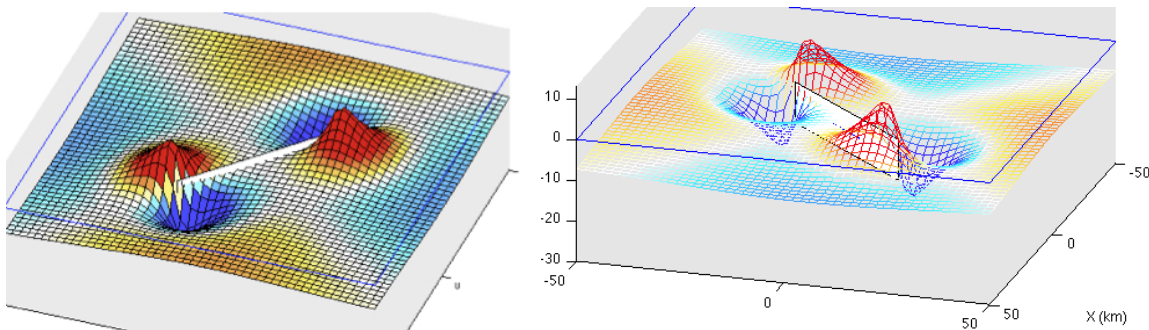
**Contoured**



3. Contours: In the “Displacement” control panel, choose “Contours” and click “Calc. & View”. Contours showing vertical displacements are superimposed on the color image (image above right). You can choose the contour interval. To get smooth contours, you must use a fine grid, because there is no interpolation of the contours..
4. Cross section: Choose “Cross section” in the “Displacement” control panel. The methods of making cross sections are similar to those described in previous sections.

## 6.5 To display the vertical displacement as a 3D image drape

1. Choose **Functions > Displacements > 3D image drape**. The color scale is controlled by the parameter in your input file. See the lower left panel below.
2. To control the amount of vertical exaggeration, choose **Functions > Change parameters > Displ. exaggeration**, and you will see a pop-up “Displ. exaggeration” window, in which you can change vertical exaggeration by entering a new value and then clicking “OK”.



3. In the Coulomb 3.3 window, you can use options of **Zoom In**, **Zoom Out**, **Pan**, **3D Rotate**, **Insert/Remove ColorBar**, and **Insert/Remove Legend**, as described in previous sections.

## 6.6 To display the vertical displacement as 3D image wireframed surface

1. Choose **Functions > Displacements > 3D image wireframed surface**. The color scale is controlled by the parameter in your input file.
2. Try changing the vertical exaggeration by **Functions > Change parameters > Vertical exaggeration > 8000**. Then, choose **Functions > Displacements > 3D image wireframed surface**. A swivelled version is shown above right.

## 6.7 To display and output the horizontal and vertical surface deformation in cross-section

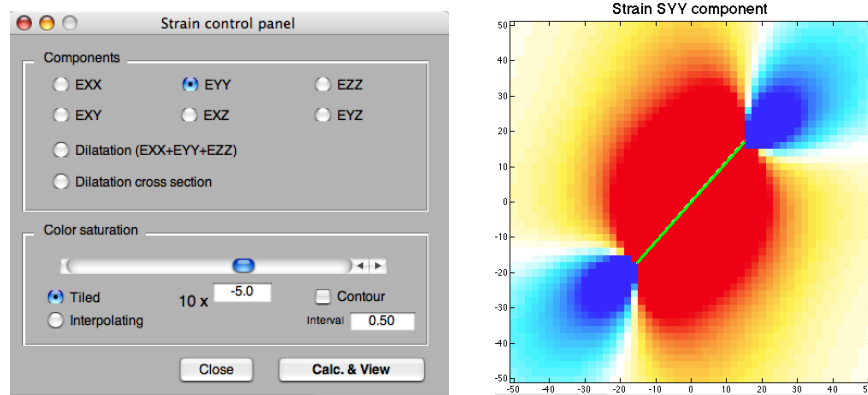
Both “Horizontal Displ. (vectors)” and “Horizontal displ. (wireframe)” provide cross-section outputs. These also produce numerical output files of the ground surface deformation components,  $U_x$ ,  $U_y$ , and  $U_z$ . You will see these lines in the Command Window:

```
User selected /Users/rstein/Desktop/Coulomb33/input_files/Example-2(TH).inp
No lat. & lon. information is included in the input file.
Total seismic moment = 6.26e+26 dyne cm (Mw = 7.13)
--> To calculate deformation, select one of the submenus from "Functions".
```

```
Displacement.cou is saved in /Users/rstein/Desktop/Coulomb33/output_files
displacement_section.cou is saved in /Users/rstein/Desktop/Coulomb33/output_files
```

## 6.8 To display any component of the strain field

1. Choose **Functions > Strain**. A Strain control panel will appear (below left).



2. In the Strain control panel, choose the type of strain you want to calculate. For example, choose “Eyy” and you will see the image above right. We are not using the “Engineering Strain” convention, where values are multiplied by 2.
3. Numerical output files. Every time you click “Calc. & View” in the “Strain” control panel, an output file called “dilatation\_section.cou” will be created or updated. When you want to save your latest runs, remember to rename the “dilatation\_section.cou” file within the “output files” sub-folder; otherwise it will be written over by your future displacement calculations. Here is an example of “dilatation\_section.cou” output file:

dilatation_section.cou					
Input file selected: Example-2(LL)_lonlat.inp					
x (km)	y (km)	z (km)	dilatation(ex+ey+ez) (-)	dilatation (-)	dilatation  (-)
-36.0000000000000000	36.0000000000000000	-0.0000000000000000	0.0000001666026758	0.0000001666026758	0.0000001666026758
-36.0000000000000000	36.0000000000000000	1.0000000000000000	0.0000001641860500	0.0000001641860500	0.0000001641860500
-36.0000000000000000	36.0000000000000000	2.0000000000000000	0.0000001616694448	0.0000001616694448	0.0000001616694448
-36.0000000000000000	36.0000000000000000	3.0000000000000000	0.0000001590625171	0.0000001590625171	0.0000001590625171

4. By choosing parameters in the the “Strain” control panel, you have the options to switch between the tiled versus interpolated data grid, change color saturation, and contours, as explained in previous sections.

## Chapter 7

## Coulomb Stress Calculations

### 7.1 The Coulomb failure hypothesis explained

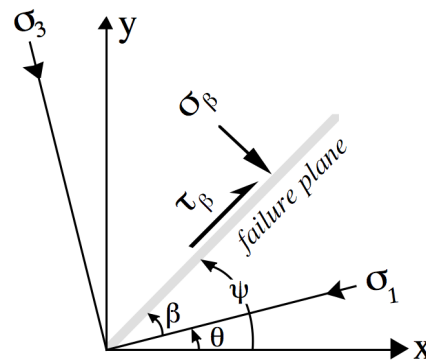
Here we calculate static stress changes caused by the displacement of a fault or dike or point source (we refer to these as "source faults"). The displacements in the elastic halfspace are used to calculate the 3D strain field; this is multiplied by the elastic stiffness to derive the stress changes.

We resolve the shear and normal (clamping/unclamping) components of the stress change on a 3D grid of points or on specified "receiver" fault planes. Receiver faults are planes with a specified strike, dip, and rake, on which the stresses imparted by the source faults are resolved; we call these "specified faults" in the Coulomb menus. The shear stress increase or decrease is dependent on the position, geometry, and slip of the source fault and on the position and geometry of the receiver fault, including its rake. The normal stress change (clamping or unclamping) is independent of the receiver fault rake.

We use the Coulomb failure criterion,  $\Delta\sigma_f = \Delta\tau_s + \mu' \Delta\sigma_n$ , in which failure is hypothesized to be promoted when the Coulomb stress change is positive. Here,  $\Delta\sigma_f$  is the change in failure stress on the receiver fault caused by slip on the source fault(s),  $\Delta\tau_s$  is the change in shear stress (reckoned positive when sheared in the direction of fault slip),  $\Delta\sigma_n$  is change in normal stress (positive if the fault is unclamped), and  $\mu'$  is the effective coefficient of friction on the fault.

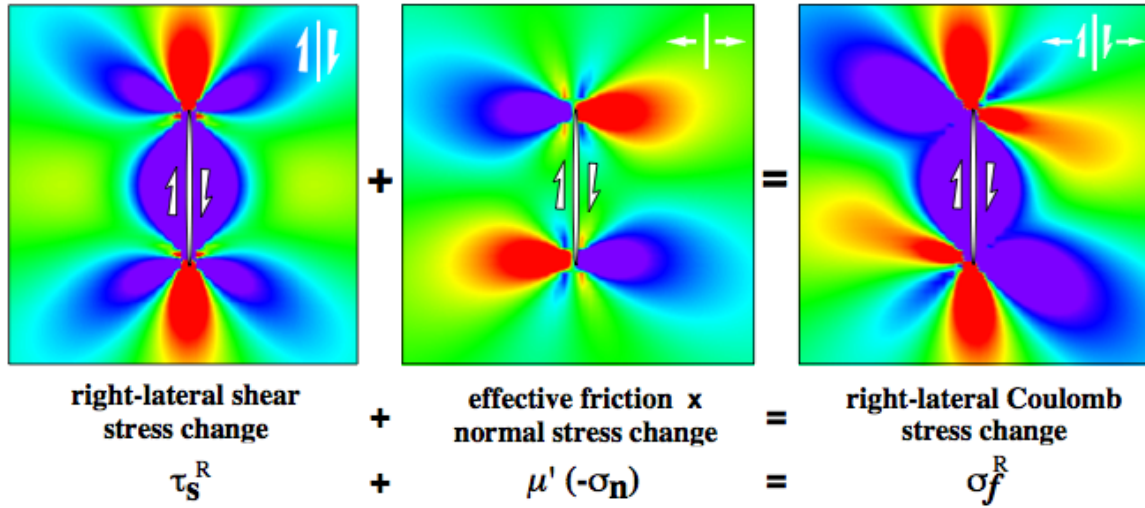
In Coulomb, we'll explore four kinds of receiver faults: (1) "specified" receiver faults in which all faults have a uniform receiver fault geometry, (2) faults optimally oriented for failure, (3) receiver faults with geometry set in the input file, and (4) focal mechanism files, in which there are always two orthogonal fault planes. The optimal orientations are a function of the regional (also called "tectonic") stress, the stress imparted by the source fault, and the assumed friction coefficient on the receiver fault.

On the following page are figures 2 and 3 from King and others (1994), which graphically present the Coulomb stress change resolved on vertical strike-slip faults parallel to the source fault (fig. 2A) and resolved on optimally oriented planes (fig. 2B) for a given regional uniaxial compression and an assumed friction coefficient. In figure 3, the influence of the regional stress magnitude is seen on the orientation of the optimal planes and on the stress change resolved on these planes. These figures were made in a primordial version of Coulomb.

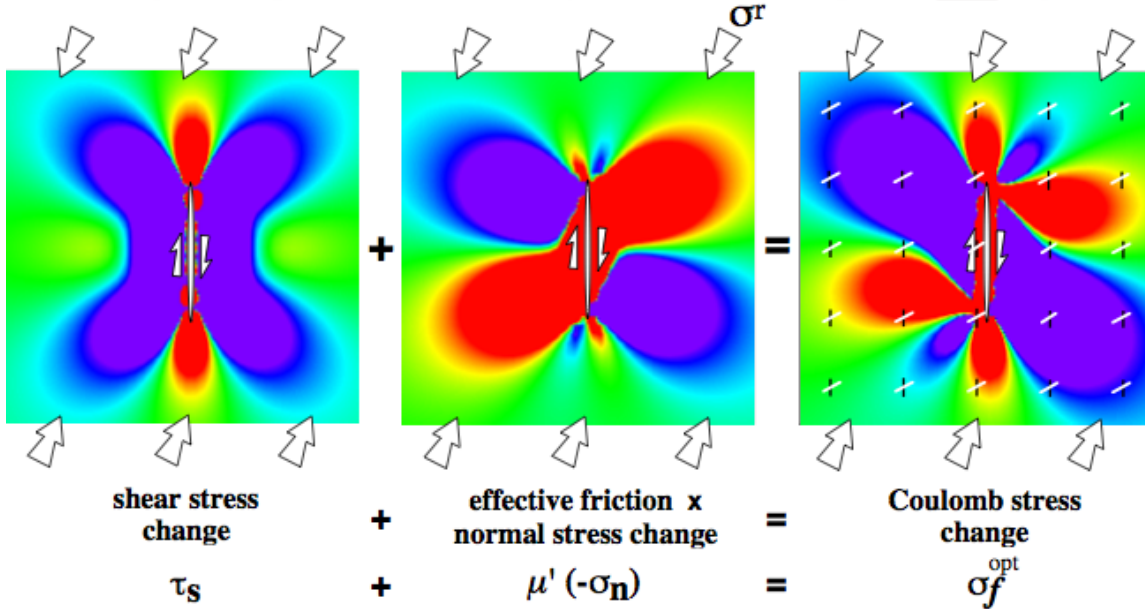


Above, just notice that the fault or "failure plane" is oriented  $\beta^\circ$  from the principal compressive stress ( $\sigma_1$ ), and the shear stress  $\tau$  and normal stress  $\sigma$  act on the fault.

### A. Coulomb stress change for *right-lateral faults parallel to master fault*

Stress ■ Rise ■ Drop


### B. Coulomb stress change for *faults optimally oriented for failure* N27°E regional compression ( $\sigma^r$ ) of 100 bars; $\mu' = 0.75$

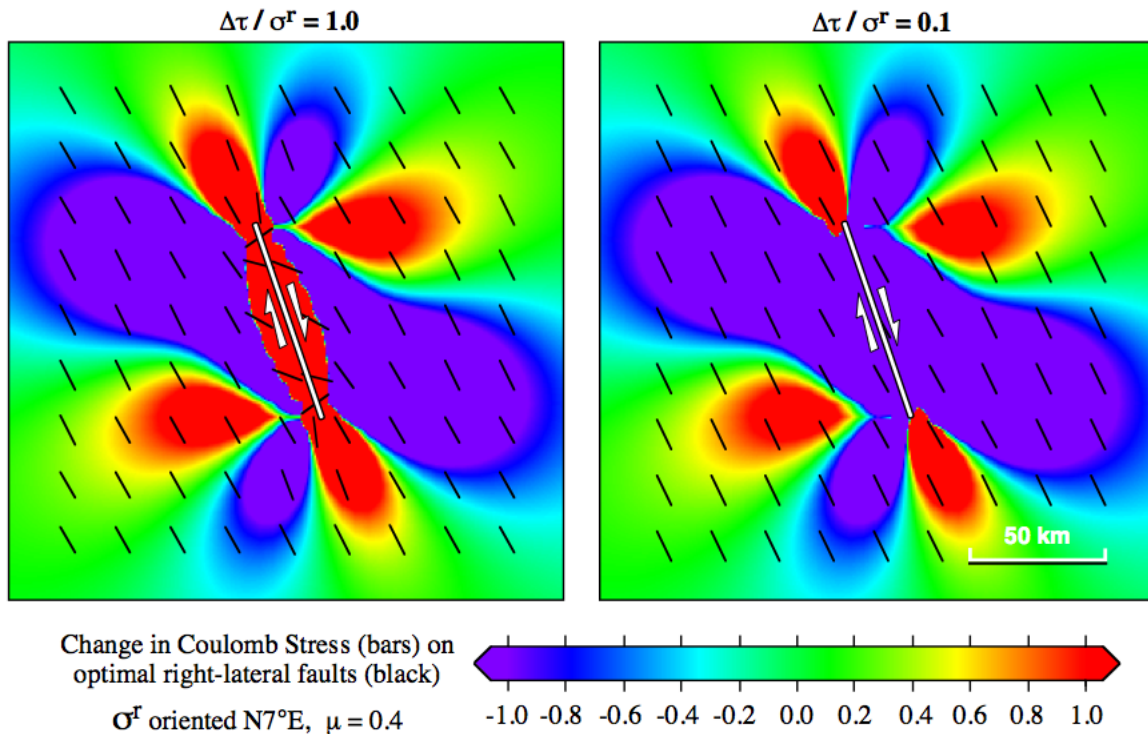
Optimum Slip Planes X left-lateral X right-lateral


**Illustration of the Coulomb stress change** (fig. 2 from King and others, 1994) above. The panels show a map view of a vertical strike-slip fault embedded in an elastic halfspace, with imposed slip that tapers toward the fault ends. Stress changes are depicted by graded colors; green represents no change in stress. (A) Graphical presentation of equation 8 of King and others (1994), a "specified fault" calculation. (B) Graphical presentation of equation 13 of King and others (1994), for optimally oriented strike-slip ("opt strike-slip") faults.

**Dependence of the Coulomb stress change on the regional stress magnitude,  $\sigma^r$ , for a given earthquake stress drop,  $\Delta\tau$**  (fig. 3 from King and others, 1994). If the earthquake relieves all of the regional stress (left panel), resulting optimum slip planes rotate near the fault. If the regional deviatoric stress is much larger than the earthquake stress drop (right panel), the orientations of the optimum slip



planes are more limited, and regions of increased Coulomb stress diminish in size and become more isolated from the source fault. In this and subsequent plots, the maximum and minimum stress changes exceed the plotted color bar range (in other words, the scale is saturated).

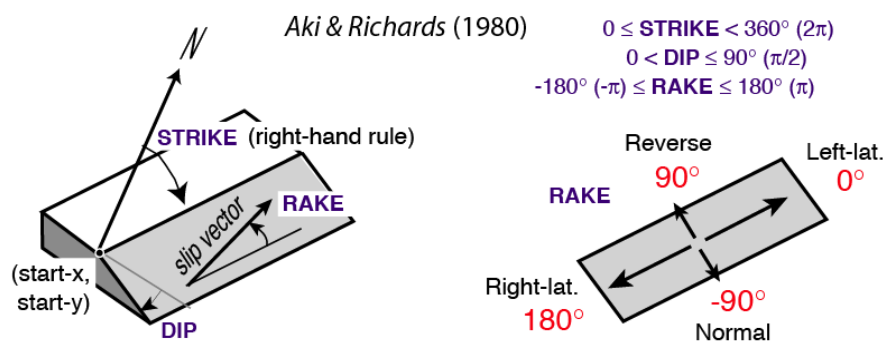


## 7.2 Coulomb stress change on specified receiver faults ("specified faults")

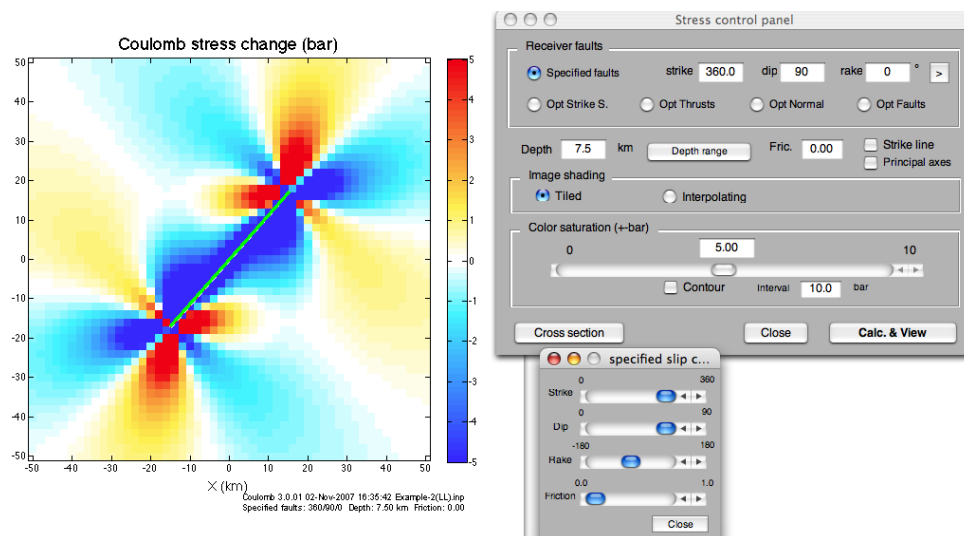
This is the simplest calculation, and is widely used by researchers. To resolve the stress, you need to specify the fault strike, dip, and rake of the receiver planes following the Aki and Richards convention, shown graphically in the next page of this manual.

1. Choose **Input > Open existing input file**. Then in the "Open input file" window, choose the "input\_files" sub-folder within the "Coulomb 33" folder, and select "Example-2(LL).inp"
2. Choose **Functions > Stress > Coulomb stress change**. The "Stress" control panel appears.
3. To calculate stress changes on specified receiver fault planes, use the default "specified faults". Coulomb averages the information on all input fault patches listed in the input file and puts the values in the boxes, but you can change them. Strike, dip, and rake are defined following the conventions of Aki and Richards (1980):

### Convention for resolving stress and for focal mechanisms



For practice, choose a strike/dip/rake of  $360^\circ/90^\circ/0^\circ$ , change the friction coefficient to 0.0, set the stress-change color saturation to  $\pm 5$  bars, and hit “Calc. & View”.



The Coulomb stress changes default using our “Anatolia” color scheme. Other schemes (“Rainbow” or “Black & White”) can be changed by pulling down the **Input > Preferences** menu bar and clicking on “Color Map”. Then re-run the input file.

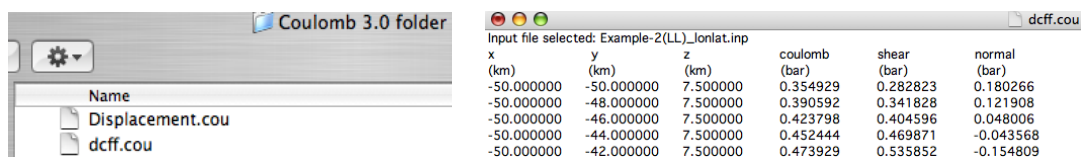
### 7.3 Using the strike/dip/rake/friction slider (Specified slip control panel)

To vary these parameters on the fly, hit the “>” button in the Stress control panel, and the “Specified slip” control panel pops up (see it above). Slide the balls to explore how the stress pattern changes.

### 7.4 Saving the graphic and numerical output of stress calculations

To save this graphic, **File > Save As...** > choose a **.eps** (if it has a color gradient map) or **.pdf** if it does not, format and rename it; its only 40 kb but is a full vector image. Stress change is calculated in the lower left corner of each grid square at the target depth specified in the input file. Calculated values of stress change may saturate (exceed the plotted range), so experiment with the slider to see more subtle features. The stress-scale legend is to the right of the plot.

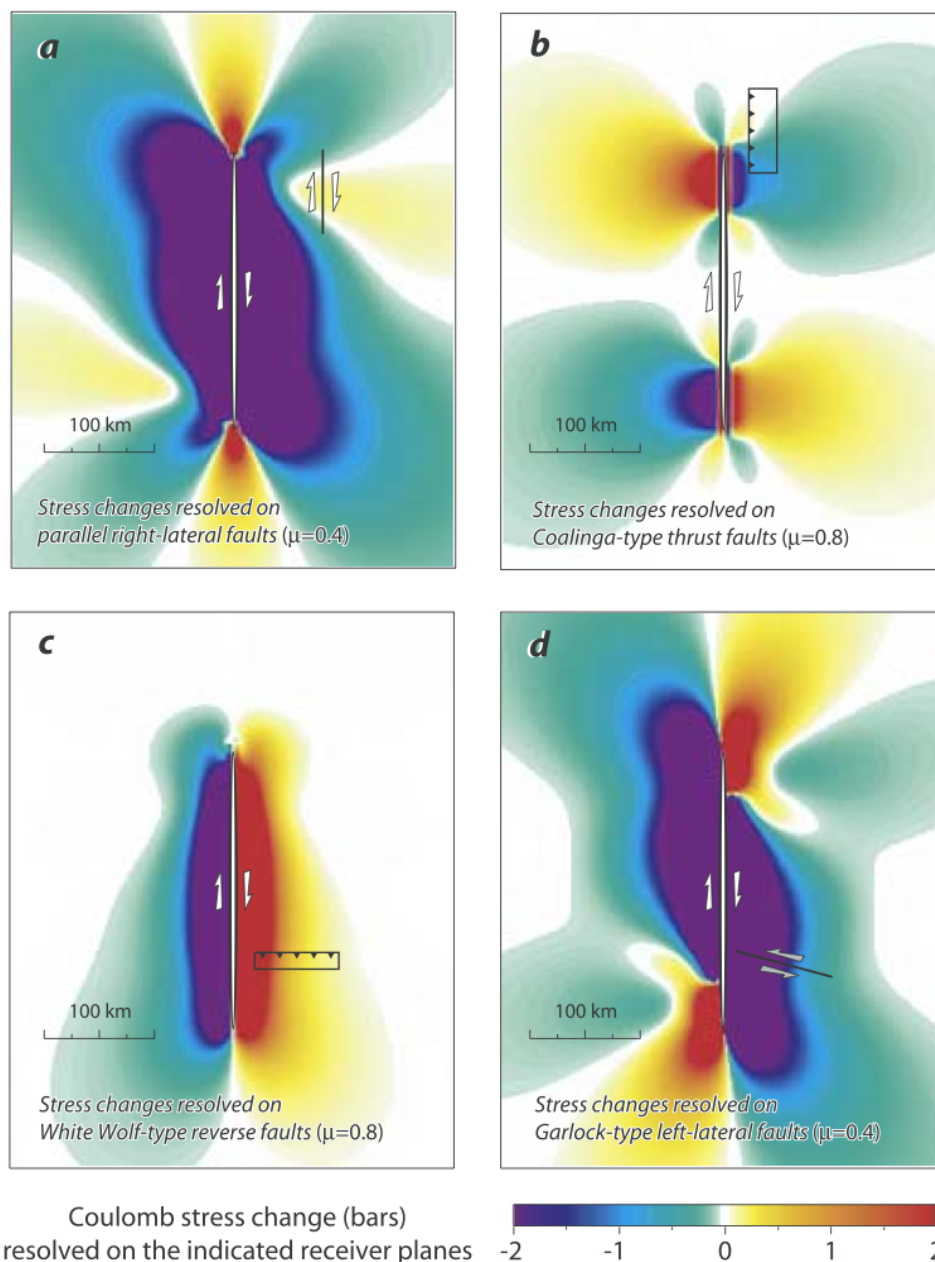
Every time you click “Cal. & View” in the “Stress” control panel, a numerical output file called “dcff.cou” will be created or overwritten and saved in a sub-folder you designate in the **Preferences** menu. Remember to rename dcff.cou if you want to save the numerical file.



### 7.5 The importance of receiver fault geometry in Coulomb modeling

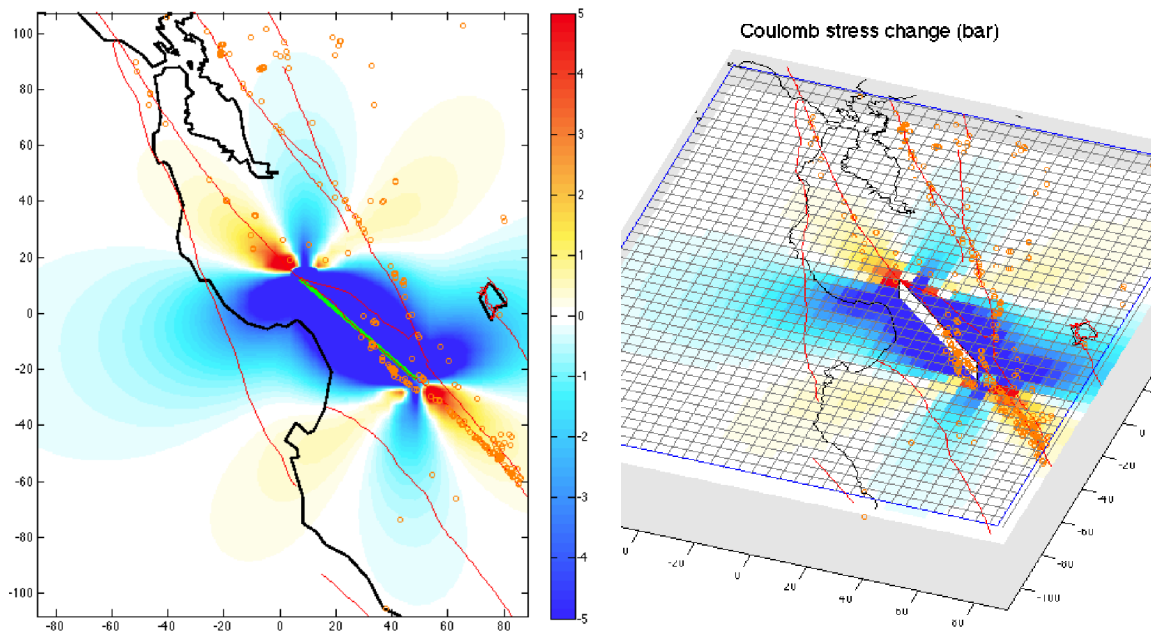
In the figure below, from Lin and Stein (2004), the source is an idealized M~7.9 right-lateral southern San Andreas rupture. The most familiar stress pattern is the case of source and receiver faults with the same strike, dip, and rake (**a**). But look how strongly the pattern changes when the receiver faults are nearby thrusts (**b-c**) or left-lateral faults (**d**). Thus, a stress shadow for one receiver may be a stress trigger zone for another receiver fault. Note also that in our work, we tend to assume a high coefficient of friction ( $\sim 0.8$ ) for

continental thrust faults, moderate friction (0.4) for strike-slip or unknown faults, and very low friction ( $>0.2$ ) for major transforms, such as the San Andreas. This is, in part, based on Parsons and others (1999).



## 7.6 Adding Coulomb stress to an overlay plot and viewing it in 3D

1. Launch "Example-SFBayArea.inp". **Overlay > Coastlines**. Open the "coastline data" folder in the Coulomb33 folder, and select "california\_coastline\_di\_pos.dat". Answer the pop-up question, "no" (some datasets treat western longitudes as negative; others do not). Now, **Overlay > Active faults**. Choose "California faults\_longlat\_dat".
2. You can now add any kind of stress changes to this plot without losing any of the overlays. Just hit **Functions > Stress > Coulomb stress change**, and select a stress component and option, and you will see a map view image such as that below left.

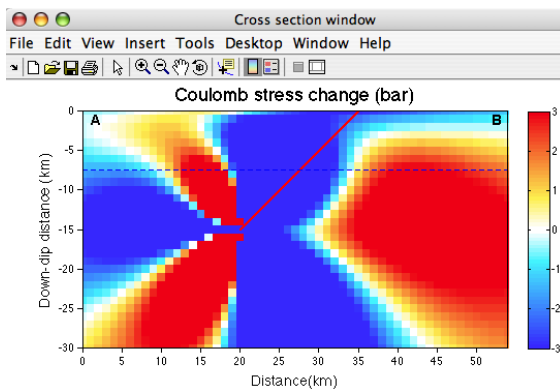


3. After completing any Coulomb stress calculation made over the grid, such as **Coulomb stress change**, **Shear stress change**, or **Normal stress change**, just return to the MATLAB window and type in "**coulomb\_3d\_view**". This calls a *plugin* (which can be found in the plugin folder in Coulomb33 folder). It executes a 3D view that you can manipulate and save as a pdf file, such as that above right.

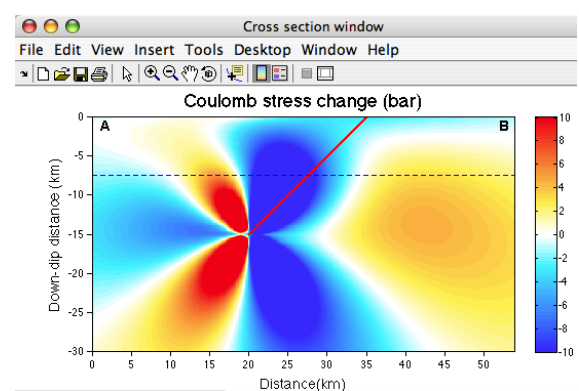
## 7.7 Coulomb stress cross-sections

1. Choose **Input > Open existing input file > Example-2(TH).inp**. Next, choose **Functions > Stress > Coulomb stress change**. Change the color saturation to 3.0 bars, and hit "Calc. & View" in the "Stress" control panel. After the mapview plot appears, hit the "Cross section" button on the Stress control panel, which displays the cross-section parameters from your input file (left plot below). Click "Calc. & View" and you will see the image below left. Now change the saturation to  $\pm 10$  bars and chose interpolated shading; hit "Calc. & View" again (right panel).

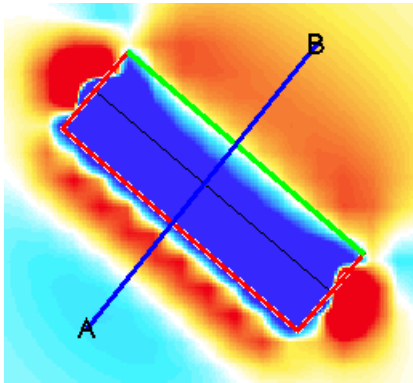
**Mosaic,  $\pm 3$  bars**



**Interpolated,  $\pm 10$  bars**



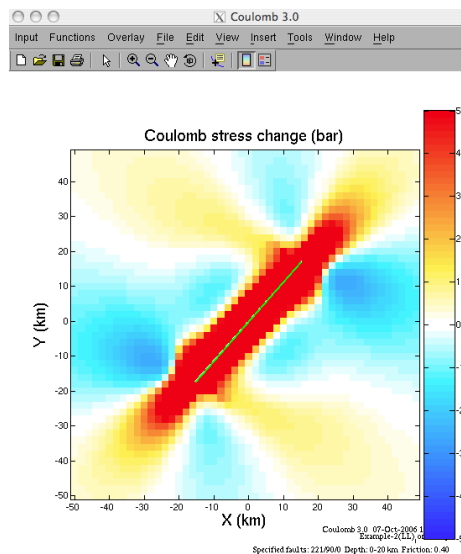
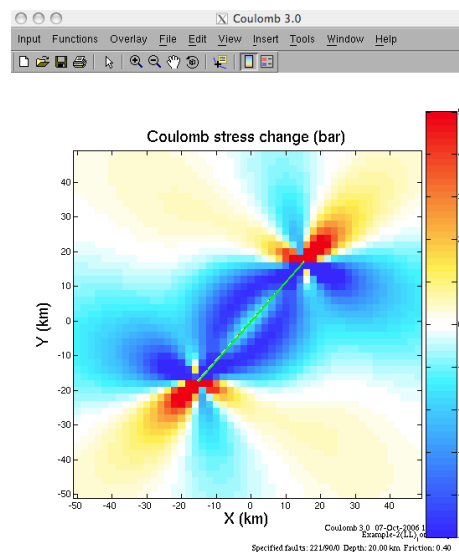
2. You can overlay seismicity in cross-sections if you first plot the mapview with earthquakes and then make the section. The default setting plots seismicity within  $\pm 20$  km of the section line. To change this, print `EQPICK_WIDTH=5` for  $\pm 5$  km, and so forth, in the command window.



**Cross section control panel**

Start (A)	x: -16.00	y: -16.00	km	
Finish (B)	x: 18.00	y: 26.00	km	Horizontal increment: 1.00 km
<input type="button" value="Mouse clicks"/> <input type="button" value="Open position file"/>				
Depth	30.00	km	Dip	90.00
Depth inc.	1.00	km		
Downdip inc.	1.0	km	<input type="button" value="Calc. &amp; view"/>	

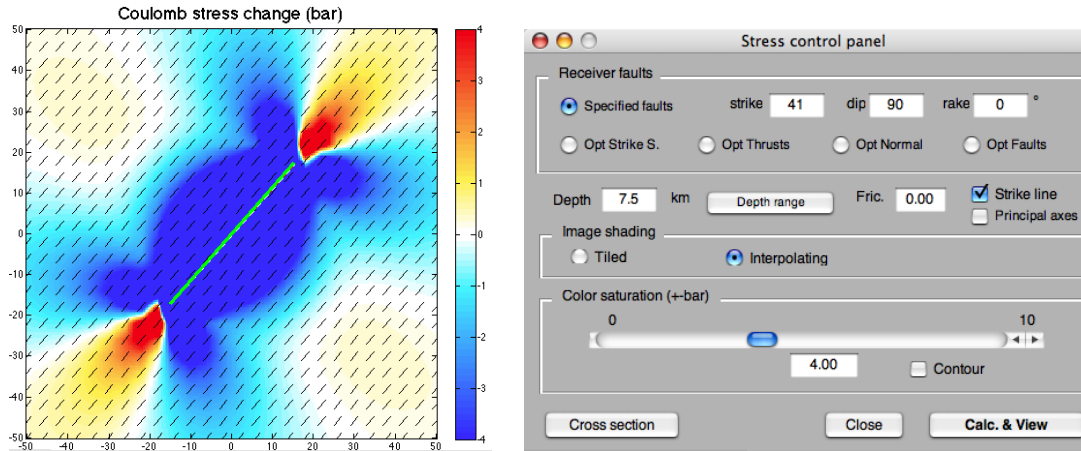
- You can also change the dip angle of the cross section by entering a non-90° value in the “Dip” box in the panel above; this is useful when you want to calculate stress on a thrust fault surface or a subduction interface. The blue dashed line is the depth at which stress was sampled in the map view. The red line is the intersection of the fault plane with the cross-section line. These can be seen in map view, which has a blue cross-section line, a red fault perimeter, a green line where the fault projects to the ground surface, and a black line where the fault intersects the depth at which stress is being sampled. You can change the depth, and many other parameters, in the “Stress” control panel.
- You can calculate the maximum or mean values of Coulomb stress changes between various depth ranges. Click “Depth range” and then “Cal. & View” in the Stress control panel, you will see “Depth control panel”. In the Depth control panel, enter depths of the top and bottom surfaces, as well as the depth increment, for which you want to perform the comparisons. You can calculate either “Maximum values” of Coulomb stress changes over the given depth range (below left), or the “Mean values” over the range (below, right). The numerical output file shows the maximum value at each grid point. The maps below were made using the left-lateral strike-slip fault input file, Example-2(LL)-lonlat.inp.

**Max stress change over a depth range****Mean stress change over a depth range**

- You can plot the orientation of the ‘specified fault’ strike in map view. Choose **Input > Open existing input file > Example-2(LL).inp**. Next, choose **Functions > Stress > Coulomb stress change**. Check the ‘strike line’ box in the *Stress control panel* and, for practice, change friction to 0.0, shading to



interpolated and then “Calc. & View”, resulting in the following image on the left. Notice that the lines strike 41° as specified. Stresses and slip lines are plotted on the lower left corner of each grid box.



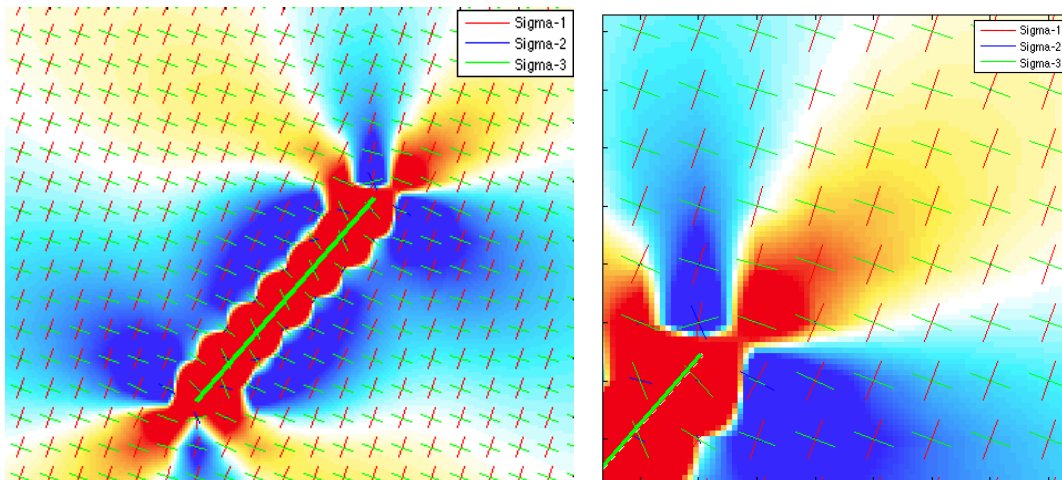
## 7.8 To display principal stress axes rotated by the earthquake stress change

Coulomb makes the tensor addition of the earthquake stress change, which diminishes with distance from the source fault, and the regional stress, which is assumed uniform, to calculate the total principal stress axes. Once the total principal stress axes are determined, Coulomb uses this and the assumed friction coefficient to determine the optimum planes.

Choose **Input > Open existing input file > Example-2(LL).inp**. Then, **Functions > Change parameters > Grid**, and change the grid to 5.0 x 5.0 km so the axes are not too crowded (this is not a requirement; you can choose any grid spacing of interest). Now, **Functions > Stress > Coulomb stress change**. In the pop-up “Stress control panel”, choose “Opt. Strike S.”, “Principal Stress”, and “Interpolating”, and click “Calc. & View”. You will see the image on left below. Using **Tools > Zoom In**, you’ll see the right image below.

### Normal view with principal axes

#### Zoomed view

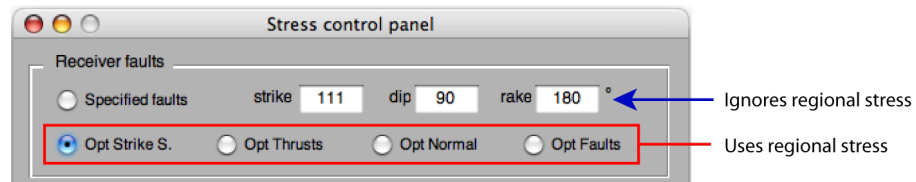


The axes are not scaled by their stress magnitudes, because too many would be invisible. Notice that the axes rotate in 3D, not just in the horizontal plane, and so  $\sigma_2$  deviates from being vertical close to the source, as a result of the stress changes imparted by the earthquake. This means that  $\sigma_2$  can be seen in near the end of the fault.



## 7.9 Using the regional stress in optimally oriented stress calculations

The regional (also called, “tectonic”) stress is used only when you choose one of the optimally oriented (“Opt.”) stress changes in the **Stress control panel** (below). Otherwise the regional stresses are ignored. See King and others (1994) for more on this topic.

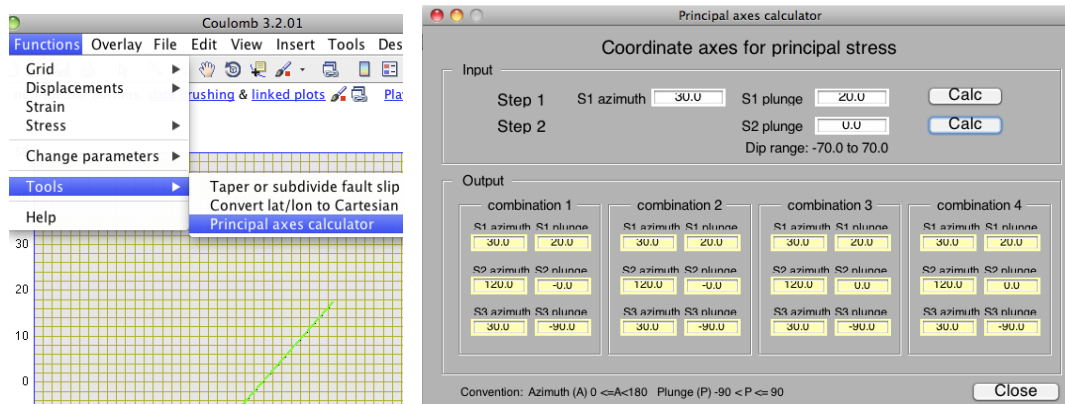


1. All of the example input files contain simple regional stress fields. The sign convention for S1, S2, and S3 is positive in compression (bars). Although you can assign axes that are neither horizontal nor vertical (in other words, they plunge at angles other than 0° and 90°), and you can assign a vertical gradient in the stress axes, such that the stress magnitude increases (or decreases) with depth, we advise you to keep it simple. We typically make the greatest principal stress, S1, horizontal and about 100 bars and the intermediate principal stress about 0 bars.
2. A reasonable regional stress must promote slip on all the faults in your area. You can use the P and T axes from focal mechanisms of earthquakes off the main faults, hydrofrac or borehole breakout information, and fault striae inversions to assess the strike of the greatest and least principal axes. The World Stress Map (<http://www-wsm.physik.uni-karlsruhe.de/>) may also be useful for this purpose. But most important, ask yourself if the stress tensor you are proposing is consistent with the region's active faults.
3. You can build principal stress axes (which must be mutually perpendicular) by selecting **Functions > Tools > Principal axis calculator**. You can also visualize the principal axes by **Functions > Stress > Coulomb stress change**, and then by checking “Principal axes” in the pop-up “Stress control panel.”

## 7.10 To display Coulomb stress changes on optimally oriented strike-slip, thrust, and normal faults (with the fault dip fixed)

“Optimally oriented” planes are those oriented such that the Coulomb stress change resolved on them is most positive (in our plots, most red). Here one assumes that aftershocks have a range of orientations and will be most abundant at the depth and location and have the geometry that most promotes failure. So at every point on our grid, we find the receiver plane on which the resolved Coulomb stress change is most positive. If the regional stress were zero, there would be a positive Coulomb stress change on some plane everywhere and at all depths. But at large distances from a source fault, the earthquake stress change will be much smaller than the regional stress, so the planes rotate very little.

1. Choose **Input > Open existing input file** > “Example-2(LL).inp”. To calculate optimally oriented faults, one must specify the regional (sometimes called, tectonic) stress field in the input file. “Example-2(LL).inp” contains a sample 3D regional stress field. If you use your own input file, make sure the regional stress tensor is properly defined. To make sure that the directions of your regional stress axes are geometrically compatible (that is, orthogonal to each other), choose **Functions > Tools > Principal axes calculator**. You will see a pop-up “Coordinate axes for principal stress” window (below).

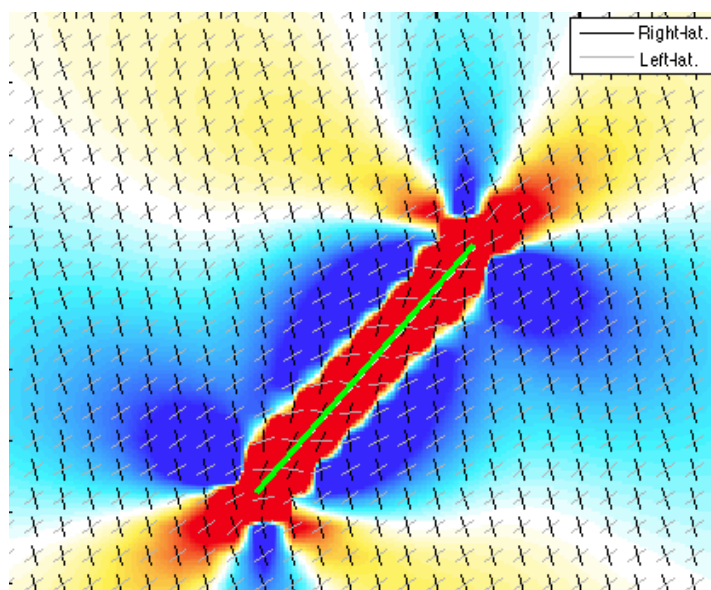


To check the compatibility of regional stress axes, first enter the strike and plunge of the greatest principal axis, S1 strike and S1 dip. Click “Calc”. Then enter the plunge of the intermediate principal stress axis, S2 dip, which should stay within the shown permissible range of values (“Dip range”) to ensure that three principal axes are mutually perpendicular. Click “Calc” again, and you will see four viable sets of combinations for the three principal axes.

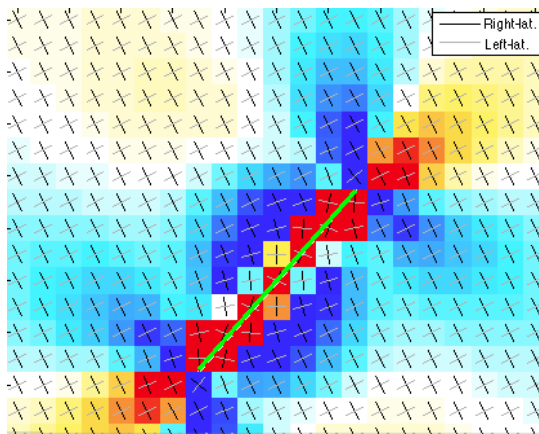
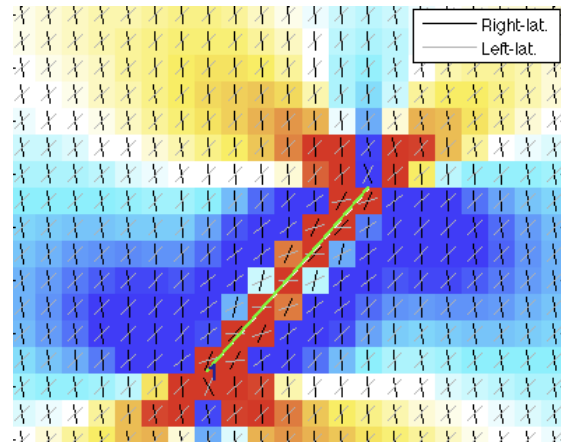
2. Choose **Functions > Stress > Coulomb stress change**. You will see the following in the pop-up “Stress control panel”:



In the “Stress control panel”, the alternatives are “Opt. Strike S.”, “Opt Thrusts”, “Opt Normal”, and “Opt Faults”. (“**Opt Faults**” is an exceedingly slow grid search over the entire focal sphere for the receiver planes at every grid point, and so choose a coarse grid and you will need patience in waiting for the completion of the calculation. Try 10° for the search increment). Here, choose “Opt Strike S.” and click on “Strike lines”; then click “Calc. & View” and you will see this in the interior of the plot:

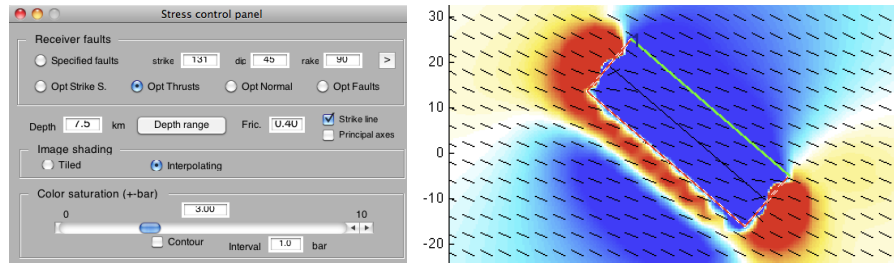


3. **Explanation of the Slip lines.** For the “Opt Strike S.” option, the receiver faults dip vertically and their strikes are a function of  $S_1$  ( $\sigma_1$ ) and the friction coefficient  $\mu$  (FRIC in Coulomb). The right-lateral and left-lateral optimum planes are plotted at every grid point. Their internal strike angle is a function only of the friction coefficient; these planes are acute to each other for high friction and orthogonal for zero friction. (For normal and thrust planes, the strike for the two planes is the same and their dip is a function of the friction coefficient). You can see large rotations of these planes very close to the source fault because the earthquake stress change is about as large as the assumed regional stress,  $\sim 100$  bars. Far from the source, the slip lines are parallel and their orientation is a function of the regional stress in the input file, because at these distances from the source, the earthquake stress changes are negligible. For thrust and normal faults, their dip is a function of the friction coefficient, and their strike is perpendicular to  $S_1$  ( $\sigma_1$ ) and  $S_3$  ( $\sigma_3$ ), respectively. The relationship of the angle,  $\beta$  between  $S_1$  and the dip (for strike-slip faults) or strike (for dip-slip faults) is  $\tan 2\beta = 1/\text{FRIC}$ . See King and others (1994), which can be accessed online from the Coulomb web site at Stein’s website, <http://profile.usgs.gov/rstein>.
4. For a friction coefficient of zero, the optimum planes would be orthogonal and we could compare them to aftershock focal mechanisms unambiguously. Then, **Functions > Change parameters > Grid**, and change the grid to 5.0 x 5.0. Then hit **Functions > Stress > Coulomb stress change**. In the “Stress control panel”, change Fric. to 0.0, check “Opt. Strike S.”, and ‘strike line’. An excerpt is shown below left. Repeat the process and in the “Stress control panel”, change the friction to 0.8 and hit the tab. You’ll see the image on the right.

**Friction coefficient = 0.0****Friction coefficient = 0.8**

The stress changes are larger and more asymmetrical with respect to the source fault for high friction, and the rotation of the optimal planes near the source fault are a little greater. These aspects are discussed in King and others (1994).

5. Strike lines for optimally oriented thrust faults. Choose **Input > Open an existing file** and choose “Example-2(TH).inp”. Then choose **Functions > Stress > Coulomb stress change**. In the “Stress control panel”, check “Opt. thrusts”, ‘strike line’, set friction at 0.4,  $\pm 3$  bar saturation, and hit “Interpolating” (left below). You will see an image like this:



Here the two strike lines are parallel in the mapview (they would not be so in cross-section), so only one is visible. The rotations are greatest in the deep red and blue areas, where the stress change is large relative to the assumed regional stress. In this example, the fault is not quite orthogonal to the assumed regional stress.

### 7.11 To resolve stress imparted to receiver faults (“Calc. stress on faults”)

This is perhaps the simplest Coulomb calculation, and it is widely used in research. The regional stress information is not used, regardless of whether it is included in the input file. Coulomb permits one to show the resolved stresses graphically and output the numerical results.

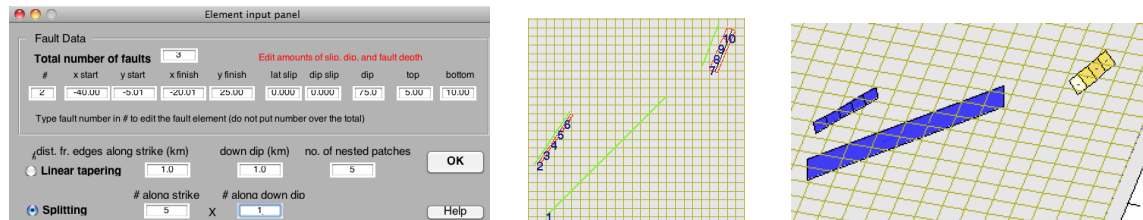
1. Choose **Input > Open & edit input file**, and select “Example-1.inp”. Notice that there is a source fault with slip (#1) and two receiver faults (#2 and #3). Enter the fault# to see the slip:

Fault Data											
Total number of faults 3											
#	x start	y start	x finish	y finish	Kode	rt.lat slip	dip slip	dip	top	bottom	
1	-35.00	-35.01	35.00	35.01	100	2.000	0.000	90.0	0.00	12.00	
	(km)	(km)	(km)	(km)		(m)	(m)	( )	(km)	(km)	

Fault Data											
Total number of faults 3											
#	x start	y start	x finish	y finish	Kode	rt.lat slip	dip slip	dip	top	bottom	
2	-40.00	-5.01	-20.01	25.00	100	0.000	0.000	75.0	5.00	10.00	
	(km)	(km)	(km)	(km)		(m)	(m)	( )	(km)	(km)	

To see the variation in resolved stress along the receiver faults, you can split them into sections by right-clicking on the fault, and selecting ‘splitting’ in the “Element input panel” (below left). After you have split the receivers, you will see an image like that below (center).

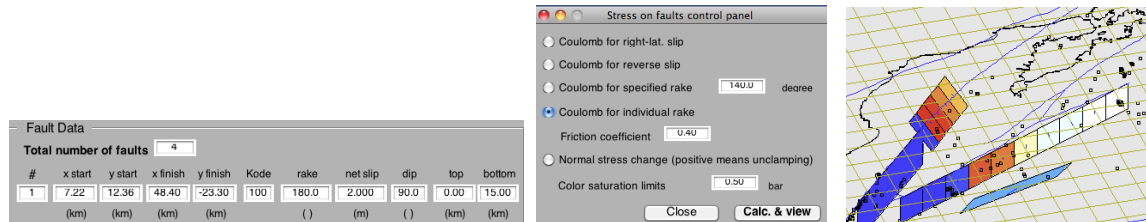


2. Now, **Functions > Stress > Calc. stress on faults**. A “Stress on faults” control panel will open to let you choose the stress component that you would like to resolve on the faults. We chose right-lateral faults; see the stress changes imparted by the source (fault#1) on the receivers (#2-10) in the image above right. Using the swivel tool, you can change the perspective; you can also change the saturation to bring out the along strike variations.
3. If your input file used the “.inp” (rake, net slip) rather than the “.inp” (rt.lat. slip, reverse slip) format, then you could use the “Coulomb for individual rake” option. **To switch how the input file is interpreted, it searches for the word, “rake,” so don’t misspell it.** In the input folder, the full 1400-patch California Reference Database is included in various formats. “CA-fault-database-rake.inp” (and “CA-fault-database-rake.mat”) are formatted by rake for this purpose. Because it is a large file, it takes time to calculate. Here are the first two sources in the database input file, with the right-lateral (rake=180°) Green Valley reverse (rake=90°) Mount Diablo thrust faults:

#	X-start	Y-start	X-fin	Y-fin	Kode	rake	net slip	dip angle	top	bot	
1	-181.8571	115.5202	-187.3601	139.9612	100	180.0000	0.0000	90.0000	0.0000	14.0000	#Green Valley (So)
1	-160.3110	81.1833	-178.9410	97.5293	100	90.0000	0.0000	38.0000	8.0000	16.0000	#Mount Diablo Thrust

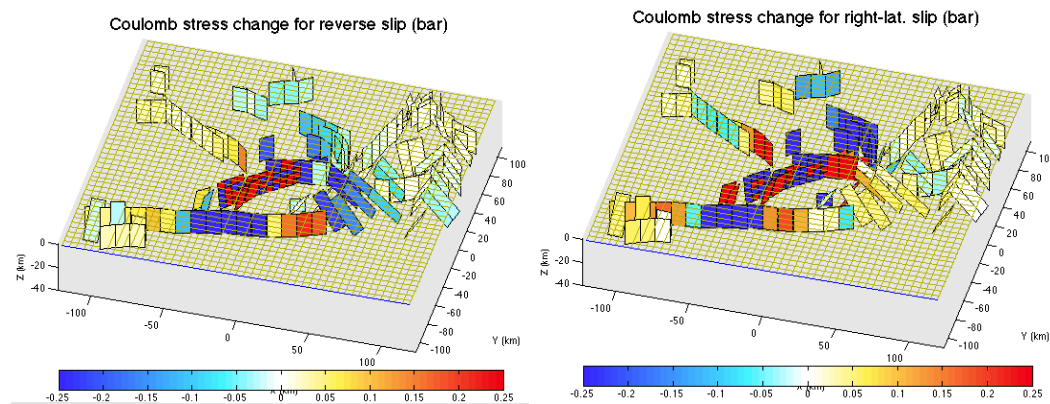
You can also use a subset and plot it, since all the faults have their associated names. Remember to make sure the “#fixed=“ in the third line of the input file is changed to reflect the number of faults in the input file (“#fixed= faults + receivers).

- Now try a file in the rake format. **Input > Open and edit existing file > SFBay\_rake.inr**. Notice that there are fields for rake and net slip instead of strike-slip and dip-slip (below left). Now choose **Functions > Stress > Calc. stress on faults** and choose “Coulomb for individual rake” (below center). You will see a perspective view with the fault patches colored by their Coulomb stress resolves for the rake of each receiver (below right). Below, we’ve added coastlines, faults, earthquakes, made the grid coarser (the nodes are not used in a “calc. stress on faults” run), and swiveled the view.



- A complex case is the 1995 Kobe earthquake. Both a uniform-slip and a variable slip source model input file are included in the input file folder, in addition to about 50 surrounding faults with various orientations and dips. **Input > Preferences > Cartesian**; then **Input > “Kobe-uniform-slip.inp”**; then **Functions > Stress > Calc. stress on faults**. Note that a numerical output file is created each time you make a **Calc. stress on faults** run, which is very useful for further analysis and gives much more stress information. Two components are shown below. Using the swivel tool with files this large takes patience due to the time lag.

### *Stress from the 1995 Kobe variable-slip model resolved on surrounding faults*



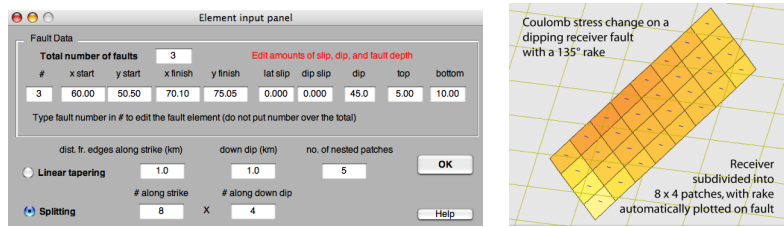
Notice that on the Kobe rupture itself, there are both red and blue patches. The Coulomb stress change is not uniformly negative (blue) because of the irregular coseismic slip which leaves spikes of stress increase, the presumed sites of along-fault aftershocks.

## 7.12 Calculating stress change on a subdivided (tiled) receiver fault

Often one would like to determine the distribution of stress change on a large receiver fault.

- Launch “Example-2(TH).inp”. **Functions > Tools > Taper or subdivide fault slip**, type fault “3” in the fault # box, split the source into 5 x 2 patches, and hit OK (below left). So now you have subdivided it into 32 patches.





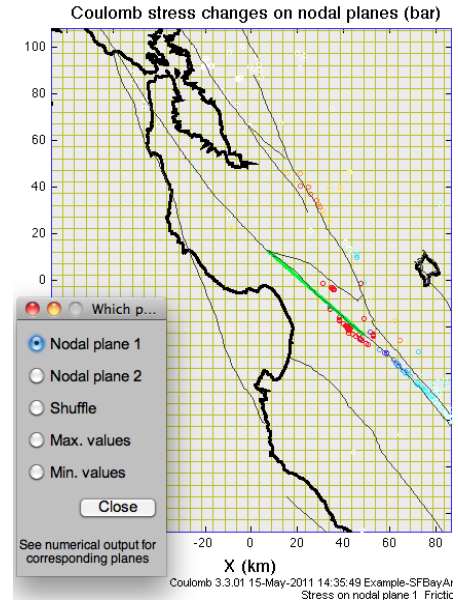
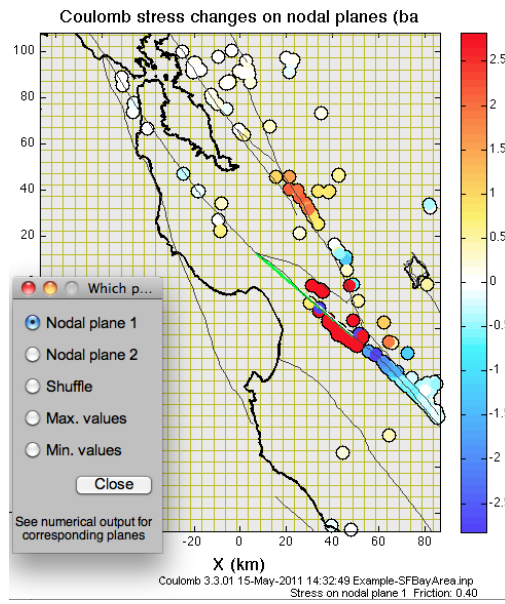
2. **Functions > Stress > Calculate stress on faults.** You can zoom in and spin the view, as shown above right. The Coulomb stress change is colored and the rake vectors are in blue.

### 7.13 Coulomb stress changes resolved on earthquake nodal planes

1. If focal mechanism information is available, you may want to test whether the fault plane associated with each earthquake was brought closer to Coulomb failure. This is presumably a more stringent test than determining if earthquakes occurred in the red regions, although typically only a fraction of the catalog contains reliable focal mechanisms. If the friction were 0, this would be a straightforward test because the shear stress change on the orthogonal nodal planes is identical (such a test is used in Parsons, 2002). But for non-zero friction, the optimum Coulomb planes are not orthogonal, and so they will be different. In fact, one plane may have a stress increase and the other a decrease. You can sometimes infer the fault plane based on independent information, and there are published approaches others have taken, such as comparing the percentage of stress increases on seismicity in the region before and after a mainshock (Ma and others, 2005), or by using seismicity alignments.
2. Using “Example-SFBayArea.inp”, **Overlay > Earthquakes >** In the “Earthquake catalog formats” window, select “NCSN ffit (focal mech)”, and then choose the dataset with this name from the folder. Earthquake circles plot on the map. Now, **Functions > Stress > Calc. stress on nodal planes.** If the focal mechanism file only includes one set of nodal planes, Coulomb asks you if you want it to generate the other set, so answer “yes.” A window appears to ask you which set (Nodal set 1 or set 2, which are usually arbitrarily ordered in a catalog, the maximum of each pair, or Shuffle—random selection of set 1 or 2). It will assign colors to each earthquake according to how much the nodal planes were brought closer to or farther from failure. It does not plot beachballs (the focal mechanism orientations). You should see this plot:

*Raster image (default)* *Vector version (set IVECTOR=1)*



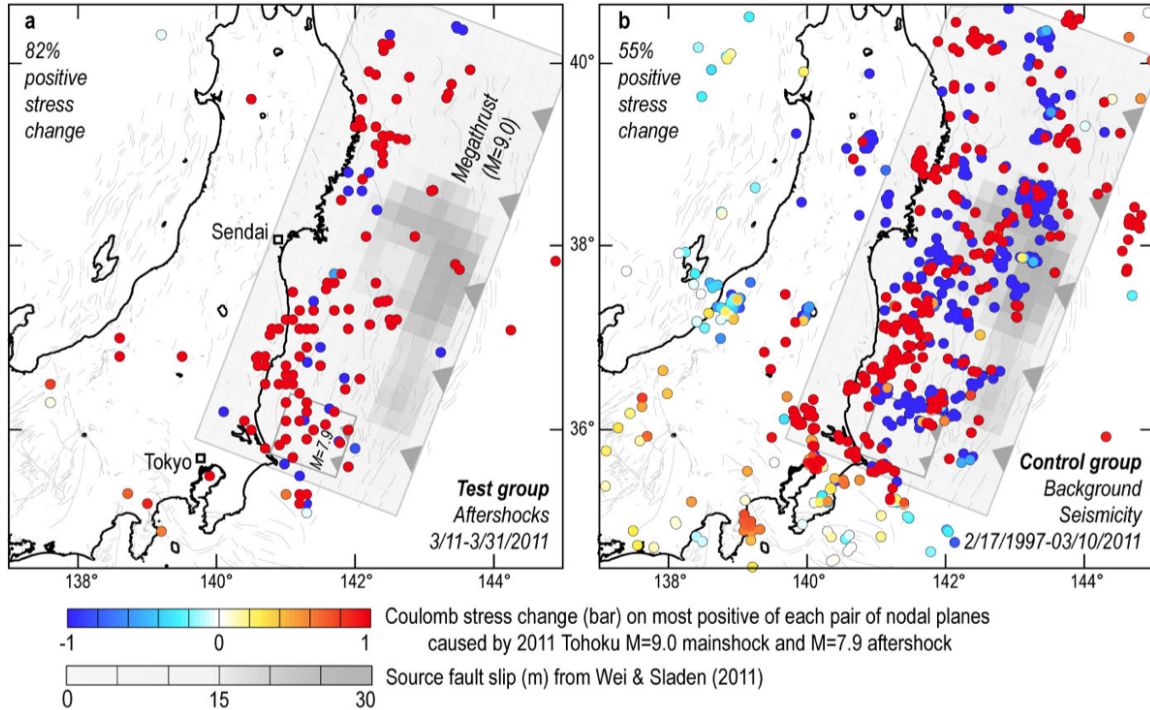


You can plot each set (Nodal plane 1 or Nodal plane 2) separately, choose the nodal plane on which the Coulomb stress change is most positive (“Max. values” or most negative, “Min. values”), shuffle them randomly. You can edit the catalog in an editor to make set 1 the likely fault planes. The numerical output file also calculates the maximum (most positive) Coulomb stress on each nodal plane and gives the corresponding optimum rake.

```
-----
This image is saved as a raster image when saved.
If you want to save a vectorized & editable image, type
    IVECTOR = 1;
in the command window here and execute it again.
-----
>> IVECTOR=1;
```

The default file is a raster image (above left), but if you write “IVECTOR=1” in the MATLAB Command Window, and then save the file, you will get a vector image like the one above right. To change the circles to disks of colors, just select all circles and increase the stroke thickness. You do not need a fine grid increment (olive green lines in the above images), because these are ignored for this calculation. We suggest you use a course grid such as  $0.5^\circ$  lon. x  $0.5^\circ$  lat.

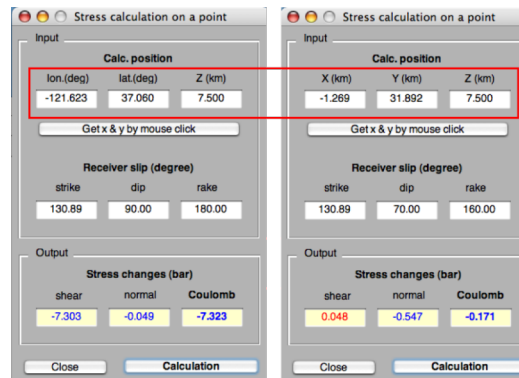
Here, below, is an example from a recent paper of ours (Toda and others, 2011). The source fault slip, in grayscale, is from **Grid > 3D view** (click on swivel tool, and then rt.click and choose “Go to x-y view”), and then we used the “Max. values” option of **Stress > Calc. stress on nodal planes**. We use the ratio of the percent of positive mechanisms of the aftershocks (the “test” group) to the percent of positive mechanisms of the background (pre-mainshock) earthquakes (the “control” group) to test the Coulomb hypothesis and the source model. Here, we tested 6 source models and 3 values of friction (0.0, 0.4, and 0.8) to find the best case.



### 7.14 Coulomb stress at a point, from lat/lon, x/y, or a mouse click

Sometimes you want to probe the calculated stress changes at a given point, rather than over a regular grid or on receiver faults. This is easy to do in Coulomb by using the mouse or by entering a lat/lon or UTM coordinates.

1. **Functions > Stress > Calc. stress at a point.** A “Stress calculation on a point” window pops up. You can enter the coordinates and depth of interest, and you can also enter the receiver fault geometry. The output is numerical, and appears in the “Output” portion of the window, with blue numbers when negative and red when positive (as below).



2. When using the **Calc. stress at a point** option, you can change the assumed friction coefficient in the same manner that you can for other stress calculations, by choosing **Functions > Change parameters > Change Coefficient fric.**. If you want to use x/y values, change to Cartesian coordinates in the **Preferences** menu. Then return to the **Calc. stress at a point** selection and use the “Stress calculation on a point” window. The lat/lon vs. Cartesian options are highlighted above in the red box.

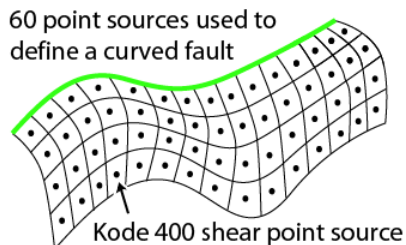
## Chapter 8

## Magmatic Sources, Google Earth Displays, Polygon Digitizing

At this point we assume that you are now familiar with the typical steps and menu options in Coulomb, and our instructions will be more abbreviated, but still accurate.

### 8.1 Point shear sources for small quakes or curved faults (Kode 400)

1. If you specify Kode 400 rather than 100 in the input file, Coulomb will interpret it as a point source with right-lateral and reverse slip components. The location of the point source is defined by the rectangle in the input file. The point is located at the center of the rectangle: at the midpoint of the start and end positions and at the mid-depth of the top and bottom positions. The plane defined by this geometry is used for strike and dip of the point source. This is a simple way to represent small shocks.
2. Another use of Kode 400 sources is if you have a very crenulated or curved fault, the overlap and underlap of the rectangles can be avoided by making a mesh of point sources (shown schematically below left). But don't sample the stress closer to the fault than the point spacing, or you will see numerical noise (aliasing).



Fault Data										
Total number of faults 1										
#	x start	y start	x finish	y finish	Kode	rt.lat potency	dip potency	dip	top	bottom
1	0.00	0.00	3.00	3.00	400	2.0e+07	0.0e+00	90.0	0.00	5.00
	(km)	(km)	(km)	(km)		(m <sup>3</sup> )	(m <sup>3</sup> )	(°)	(km)	(km)

3. We provide an input file with a single point source, "Example-Kode400.inp". Note that the right-lateral and reverse units are in potency ( $\text{m}^3$ ), not in slip (m), since a point has no area (see above right, from **open & edit input file**). Potency, or the geometric moment, is seismic moment/shear modulus (see boxed equation in Chapter 3 to calculate G from E and PR).

### 8.2 Crack opening or closing (Tensile Kode 200 and 300 sources)

Many magmatic intrusion problems involve a tabular body, such as dike or sill, undergoing expansion or contraction. Here we introduce the deformation and stress change caused by a tensile component of displacement, such as the opening or closing of a tabular or crack-like body, using the equations of Okada (1992). For simplicity, the input file format for Coulomb has only two slip components, labelled "rt.lat" and "reverse" or "rake" and "netslip". So, when you change the Kode of the source to 200 or 300, the first of these slip components takes on a tensile-displacement interpretation by the program, as described below.

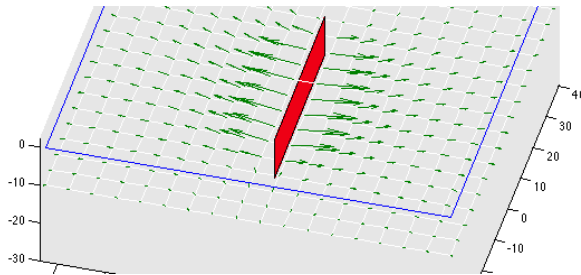
1. **Kode 200** permits tensile (opening) displacement and strike slip to be input. (dike opening is positive; unit = meters), "Example-6(200Kode).inp". Here's how a Kode 200 source appears in the **Functions > Open & edit input file** window,

Fault Data										
Total number of faults 1										
#	x start	y start	x finish	y finish	Kode	rt.lat slip	tensile open	dip	top	bottom
1	2.00	-15.00	2.00	15.00	200	0.000	1.000	90.0	5.00	25.00
	(km)	(km)	(km)	(km)		(m)	(m)	(°)	(km)	(km)

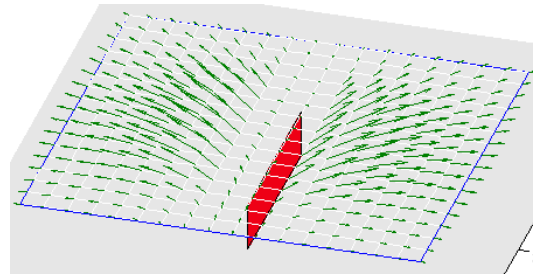
2. **Kode 300** permits tensile (opening) slip and dip-slip to be input. For Kode 300, put tensile slip in the "rt.lat." column (again, dike opening is positive), and put reverse slip in the "reverse" column.

3. If the element has three components of slip (strike-slip, dip-slip, and tensile-slip), you can accomplish this by including both Kode 200 and a Kode 300 sources in the input file as shown in the file below, "Example-7(200-300kode).inp".
6. Define the dike geometry (endpoints, dip, and top/bottom depth) as you do for faults. Unfortunately, the way we define sources and receivers does not permit one to put in a strictly horizontal plane, since the top and bottom depths would be identical, but you can put a tiny dip ( $\sim 1^\circ$ ), and it will work fine.
5. Uniform opening or closing of a dike is likely to be unrealistic. Just as you can for faults, you can taper the displacement toward the edges by **Functions > Tools > Taper**.
6. Select the file, Example-8(dike).inp, and then choose **Functions > Displacements > 3D Vectors**. You will get the image shown on the left. Now, **Functions > Change Parameters > Vertical Exaggeration > 25000**, and change **Calculation depth** to the surface (0.0 km). You will get the image on the right. Experiment with view angles.

**3D Vectors at 10 km depth for a dike  
surface for a dike**



**3D Vectors at the free  
surface for a dike**



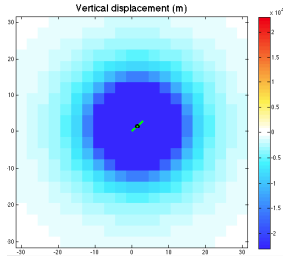
### 8.3 Point source of deflation or inflation (Kode 500)

We have implemented the formula of Okada (1992) for a buried point source of expansion or contraction. Of course, the calculated stress changes very close to such a point source are infinite and are thus unreliable, but at larger distances, this source is useful for magmatic intrusion problems, such as studying how an intrusion event may bring other faults or dikes closer to failure. An example of this is Nostro and others, 1998, available at <http://profile.usgs.gov/rstein>. As with the dike or sill source, we have created two "kodes" for mixed volumetric and shear displacements.

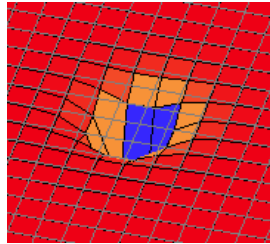
1. The unit for deflation or inflation is potency ( $\text{m}^3$ ), the volume change associated with the evacuation or expansion of a spherical magma chamber. **Expansion is positive**. The unit for the strike or dip slip is meters, as usual. One designates the source as Kode 500.
2. **Kode 500** permits both a dike and point source of expansion to be input. Put the tensile opening in the first ("rt-lat.") column (units are  $\text{m}^3$ ; right-lateral is positive), and put the point source in the "reverse" column (units are  $\text{m}^3$ ; expansion is positive).
3. The location of the point source is defined by a plane in the input file. The point is located at the midpoint of the start and end positions and at the midpoint of the top and bottom positions. The plane defined by this geometry is used for the dike opening. So if you only calculate the point-source expansion, the length and width of the plane are unimportant; only if you also want to consider opening or closing of the planar dike do these dimensions get used in the calculation. The point source is indicated in graphic output files as a small black circle.

The figures below left were made using “Example-9(Kode500).inp” with two different **Displacement** options selected. The surface projection of the dike is the short green line.

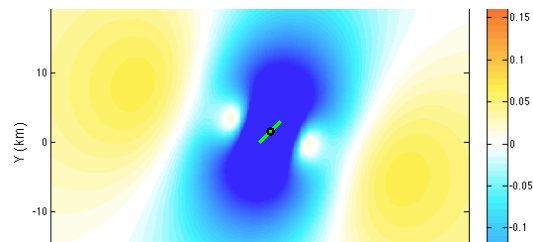
**Vertical displ.**



**3D image drape  
normal faults**



**Stress change on optimal**



In the example above right, we have chosen **Stress > Coulomb stress change > Opt Normal**, with a 1 x 1 km grid, friction=0.8, depth of 8 km, and color saturation of  $\pm 0.25$  bars:

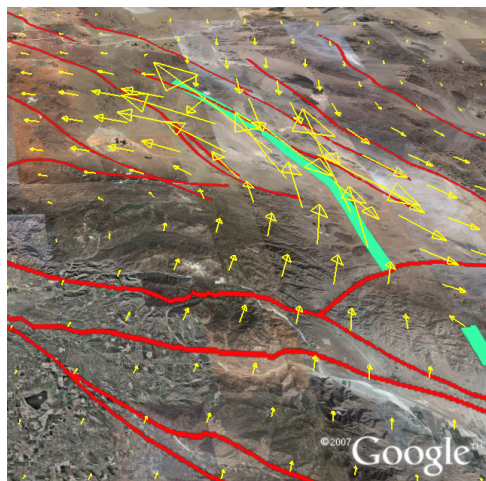
## 8.4 Displaying Displacement, Stress, and Overlays in Google Earth

Google Earth offers wonderful opportunities to drape Coulomb files on satellite images and DEMs. You need to download and install Google Earth on your computer before following these steps. In addition to this, you will need Adobe Illustrator or any good graphic application.

1. Make sure that you have selected the “lon. & lat.” **Coordinate** option in the **Preferences**.
2. Run any horizontal displacement function, such as **Horizontal displ. (vectors)** or **Horizontal displ. (wireframe)**. Add the **Overlay** options that you would like in the plot. When the final plot appears in the Coulomb 3.3 window, type “**coulomb2googleearth**” in the MATLAB Command Window, and hit return. You will get messages in the command window once files are saved.

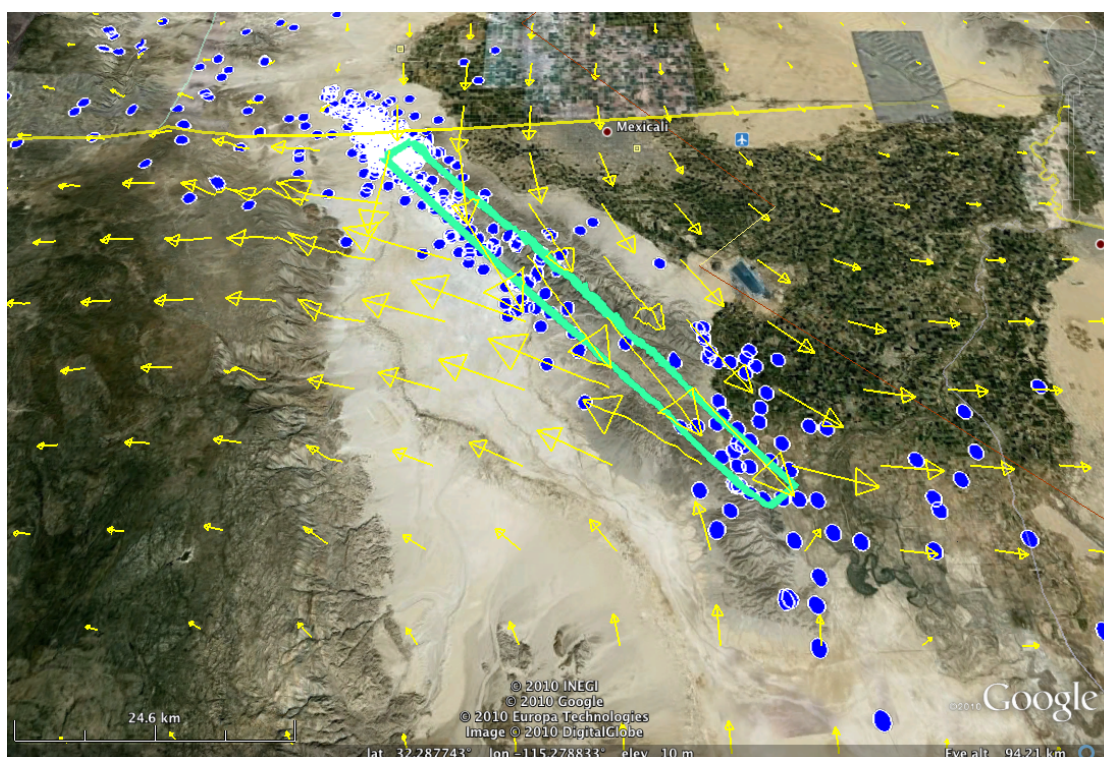
```
>> coulomb2googleearth
Calculating... Please wait...
-> 'coulomb_study_area_box.kml' is saved in the current directory.
-> 'coulomb_displ_horizontal.kml' is saved in the current directory.
-> 'coulomb_source_fault_plot.kml' is saved in the current directory.
-> 'coulomb_afault_plot.kml' is saved in the current directory.
Done!
```

3. Then, you can drag the kml files onto the Google Earth icon on your computer dock or desktop, or you can open the files from the Google Earth menu.



Above we used “Landers-uniform-slip.inp” and **Displacement > Horizontal Displ. (Vectors)**.





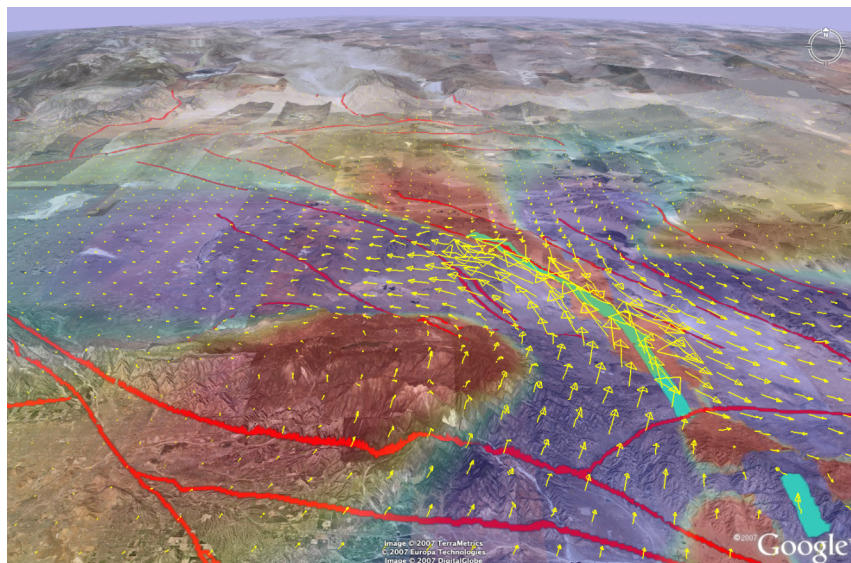
The figure above was made for the 2010 M=7.2 El Major-Cucapah, Mexico, earthquake using the input file, “Baja\_CA\_2010\_eq.mat” and choosing surface **Displacement Vectors**. We have tilted the scene for perspective and exaggerated the relief to the maximum 3-fold level in Google Earth.

4. For color gradient images such as are created in the **Coulomb stress change**, **Shear stress change**, **Normal stress change** options, or the **Vertical displacement (color)** options **File > Save As... pdf** using the commands, renaming them.
5. Open the .pdf files in Illustrator or the graphics software you are using, and remove all the text and lines, keeping only the color (raster) image. Save the color image as .jpeg file, and name it “coulombmap.jpeg” in the Coulomb directory.
6. Type “coulomb2googleearth” in the command window. This calls a script that is run by Coulomb. You will get the overlay kml file.

```
>> coulomb2googleearth
Calculating... Please wait...
-> 'coulomb_study_area_box.kml' is saved in the current directory.
-> 'coulomb_source_fault_plot.kml' is saved in the current directory.
Done!
>>
```

In the preceding image, a Coulomb stress change image was added. Google Earth also lets you control the translucency of the jpeg.

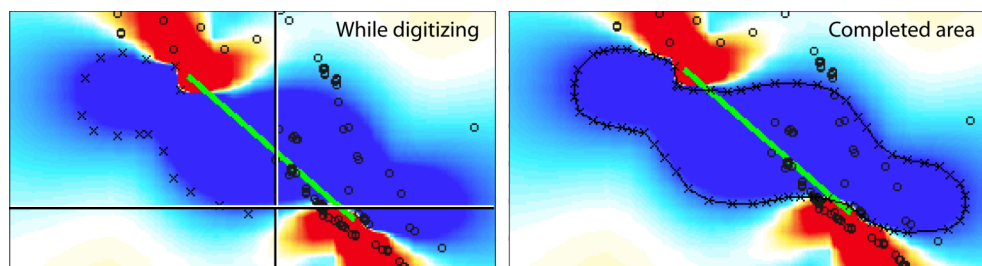
7. The full plugin script can be found in the “plugins” folder in the Coulomb33 folder. See the figure on the next page to see a color gradient map plus vector information.



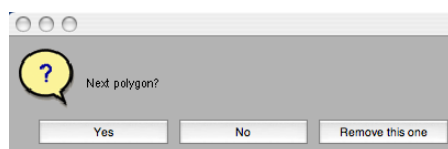
## 8.5 Digitize Polygon Function (to create a lat/lon file of an arbitrary area, such as a stress-change contour)

The “Digitize Polygon” function is useful for comparing a zone of Coulomb stress change with aftershocks or the seismicity rate change as calculated from the independent MATLAB program, ZMAP.

1. Make sure that you have selected the “lon. & lat.” **Coordinate** option in the **Preferences** menu.
2. Run any 2D map view function in Coulomb, and then type “**digitize\_polygon**” in the MATLAB Command Window, and hit return. Here, we have used “Example-SFBayArea.inp” selected a Coulomb mapview, and digitized a -3 bar stress shadow contour.



3. The mouse becomes a digitizing cursor in the Coulomb main window. You will see a large “+” over the map (above left). To digitize, make multiple left-button clicks to circumscribe an area. Finalize and close the area by using a right-button click; the graphic will then show the completed area (above right). A window (left below) asks if you intend to digitize multiple areas; hit “no” if this is all you will do. The digitized file is saved in the Coulomb33 folder as “polygons1.dat”, etc. The first 8 lines are shown below at right; it is in lat/lon coordinates; western longitudes are negative.



```
polygons1.dat
-1.2195162e+02 3.7086540e+01
-1.2195645e+02 3.7129961e+01
-1.2200000e+02 3.7145714e+01
-1.2203387e+02 3.7153590e+01
-1.2208225e+02 3.7165405e+01
-1.2218870e+02 3.7165405e+01
-1.2222740e+02 3.7133899e+01
-1.2225159e+02 3.7102393e+01
```

4. In ZMAP, you can move the file to the ZMAP folder and read it from the area selection function. For Stefan Wiemer’s ZMAP, see <http://www.earthquake.ethz.ch/software/zmap>



## Chapter 9

## Input File Structure

## Structure and formats of the Input file

**Example-1.inp**

61/1657 Macintosh HD:Desktop Folder:Coulomb:Input\_Files:Ex

This is an example. You can use first two lines (rows) for some comments or notes. Two lines of comments and notes.

#reg1= 0 #reg2= 0 #fixed= 3 sym= 1 PR1,PR2: Poisson's ratio for region 1 and 2  
PR1= .250 PR2= .250 DEPTH= 8.00 DEPTH: Target depth [km] E1,E2: Young's modulus [bar]  
E1= 0.800000E+06 E2= 0.800000E+06  
XSVH= .000 VSVH= .000  
FRIC= .400  
S1DR= 89.9000 S1DP= .000000 S1IN= 100.000 S1GD= .000000  
S2DR= 89.9000 S2DP= 90.0000 S2IN= 20.0000 S2GD= .000000  
S3DR= 179.900 S3DP= .000000 S3IN= .000000 S3GD= .000000  
Parameters for regional stress field (for explanation and graphic plot, see Conventions figure in Chapter 2)

#	X-start	Y-start	X-fin	Y-fin	Kode	shear(m)	reverse(m)	dip angle	top(km)	bot(km)	
1	-35.00	-35.00	35.00	35.01	100	2.00	0.00	90.00	0.00	12.00	source
1	-40.00	-5.00	-20.01	25.00	100	0.00	0.00	75.00	5.00	10.00	receiver-1
1	60.00	50.50	70.10	75.05	100	0.00	0.00	45.00	5.00	10.00	receiver-2

Grid Parameters

#	Start-x	Start-y	Finish-x	Finish-y	x-increment	y-increment
1	-100.0000	-100.0000	100.0100	100.0100	5.000000	5.000000

Size Parameters

#	Plot size	Shade/Color increment	Exaggeration for disp. & dist.
1	1.0000	0.200000	10000.00

Cross section default

#	Start-x	Start-y	Finish-x	Finish-y	Distant-increment	Z-depth	Z-increment
1	-16.00000	-16.00000	18.00000	26.00000	1.000000	30.00000	1.000000

Input file (Explanation)

**Example-1.inp**

0/2227 Macintosh HD:Desktop Folder:Coulomb:Input\_Files:Example-1.inp

This is an example. You can use first two lines (rows) for some comments or notes. I3, I3, I3, I3  
#reg1=0 #reg2=0 #fixed=3 sym=1 I3, I3, I3, I3  
PR1=0.250 PR2=0.250 DEPTH=8.00 G15.3, G15.3, G15.3  
E1=0.800000E+06 E2=0.800000E+06 E15.3, E15.3  
XSVH=0.000 VSVH=0.000 G15.3, G15.3  
FRIC=0.400 G15.3  
S1DR=89.9000 S1DP=0.000000 S1IN=100.000 S1GD=0.000000 E15.6, E15.6, E15.6, E15.6  
S2DR=89.9000 S2DP=90.0000 S2IN=20.0000 S2GD=0.000000 E15.6, E15.6, E15.6, E15.6  
S3DR=179.900 S3DP=0.000000 S3IN=0.000000 S3GD=0.000000 E15.6, E15.6, E15.6, E15.6  
#X-start Y-start X-fin Y-fin Kode shear(m) reverse(m) dip angle top(km) bot(km)  
1 -35.00 -35.00 35.00 35.01 100 2.00 0.00 90.00 0.00 12.00 source  
1 -40.00 -5.00 -20.01 25.00 100 0.00 0.00 75.00 5.00 10.00 receiver-1  
1 60.00 50.50 70.10 75.05 100 0.00 0.00 45.00 5.00 10.00 receiver-2  
I3 G10.4 G10.4 G10.4 G10.4 I3 G10.4 G10.4 G10.4 G10.4 a30  
Grid Parameters  
1 Start-x=-100.0000 G16.7  
2 Start-y=-100.0000 G16.7  
3 Finish-x=100.0100 G16.7  
4 Finish-y=100.0100 G16.7  
5 x-increment=5.000000 G16.7  
6 y-increment=5.000000 G16.7  
Size Parameters  
1 Plot size=1.0000 G16.7  
2 Shade/Color increment=0.200000 G16.7  
3 Exaggeration for disp. & dist.=10000.00 G16.7  
Cross section default  
1 Start-x=-16.00000 G16.7  
2 Start-y=-16.00000 G16.7  
3 Finish-x=18.00000 G16.7  
4 Finish-y=26.00000 G16.7  
5 Distant-increment=1.000000 G16.7  
6 Z-depth=30.00000 G16.7  
7 Z-increment=1.000000 G16.7

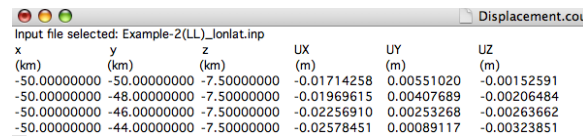
Input file with invisible mark (Format for Fortran 77)

## Numerical Output Files

In addition to Coulomb's internal graphics, you may want to analyse or plot the underlying numerical output, so all Coulomb graphics calculations produce a numerical output file with useful headers. These can be opened in Excel or brought into a rasterizing program for replotting.

### 9.1 Map view displacement output file

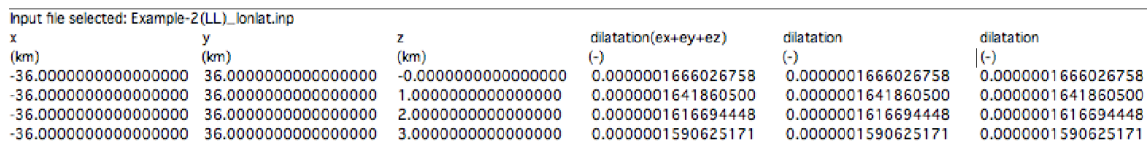
Every time when you click “Cal. & View” in the *Displacement control panel*, a text output file called “Displacement.cou” will be created or updated and saved in the sub-folder you designated in the Coulomb preferences menu (the default is “output\_files”). When you want to save your latest runs, remember to rename the “Displacement.cou” file within the “Output files” sub-folder; otherwise it will be overwritten by your future calculations. Here is an example of “Displacement.cou” text output file.



x (km)	y (km)	z (km)	UX (m)	UY (m)	UZ (m)
-50.00000000	-50.00000000	-7.50000000	-0.01714258	0.00551020	-0.00152591
-50.00000000	-48.00000000	-7.50000000	-0.01969615	0.00407689	-0.00206484
-50.00000000	-46.00000000	-7.50000000	-0.02256910	0.00253268	-0.00263662
-50.00000000	-44.00000000	-7.50000000	-0.02578451	0.00089117	-0.00323851

### 9.2 Map view strain output file

Every time when you click “Cal. & View” in the *Strain control panel*, a text output file called ‘strain.cou’ will be created or updated and saved in a sub-folder called “output files” within the “Coulomb 3.3 folder”. When you want to save your latest runs, remember to rename the ‘strain.cou’ file within the “output files” sub-folder; otherwise it will be written over by your future displacement calculations. Following is an example of ‘strain.cou’ text output file.



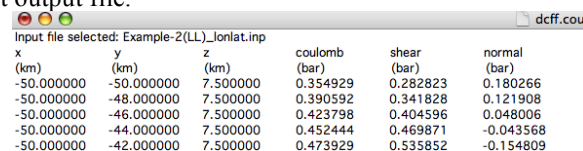
x (km)	y (km)	z (km)	dilatation(ex+ey+ez) (-)	dilatation (-)	dilatation (-)
-36.0000000000000000	36.0000000000000000	-0.0000000000000000	0.0000001666026758	0.0000001666026758	0.0000001666026758
-36.0000000000000000	36.0000000000000000	1.0000000000000000	0.0000001641860500	0.0000001641860500	0.0000001641860500
-36.0000000000000000	36.0000000000000000	2.0000000000000000	0.0000001616694448	0.0000001616694448	0.0000001616694448
-36.0000000000000000	36.0000000000000000	3.0000000000000000	0.0000001590625171	0.0000001590625171	0.0000001590625171

### 9.3 Cross-section dilatation output file

When you click “Cal. & View” in the *Strain control panel* and have selected the “Dilatation cross section” option, a text output file called “dilatation\_section.cou” will be created or updated and saved in the sub-folder.

### 9.4 Map view Coulomb stress output file

Every time when you click “Cal. & View” in the *Stress control panel*, a text output file called “dcff.cou” will be created or updated and saved. “Dcff” is an abbreviation for the change in the Coulomb failure function. When you want to save your latest runs, remember to rename the “dcff.cou” file within the “Output files” sub-folder; otherwise it will be written over by your future calculations. Following is an example of “dcff.cou” text output file.



x (km)	y (km)	z (km)	coulomb (bar)	shear (bar)	normal (bar)
-50.000000	-50.000000	7.500000	0.354929	0.282823	0.180266
-50.000000	-48.000000	7.500000	0.390592	0.341828	0.121908
-50.000000	-46.000000	7.500000	0.423798	0.404596	0.048006
-50.000000	-44.000000	7.500000	0.452444	0.469871	-0.043568
-50.000000	-42.000000	7.500000	0.473929	0.535852	-0.154809

### 9.5 Cross-section Coulomb stress output file

Every time when you click “Calc. & View” in the *Cross section control panel*, a text output file called “dcff\_section.cou” will be created or updated. Remember to rename it if you want to save the latest cross section run, because “dcff\_section.cou” will be overwritten. The following is an example of “dcff\_section.cou” text output file.

Input file selected: Example-2(LL)\_lonlat.inp

x	y	z	coulomb	shear	normal
(km)	(km)	(km)	(bar)	(bar)	(bar)
-36.000000	36.000000	-0.000000	0.440732	0.332070	0.271655
-36.000000	36.000000	1.000000	0.440016	0.332287	0.269323
-36.000000	36.000000	2.000000	0.438220	0.331613	0.266516
-36.000000	36.000000	3.000000	0.435482	0.330172	0.263275
-36.000000	36.000000	4.000000	0.431935	0.328079	0.259642

## 9.6 Element Conditions stress output file for “Calc. stress on faults” option

Every time when you select “Calc. stress on faults”, Coulomb produces an “Element\_conditions.csv” file with the results in tabular form. It includes not only the specified rake you selected for the calculation, but also the maximum (most positive) Coulomb stress change and the associated rake for this maximum.

Element\_conditions.csv

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
	Fault #	X-cent (km)	Y-cent (km)	Z-cent (km)	length (km)	strike (deg)	dip (deg)	lat-slip (m)	dip-slip (m)	sig-right (bar)	sig_rev (bar)	normal (bar)	coul-right (bar)	coul_rev (bar)	opt-rake (deg)	opt-coul (bar)	spec-rake (deg)	spec-coul (bar)	nt-rake (deg)	rake-coul (bar)
1	1	0.0	0.0	6.0	99.01	45	90	2	0	-23.39	0.00	0.00	-23.39	0.00	0	23.39	135	-16.54	0	-16.54
2	2	-37.4	-2.4	7.5	7.212	33.7	75	0	0	-1.93	0.08	1.64	-1.28	0.74	2.5	2.59	135	-0.65	0	-0.65
3	2	-33.4	3.6	7.5	7.212	33.7	75	0	0	-2.12	0.02	1.23	-1.62	0.52	0.6	2.61	135	-0.99	0	-0.99
4	2	-29.4	9.6	7.5	7.212	33.7	75	0	0	-2.10	-0.02	1.02	-1.69	0.39	-0.5	2.51	135	-1.09	0	-1.09

## 9.7 Numerical output file for Focal mechanism calculations, Focal\_mech\_stress.csv

Here is sample output of the focal mechanism file; you will see that it contains considerably more information than is contained in the graphical output.

Focal\_mech\_str

	A	B	C	D	E	F	G	H	I	J	K
	year	month	day	hour	minute	lon. (deg)	lat. (deg)	depth (km)	magnitude	strike1 (deg)	dip1 (deg)
1	2006	3	3	19	24	-122.20883	37.858665	8.97	2.82	80	85
2	2006	3	3	19	34	-122.21	37.857666	8.48	3.36	175	80
3	2006	3	3	19	34	-122.21	37.857666	8.48	3.36	80	75
4	2006	3	3	0	11	-121.14833	36.556168	7.7	3.17	130	70
5	2006	3	3	2	11	-121.54483	37.156666	8.39	2.16	335	45

ess\_output.csv

L	M	N	O	P	Q	R	S	T	U
rake1 (deg)	shear1 (bar)	normal1 (bar)	coulomb1 (bar)	strike2 (deg)	dip2 (deg)	rake2 (deg)	shear2 (bar)	normal2 (bar)	coulomb2 (bar)
-160	-0.135255	0.320712	-0.00697	348	70	-5	-0.134561	0.061826	-0.10983
20	-0.14941	0.080696	-0.117132	81	70	169	-0.14831	0.303649	-0.026851
-170	-0.127497	0.317226	-0.000607	347	80	-15	-0.125897	0.05679	-0.103181
-10	-0.747524	-0.001634	-0.748178	223	81	-160	-0.747265	0.252265	-0.646359
10	0.132575	-0.086132	0.098122	238	83	135	0.141864	1.499884	0.741818